



# User's Guide

*for*

## LibHuAirProp

Library of Psychrometric, Thermodynamic,  
and Transport Properties  
for *Real* Humid Air, Steam, Water, and Ice  
I-P & SI Units

## FluidDYM for DYMOLA<sup>®</sup>

Version 6.0

*Based on ASHRAE Research Project RP-1485  
and PTB-CP-3 Report*

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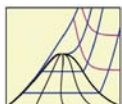
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Prepared by



**THERMO  
FLUID  
PROP**

[www.thermofluidprop.com](http://www.thermofluidprop.com)

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# LibHuAirProp Product Information

Do you need property values for moist air in I-P or SI units in your daily work?

► Use the property library LibHuAirProp ◀

Do you need these properties in Excel<sup>®</sup>, MATLAB<sup>®</sup>, Mathcad<sup>®</sup>, EES<sup>®</sup>, LabVIEW<sup>™</sup>, DYMOLA<sup>®</sup>, or SimulationX<sup>®</sup>?

► Use the add-ins FluidEXL, FluidLAB, FluidMAT, FluidEES, FluidVIEW, or FluidDYM ◀

What properties can be calculated using this software?

- thermodynamic properties      psychrometric functions ◀
- transport properties      backward functions ◀

What range of state is covered by this property library?

- unsaturated and saturated moist air ◀
- supersaturated moist air (liquid fog and ice fog) ◀
- temperatures from -143.15°C (-225.67°F) to 350°C (662°F) ◀
- pressures from 0.01 kPa (0.00145 psi) to 10,000 kPa (1450.4 psi) ◀

What are the references of LibHuAirProp?

Tables for moist air properties in the 2009 ASHRAE Handbook of Fundamentals were calculated using LibHuAirProp

Psychrometrics

1.3

Table 2 Thermodynamic Properties of Moist Air at Standard Atmospheric Pressure, 101.325 kPa

| Temp., °C<br><i>t</i> | Humidity Ratio<br><i>W</i> , kg <sub>a</sub> /kg <sub>da</sub> | Specific Volume, m <sup>3</sup> /kg <sub>da</sub> |                       |                       | Specific Enthalpy, kJ/kg <sub>da</sub> |                       |                       | Specific Entropy, kJ/(kg <sub>da</sub> ·K) |                       | Temp., °C<br><i>t</i> |
|-----------------------|----------------------------------------------------------------|---------------------------------------------------|-----------------------|-----------------------|----------------------------------------|-----------------------|-----------------------|--------------------------------------------|-----------------------|-----------------------|
|                       |                                                                | <i>v</i> <sub>da</sub>                            | <i>v</i> <sub>g</sub> | <i>v</i> <sub>s</sub> | <i>h</i> <sub>da</sub>                 | <i>h</i> <sub>g</sub> | <i>h</i> <sub>s</sub> | <i>s</i> <sub>da</sub>                     | <i>s</i> <sub>s</sub> |                       |
| -60                   | 0.0000067                                                      | 0.6027                                            | 0.0000                | 0.6027                | -60.341                                | 0.016                 | -60.325               | -0.2494                                    | -0.2494               | -60                   |
| -59                   | 0.0000076                                                      | 0.6055                                            | 0.0000                | 0.6055                | -59.335                                | 0.018                 | -59.317               | -0.2447                                    | -0.2446               | -59                   |
| -58                   | 0.0000087                                                      | 0.6084                                            | 0.0000                | 0.6084                | -58.329                                | 0.021                 | -58.308               | -0.2400                                    | -0.2399               | -58                   |
| -57                   | 0.0000100                                                      | 0.6112                                            | 0.0000                | 0.6112                | -57.323                                | 0.024                 | -57.299               | -0.2354                                    | -0.2353               | -57                   |
| -56                   | 0.0000114                                                      | 0.6141                                            | 0.0000                | 0.6141                | -56.317                                | 0.027                 | -56.289               | -0.2307                                    | -0.2306               | -56                   |
| -55                   | 0.0000129                                                      | 0.6169                                            | 0.0000                | 0.6169                | -55.311                                | 0.031                 | -55.280               | -0.2261                                    | -0.2260               | -55                   |
| -54                   | 0.0000147                                                      | 0.6198                                            | 0.0000                | 0.6198                | -54.305                                | 0.035                 | -54.269               | -0.2215                                    | -0.2213               | -54                   |
| -53                   | 0.0000167                                                      | 0.6226                                            | 0.0000                | 0.6226                | -53.299                                | 0.040                 | -53.258               | -0.2169                                    | -0.2167               | -53                   |
| -52                   | 0.0000190                                                      | 0.6255                                            | 0.0000                | 0.6255                | -52.293                                | 0.046                 | -52.247               | -0.2124                                    | -0.2121               | -52                   |
| -51                   | 0.0000215                                                      | 0.6283                                            | 0.0000                | 0.6283                | -51.287                                | 0.052                 | -51.235               | -0.2078                                    | -0.2076               | -51                   |

Thermodynamic and psychrometric property algorithms from ASHRAE Research Project 1485

## FINAL REPORT

### ASHRAE RP-1485

#### Thermodynamic Properties of Real Moist Air, Dry Air, Steam, Water, and Ice

By S. Herrmann<sup>a</sup>, H.-J. Kretschmar<sup>a</sup>, and D.P. Gatlley<sup>b</sup>

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November 17, 2008 (Submitted to TC for review)

March 12, 2009 (Final with corrections)

December 11, 2009 (revised Table C.2)

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#### Thermodynamic Properties of Real Moist Air, Dry Air, Steam, Water, and Ice (RP-1485)

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Received February 14, 2009; accepted May 6, 2009

This paper is based on findings resulting from ASHRAE Research Project RP-1485.

This research updates the modeling of moist air as a real gas mixture using the virial equation of state. It includes the Hyland and Wexler model (1983a, 1983b) and considers the Nelson-Sauer model (2002). All new National Institute of Standards and Technology reference equations and the latest International Association for the Properties of Water and Steam (IAPWS) standards, as well as the current values for the molar masses and gas constants, have been incorporated. The deviations of the proposed model to the Hyland-Wexler and Nelson-Sauer models are very low at ambient pressures but increase with increasing pressures and temperatures. The range of validity of the new model is in pressure from 0.01 kPa up to 10 MPa, in temperature from -143.15°C up to 350°C, and in humidity ratio from 0 kg<sub>a</sub>/kg<sub>da</sub> up to 10 kg<sub>a</sub>/kg<sub>da</sub>. This model was used to produce moist air and H<sub>2</sub>O saturation property tables for the psychrometric chapter in the 2009 ASHRAE Handbook—Fundamentals (ASHRAE 2009). The paper summarizes ASHRAE Research Project 1485 (RP-1485).

## Transport properties of moist air from the PTB Report PTB-CP-3 and the related paper in the Journal of Engineering for Gas Turbines and Power

### PTB Report

#### Determination of Thermodynamic and Transport Properties of Humid Air for Power-Cycle Calculations

By S. Herrmann<sup>1,2,3</sup>, H.-J. Kretzschmar<sup>1,4</sup>, V. Teske<sup>2,5</sup>, E. Voigt<sup>2</sup>, P. Ulbig<sup>6</sup>, R. Span<sup>7</sup>, D.P. Gatlley<sup>8</sup>

January 2009

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### Properties of Humid Air for Calculating Power Cycles

*Accurate calculation algorithms for the thermodynamic and transport properties of humid air are required for modeling compressed air energy-storage power cycles and designing their individual components. The development of such algorithms was part of the Advanced Adiabatic Compressed Air Energy Storage (AA-CAES) project, which had been supported by the European Commission. To obtain the statements of this paper, all available experimental data and new experimental data generated within the AA-CAES project were used as basis for comparisons between the different models for thermodynamic and transport properties. As a result, one model for calculating thermodynamic and one model for transport properties of humid air in AA-CAES cycle design and operation is recommended. Their application is possible for wide ranges of temperature from 243 K up to 2000 K, total pressure from 0.611 MPa up to 100 MPa, and water content up to 10%, must fraction with some restrictions concerning the calculation of viscosity  $\eta$  and thermal conductivity  $\lambda$  (up to 1000 K for both and up to 40 MPa for  $\lambda$ ). These models have been implemented into a property library, which meets the requirements of programs for calculating compressed air energy-storage cycles. The developed property library can be used for the daily work of an engineer who calculates such cycles. The results summarized in this paper have been used for preparing Section 6, "Real Gas" of the ASME Report No. STP-75-G12, "Thermophysical Properties of Gases used in Working Gas Turbine Applications." [DOI: 10.1115/1.4000611]*

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## Properties of dry air from the NIST Reference Equation of Lemmon et al. and properties of steam, water, and ice from the Industrial Formulation IAPWS-IF97, the Scientific Formulation IAPWS-95, and other current IAPWS formulations

### Thermodynamic Properties of Air and Mixtures of Nitrogen, Argon, and Oxygen From 60 to 2000 K at Pressures to 2000 MPa

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Received June 28, 1999; revised manuscript received December 2, 1999

A thermodynamic property formulation for standard dry air based upon available experimental  $p$ - $v$ - $T$ , heat capacity, speed of sound, and vapor-liquid equilibrium data is presented. This formulation is valid for liquid, vapor, and supercritical air at temperatures from the solidification point on the bubble-point curve (59.75 K) to 2000 K at pressures up to 2000 MPa. In the absence of reliable experimental data for air above 873 K and 70

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J. Phys. Chem. Ref. Data, Vol. 29, No. 3, 2000

### The International Association for the Properties of Water and Steam

Lucerne, Switzerland  
August 2007

Revised Release on the IAPWS Industrial Formulation 1997  
for the Thermodynamic Properties of Water and Steam  
(The revision only relates to the extension of region 5 to 50 MPa)

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### The International Association for the Properties of Water and Steam

Doorwerth, The Netherlands  
September 2009

Revised Release on the IAPWS Formulation 1995 for the Thermodynamic  
Properties of Ordinary Water Substance for General and Scientific Use

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## Who are the authors of LibHuAirProp?

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# Property Library for *Real* Humid Air, Steam, Water, and Ice

## ASHRAE-LibHuAirProp

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## 0 Package Contents

### Add-In for 32-bit version of DYMOLA®

The following ZIP file is delivered for your computer running a 32-bit version of DYMOLA®.

#### ZIP file "CD\_FluidDYM\_ASHRAE\_LibHuAirProp.zip" for DYMOLA®

The ZIP file contains the following files:

|                                              |                                                                 |
|----------------------------------------------|-----------------------------------------------------------------|
| FluidDYM_ASHRAE_LibHuAirProp_Users_Guide.pdf | User's Guide                                                    |
| FluidDYM_ASHRAE_LibHuAirProp_Setup.exe       | Installation program for the FluidDYM Add-In for use in DYMOLA® |

### Add-In for 64-bit version of DYMOLA®

The following ZIP file is delivered for your computer running a 64-bit version of DYMOLA®.

#### ZIP file "CD\_FluidDYM\_ASHRAE\_LibHuAirProp\_64.zip" for DYMOLA®

The ZIP file contains the following files:

|                                              |                                                                   |
|----------------------------------------------|-------------------------------------------------------------------|
| FluidDYM_ASHRAE_LibHuAirProp_Users_Guide.pdf | User's Guide                                                      |
| FluidDYM_ASHRAE_LibHuAirProp_64_Setup.msi    | - Self-extracting and self-installing program                     |
| Setup.exe                                    | - Installation program for the FluidDYM Add-In for use in DYMOLA® |





# **Part I-P Units**

# 1 Property Library ASHRAE-LibHuAirProp-IP

## 1.1 Function Overview

### 1.1.1 Function Overview for Real Moist Air

| Functional Dependence                 | Function Name     | Property or Function                                     | Unit of the Result   | Page |
|---------------------------------------|-------------------|----------------------------------------------------------|----------------------|------|
| $a = f(p, t, W)$                      | a_ptW_HAP_IP      | Thermal diffusivity                                      | ft <sup>2</sup> /s   | 3/2  |
| $\alpha_p = f(p, t, W)$               | alphap_ptW_HAP_IP | Relative pressure coefficient                            | 1/°R                 | 3/3  |
| $\beta_p = f(p, t, W)$                | betap_ptW_HAP_IP  | Isothermal stress coefficient                            | lb/ft <sup>3</sup>   | 3/4  |
| $c = f(p, t, W)$                      | c_ptW_HAP_IP      | Speed of sound                                           | ft/s                 | 3/5  |
| $c_p = f(p, t, W)$                    | cp_ptW_HAP_IP     | Specific isobaric heat capacity                          | Btu/(lb·°R)          | 3/6  |
| $c_v = f(p, t, W)$                    | cv_ptW_HAP_IP     | Specific isochoric heat capacity                         | Btu/(lb·°R)          | 3/7  |
| $f = f(p, t)$                         | f_pt_HAP_IP       | Enhancement factor (decimal ratio)                       | -                    | 3/8  |
| $h = f(p, t, W)$                      | h_ptW_HAP_IP      | Air-specific enthalpy                                    | Btu/lb <sub>a</sub>  | 3/9  |
| $\eta = f(p, t, W)$                   | Eta_ptW_HAP_IP    | Dynamic viscosity                                        | lb·s/ft <sup>2</sup> | 3/10 |
| $\kappa = f(p, t, W)$                 | Kappa_ptW_HAP_IP  | Isentropic exponent                                      | -                    | 3/11 |
| $\lambda = f(p, t, W)$                | Lambda_ptW_HAP_IP | Thermal conductivity                                     | Btu/(h·ft·°R)        | 3/12 |
| $\nu = f(p, t, W)$                    | Ny_ptW_HAP_IP     | Kinematic viscosity                                      | ft <sup>2</sup> /s   | 3/13 |
| $p = f(t, s, W)$                      | p_tsW_HAP_IP      | Pressure of humid air                                    | psi                  | 3/14 |
| $p = f(z_{\text{ele}})$               | p_zele_HAP_IP     | Pressure of humid air from elevation                     | psi                  | 3/15 |
| $p_{\text{Air}} = f(p, t, W)$         | pAIR_ptW_HAP_IP   | Partial pressure of dry air in moist air                 | psi                  | 3/16 |
| $p_{\text{H}_2\text{O}} = f(p, t, W)$ | pH2O_ptW_HAP_IP   | Partial pressure of water vapor in moist air             | psi                  | 3/17 |
| $p_{\text{H}_2\text{O}_s} = f(p, t)$  | pH2Os_pt_HAP_IP   | Partial saturation pressure of water vapour in moist air | psi                  | 3/18 |

| Functional Dependence                 | Function Name   | Property or Function                                                                                       | Unit of the Result               | Page |
|---------------------------------------|-----------------|------------------------------------------------------------------------------------------------------------|----------------------------------|------|
| $\phi = f(p, t, W)$                   | phi_ptW_HAP_IP  | Relative humidity (decimal ratio)                                                                          | -                                | 3/19 |
| $Pr = f(p, t, W)$                     | Pr_ptW_HAP_IP   | PRANDTL number                                                                                             | -                                | 3/20 |
| $\psi_{\text{Air}} = f(W)$            | PsiAir_W_HAP_IP | Mole fraction of dry air in moist air                                                                      | mol <sub>a</sub> /mol            | 3/21 |
| $\psi_{\text{H}_2\text{O}} = f(W)$    | PsiH2O_W_HAP_IP | Mole fraction of water vapor in moist air                                                                  | mol <sub>w</sub> /mol            | 3/22 |
| $\rho = f(p, t, W)$                   | Rho_ptW_HAP_IP  | Density                                                                                                    | lb/ft <sup>3</sup>               | 3/23 |
| $s = f(p, t, W)$                      | s_ptW_HAP_IP    | Air-specific entropy                                                                                       | Btu/(lb·°R)                      | 3/24 |
| $t = f(p, h, \phi)$                   | t_phphi_HAP_IP  | Backward function: temperature from total pressure, air-specific enthalpy and relative humidity            | °F                               | 3/25 |
| $t = f(p, h, W)$                      | t_phW_HAP_IP    | Backward function: temperature from total pressure, enthalpy and humidity ratio                            | °F                               | 3/26 |
| $t = f(p, s, W)$                      | t_psW_HAP_IP    | Backward function: temperature from total pressure, entropy and humidity ratio                             | °F                               | 3/27 |
| $t = f(p, t_{\text{wb}}, W)$          | t_ptwbW_HAP_IP  | Backward function: temperature from total pressure, wet-bulb temperature and humidity ratio                | °F                               | 3/28 |
| $t_d = f(p, W)$                       | td_pW_HAP_IP    | Dew-point/frost-point temperature                                                                          | °F                               | 3/29 |
| $t_s = f(p, p_{\text{H}_2\text{O}})$  | ts_ppH2O_HAP_IP | Backward function: saturation temperature of water from total pressure and partial pressure of water vapor | °F                               | 3/30 |
| $t_{\text{wb}} = f(p, t, W)$          | twb_ptW_HAP_IP  | Wet-bulb/ice-bulb temperature                                                                              | °F                               | 3/31 |
| $u = f(p, t, W)$                      | u_ptW_HAP_IP    | Air-specific internal energy                                                                               | Btu/lb <sub>a</sub>              | 3/32 |
| $v = f(p, t, W)$                      | v_ptW_HAP_IP    | Air-specific volume                                                                                        | ft <sup>3</sup> /lb <sub>a</sub> | 3/33 |
| $W = f(p, t, p_{\text{H}_2\text{O}})$ | W_ptpH2O_HAP_IP | Humidity ratio from total pressure, temperature, and partial pressure of water vapor                       | lb <sub>w</sub> /lb <sub>a</sub> | 3/34 |
| $W = f(p, t, \phi)$                   | W_ptphi_HAP_IP  | Humidity ratio from total pressure, temperature, and relative humidity                                     | lb <sub>w</sub> /lb <sub>a</sub> | 3/35 |
| $W = f(p, t_d)$                       | W_ptd_HAP_IP    | Humidity ratio from total pressure and dew-point temperature                                               | lb <sub>w</sub> /lb <sub>a</sub> | 3/36 |

| Functional Dependence | Function Name  | Property or Function                                                                 | Unit of the Result               | Page |
|-----------------------|----------------|--------------------------------------------------------------------------------------|----------------------------------|------|
| $W = f(p, t, t_{wb})$ | W_pttwb_HAP_IP | Humidity ratio from total pressure, (dry bulb) temperature, and wet-bulb temperature | lb <sub>w</sub> /lb <sub>a</sub> | 3/37 |
| $W_s = f(p, t)$       | Ws_pt_HAP_IP   | Saturation humidity ratio                                                            | lb <sub>w</sub> /lb <sub>a</sub> | 3/38 |
| $\xi_{Air} = f(W)$    | XiAir_W_HAP_IP | Mass fraction of dry air in moist air                                                | lb <sub>a</sub> /lb              | 3/39 |
| $\xi_{H2O} = f(W)$    | XiH2O_W_HAP_IP | Mass fraction of water vapor in moist air                                            | lb <sub>w</sub> /lb              | 3/40 |
| $Z = f(p, t, W)$      | Z_ptW_HAP_IP   | Compression factor (decimal ratio)                                                   | -                                | 3/41 |

## Range of Validity of Thermodynamic Properties

| Property               | Range of Validity |        |          |        |        |                                  |
|------------------------|-------------------|--------|----------|--------|--------|----------------------------------|
| Pressure:              | 0.00145           | $\leq$ | $p$      | $\leq$ | 1450.4 | psi                              |
| Temperature:           | -225.67           | $\leq$ | $t$      | $\leq$ | 662    | °F                               |
| Humidity ratio:        | 0                 | $\leq$ | $W$      | $\leq$ | 10     | lb <sub>w</sub> /lb <sub>a</sub> |
| Relative humidity:     | 0                 | $\leq$ | $\phi$   | $\leq$ | 1      | (decimal ratio)                  |
| Dew-point temperature: | -225.67           | $\leq$ | $t_d$    | $\leq$ | 662    | °F                               |
| Wet-bulb temperature:  | -225.67           | $\leq$ | $t_{wb}$ | $\leq$ | 662    | °F                               |

## Units

| Symbol   | Quantity              | Unit                                                     |
|----------|-----------------------|----------------------------------------------------------|
| $p$      | Pressure              | psi                                                      |
| $t$      | Temperature           | °F                                                       |
| $W$      | Humidity ratio        | lb <sub>w</sub> /lb <sub>a</sub> (lb water / lb dry air) |
| $\phi$   | Relative humidity     | (decimal ratio)                                          |
| $t_d$    | Dew point temperature | °F                                                       |
| $t_{wb}$ | Wet bulb temperature  | °F                                                       |

## Range of Validity of Transport Properties

| Property           | Range of Validity |        |        |        |        |                                  |
|--------------------|-------------------|--------|--------|--------|--------|----------------------------------|
| Pressure:          | 0.00145           | $\leq$ | $p$    | $\leq$ | 1450.4 | psi                              |
| Temperature:       | -99.67            | $\leq$ | $t$    | $\leq$ | 662    | °F                               |
| Humidity ratio:    | 0                 | $\leq$ | $W$    | $\leq$ | 10     | lb <sub>w</sub> /lb <sub>a</sub> |
| Relative humidity: | 0                 | $\leq$ | $\phi$ | $\leq$ | 1      | (decimal ratio)                  |

## Molar Masses

| Component | Molar Mass         | Reference |
|-----------|--------------------|-----------|
| Dry Air   | 63.859 lb/kmol     | [17]      |
| Water     | 39.7168998 lb/kmol | [5], [6]  |

## Reference States

| Property    | Dry Air       | Steam, Water, and Ice                      |
|-------------|---------------|--------------------------------------------|
| Pressure    | 14.6959 psi   | $p_s(32.018^\circ\text{F}) = 0.088714$ psi |
| Temperature | 32°F          | 32.018°F                                   |
| Enthalpy    | 0 Btu/lb      | 0.00026301926 Btu/lb                       |
| Entropy     | 0 Btu/(lb*°R) | 0 Btu/(lb*°R)                              |

### 1.1.2 Function Overview for Steam and Water for Temperatures $t \geq 32^\circ\text{F}$

| Functional Dependence      | Function Name | Property or Function                        | Unit of the Result | Page |
|----------------------------|---------------|---------------------------------------------|--------------------|------|
| $h_{\text{liq}} = f(p, t)$ | hliq_pt_97_IP | Specific enthalpy of liquid water           | Btu/lb             | 3/43 |
| $h_{\text{liq},s} = f(t)$  | hliqs_t_97_IP | Specific enthalpy of saturated liquid water | Btu/lb             | 3/44 |
| $h_{\text{vap},s} = f(t)$  | hvaps_t_97_IP | Specific enthalpy of saturated water vapor  | Btu/lb             | 3/45 |
| $p_s = f(t)$               | ps_t_97_IP    | Saturation pressure of water                | psi                | 3/46 |
| $s_{\text{liq}} = f(p, t)$ | sliq_pt_97_IP | Specific entropy of liquid water            | Btu/(lb·°R)        | 3/47 |
| $s_{\text{liq},s} = f(t)$  | sliqs_t_97_IP | Specific entropy of saturated liquid water  | Btu/(lb·°R)        | 3/48 |
| $s_{\text{vap},s} = f(t)$  | svaps_t_97_IP | Specific entropy of saturated water vapor   | Btu/(lb·°R)        | 3/49 |
| $t_s = f(p)$               | ts_p_97_IP    | Saturation temperature of water             | °F                 | 3/50 |
| $v_{\text{liq}} = f(p, t)$ | vliq_pt_97_IP | Specific volume of liquid water             | ft³/lb             | 3/51 |
| $v_{\text{liq},s} = f(t)$  | vliqs_t_97_IP | Specific volume of saturated liquid water   | ft³/lb             | 3/52 |
| $v_{\text{vap},s} = f(t)$  | vvaps_t_97_IP | Specific volume of saturated water vapor    | ft³/lb             | 3/53 |

**Range of Validity**

| Property     | Range of Validity |        |     |        |            |
|--------------|-------------------|--------|-----|--------|------------|
| Pressure:    | 0.00145           | $\leq$ | $p$ | $\leq$ | 1450.4 psi |
| Temperature: | 32                | $\leq$ | $t$ | $\leq$ | 662 °F     |

**Reference State**

| Property    | Water Vapor and Liquid Water               |
|-------------|--------------------------------------------|
| Pressure    | $p_s(32.018^\circ\text{F}) = 0.088714$ psi |
| Temperature | 32.018°F                                   |
| Enthalpy    | 0.00026301926 Btu/lb                       |
| Entropy     | 0 Btu/(lb*°R)                              |

**Units**

| Symbol | Quantity    | Unit |
|--------|-------------|------|
| $p$    | Pressure    | psi  |
| $t$    | Temperature | °F   |

### 1.1.3 Function Overview for Steam and Ice for Temperatures $t \leq 32^\circ\text{F}$

| Functional Dependence       | Function Name   | Property                                   | Unit of the Result | Page |
|-----------------------------|-----------------|--------------------------------------------|--------------------|------|
| $h_{\text{ice,sub}} = f(t)$ | hicesub_t_06_IP | Specific enthalpy of saturated ice         | Btu/lb             | 3/55 |
| $h_{\text{vap,sub}} = f(t)$ | hvapsub_t_95_IP | Specific enthalpy of saturated water vapor | Btu/lb             | 3/56 |
| $p_{\text{mel}} = f(t)$     | pmel_t_08_IP    | Melting pressure of ice                    | psi                | 3/57 |
| $p_{\text{sub}} = f(t)$     | psub_t_08_IP    | Sublimation pressure of ice                | psi                | 3/58 |
| $s_{\text{ice,sub}} = f(t)$ | sicesub_t_06_IP | Specific entropy of saturated ice          | Btu/(lb·°R)        | 3/59 |
| $s_{\text{vap,sub}} = f(t)$ | svapsub_t_95_IP | Specific entropy of saturated water vapor  | Btu/(lb·°R)        | 3/60 |
| $t_{\text{mel}} = f(p)$     | tmel_p_08_IP    | Melting temperature of ice                 | °F                 | 3/61 |
| $t_{\text{sub}} = f(p)$     | tsub_p_08_IP    | Sublimation temperature of ice             | °F                 | 3/62 |
| $v_{\text{ice,sub}} = f(t)$ | vicesub_t_06_IP | Specific volume of saturated ice           | ft³/lb             | 3/63 |
| $v_{\text{vap,sub}} = f(t)$ | vvapsub_t_95_IP | Specific volume of saturated water vapor   | ft³/lb             | 3/64 |



**Range of Validity**

| Property     | Range of Validity                                             |        |     |        |        |                    |
|--------------|---------------------------------------------------------------|--------|-----|--------|--------|--------------------|
| Pressure:    | $p_{\text{sub}}(-225.67^{\circ}\text{F}) = 1.7407\text{E-}12$ | $\leq$ | $p$ | $\leq$ | 1450.4 | psi                |
| Temperature: | -225.67                                                       | $\leq$ | $t$ | $\leq$ | 32     | $^{\circ}\text{F}$ |

**Units**

| Symbol | Quantity    | Unit               |
|--------|-------------|--------------------|
| $p$    | Pressure    | psi                |
| $t$    | Temperature | $^{\circ}\text{F}$ |

**Reference State**

| Property    | Water Vapor and Ice                                   |
|-------------|-------------------------------------------------------|
| Pressure    | $p_{\text{s}}(32.018^{\circ}\text{F}) = 0.088714$ psi |
| Temperature | 32.018 $^{\circ}\text{F}$                             |
| Enthalpy    | 0.00026301926 Btu/lb                                  |
| Entropy     | 0 Btu/(lb $^{\circ}\text{R}$ )                        |

## 1.2 Conversion of SI and I-P Units

| Property                                 | Conversion: SI Units → I-P Units                                                                           | Conversion: I-P Units → SI Units                                                                        | Units SI          | Units I-P            |
|------------------------------------------|------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------|-------------------|----------------------|
| Thermal diffusivity $a$                  | $\frac{a_{IP}}{\frac{ft^2}{s}} = \frac{a_{SI}}{\frac{m^2}{s}} \times 10.76391042$                          | $\frac{a_{SI}}{\frac{m^2}{s}} = \frac{a_{IP}}{\frac{ft^2}{s}} \times 0.0929304$                         | m <sup>2</sup> /s | ft <sup>2</sup> /s   |
| Relative pressure coefficient $\alpha_p$ | $\frac{\alpha_{p,IP}}{\frac{1}{^\circ R}} = \frac{\alpha_{p,SI}}{\frac{1}{K}} \times \frac{9}{5}$          | $\frac{\alpha_{p,SI}}{\frac{1}{K}} = \frac{\alpha_{p,IP}}{\frac{1}{^\circ R}} \times \frac{5}{9}$       | 1/K               | 1/°R                 |
| Isothermal stress coefficient $\beta_p$  | $\frac{\beta_{p,IP}}{\frac{lb}{ft^3}} = \frac{\beta_{p,SI}}{\frac{kg}{m^3}} \times 0.062428$               | $\frac{\beta_{p,SI}}{\frac{kg}{m^3}} = \frac{\beta_{p,IP}}{\frac{lb}{ft^3}} \times 16.018463$           | kg/m <sup>3</sup> | lb/ft <sup>3</sup>   |
| Speed of sound $c$                       | $\frac{c_{IP}}{\frac{ft}{s}} = \frac{c_{SI}}{\frac{m}{s}} \times 3.2808399$                                | $\frac{c_{SI}}{\frac{m}{s}} = \frac{c_{IP}}{\frac{ft}{s}} \times 0.3048$                                | m/s               | ft/s                 |
| Specific isobaric heat capacity $c_p$    | $\frac{c_{p,IP}}{\frac{Btu}{lb \cdot ^\circ R}} = \frac{c_{p,SI}}{\frac{kJ}{kg \cdot K}} \times 0.2388459$ | $\frac{c_{p,SI}}{\frac{kJ}{kg \cdot K}} = \frac{c_{p,IP}}{\frac{Btu}{lb \cdot ^\circ R}} \times 4.1868$ | kJ/(kg·K)         | Btu/(lb·°R)          |
| Specific isochoric heat capacity $c_v$   | $\frac{c_{v,IP}}{\frac{Btu}{lb \cdot ^\circ R}} = \frac{c_{v,SI}}{\frac{kJ}{kg \cdot K}} \times 0.2388459$ | $\frac{c_{v,SI}}{\frac{kJ}{kg \cdot K}} = \frac{c_{v,IP}}{\frac{Btu}{lb \cdot ^\circ R}} \times 4.1868$ | kJ/(kg·K)         | Btu/(lb·°R)          |
| Dynamic viscosity $\eta$                 | $\frac{\eta_{IP}}{\frac{lb \cdot s}{ft^2}} = \frac{\eta_{SI}}{\frac{Pa \cdot s}{s}} \times 0.02088543$     | $\frac{\eta_{SI}}{\frac{Pa \cdot s}{s}} = \frac{\eta_{IP}}{\frac{lb \cdot s}{ft^2}} \times 47.880259$   | Pa·s              | lb·s/ft <sup>2</sup> |
| Enhancement factor $f$                   | $f_{IP} = f_{SI}$                                                                                          | $f_{SI} = f_{IP}$                                                                                       | -                 | -                    |

| Property                                             | Conversion: SI Units → I-P Units                                                                                                                            | Conversion: I-P Units → SI Units                                                                                                                                        | Units SI                | Units I-P                 |
|------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------|---------------------------|
| Air-specific enthalpy<br>(moist air) $h$             | $\frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}_a}} = \frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}_a}} \times 0.4299226 + 7.68565365666$                             | $\frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}_a}} = \left( \frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}_a}} - 7.68565365666 \right) \times 2.326$                              | kJ/kg <sub>a</sub>      | Btu/lb <sub>a</sub>       |
| Specific enthalpy<br>(water, water vapor, ice) $h_w$ | $\frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}}} = \frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}}} \times 0.4299226$                                                 | $\frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}}} = \frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}}} \times 2.326$                                                                 | kJ/kg                   | Btu/lb                    |
| Isentropic exponent $\kappa$                         | $\kappa_{IP} = \kappa_{SI}$                                                                                                                                 | $\kappa_{SI} = \kappa_{IP}$                                                                                                                                             | -                       | -                         |
| Thermal conductivity $\lambda$                       | $\frac{\lambda_{IP}}{\frac{\text{Btu}}{\text{h ft } ^\circ\text{R}}} = \frac{\lambda_{SI}}{\frac{\text{W}}{\text{m K}}} \times 0.57778932$                  | $\frac{\lambda_{SI}}{\frac{\text{W}}{\text{m K}}} = \frac{\lambda_{IP}}{\frac{\text{Btu}}{\text{h ft } ^\circ\text{R}}} \times 1.73073467$                              | W/(m·K)                 | Btu/(h·ft·°R)             |
| Kinematic viscosity $\nu$                            | $\frac{\nu_{IP}}{\frac{\text{ft}^2}{\text{s}}} = \frac{\nu_{SI}}{\frac{\text{m}^2}{\text{s}}} \times 10.763910417$                                          | $\frac{\nu_{SI}}{\frac{\text{m}^2}{\text{s}}} = \frac{\nu_{IP}}{\frac{\text{ft}^2}{\text{s}}} \times 0.092903040$                                                       | m <sup>2</sup> /s       | ft <sup>2</sup> /s        |
| Pressure $p$                                         | $\frac{p_{IP}}{\text{psi}} = \frac{p_{SI}}{\text{kPa}} \times 0.14503774$                                                                                   | $\frac{p_{SI}}{\text{kPa}} = \frac{p_{IP}}{\text{psi}} \times 6.894757$                                                                                                 | kPa                     | psi                       |
| Relative humidity $\phi$                             | $\phi_{IP} = \phi_{SI}$                                                                                                                                     | $\phi_{SI} = \phi_{IP}$                                                                                                                                                 | -                       | -                         |
| Prandtl number $Pr$                                  | $Pr_{IP} = Pr_{SI}$                                                                                                                                         | $Pr_{SI} = Pr_{IP}$                                                                                                                                                     | -                       | -                         |
| Mole fraction $\psi$                                 | $\psi_{IP} = \psi_{SI}$                                                                                                                                     | $\psi_{SI} = \psi_{IP}$                                                                                                                                                 | mol/mol                 | mol/mol                   |
| Density $\rho$                                       | $\frac{\rho_{IP}}{\frac{\text{lb}}{\text{ft}^3}} = \frac{\rho_{SI}}{\frac{\text{kg}}{\text{m}^3}} \times 0.062428$                                          | $\frac{\rho_{SI}}{\frac{\text{kg}}{\text{m}^3}} = \frac{\rho_{IP}}{\frac{\text{lb}}{\text{ft}^3}} \times 16.018463$                                                     | kg/m <sup>3</sup>       | lb/ft <sup>3</sup>        |
| Air-specific entropy<br>(moist air) $s$              | $\frac{s_{IP}}{\frac{\text{Btu}}{\text{lb}_a } ^\circ\text{R}}} = \frac{s_{SI}}{\frac{\text{kJ}}{\text{kg}_a } \text{K}}} \times 0.2388459 + 0.01616365106$ | $\frac{s_{SI}}{\frac{\text{kJ}}{\text{kg}_a } \text{K}}} = \left( \frac{s_{IP}}{\frac{\text{Btu}}{\text{lb}_a } ^\circ\text{R}}} - 0.01616365106 \right) \times 4.1868$ | kJ/(kg <sub>a</sub> ·K) | Btu/(lb <sub>a</sub> ·°R) |

| Property                                            | Conversion: SI Units → I-P Units                                                                                                                                                                                                                                     | Conversion: I-P Units → SI Units                                                                                                                                                                                                                                                 | Units SI                                 | Units I-P                                       |
|-----------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------|-------------------------------------------------|
| Specific entropy<br>(water, water vapor, ice) $s_w$ | $\frac{s_{IP}}{\frac{\text{Btu}}{\text{lb}_a \cdot ^\circ\text{R}}} = \frac{s_{SI}}{\frac{\text{kJ}}{\text{kg}_a \cdot \text{K}}} \times 0.23884589$                                                                                                                 | $\frac{s_{SI}}{\frac{\text{kJ}}{\text{kg}_a \cdot \text{K}}} = \frac{s_{IP}}{\frac{\text{Btu}}{\text{lb}_a \cdot ^\circ\text{R}}} \times 4.1868$                                                                                                                                 | $\text{kJ}/(\text{kg}_a \cdot \text{K})$ | $\text{Btu}/(\text{lb}_a \cdot ^\circ\text{R})$ |
| Temperature $t$                                     | $\frac{t_{IP}}{^\circ\text{F}} = \frac{t_{SI}}{^\circ\text{C}} \times \frac{9}{5} + 32$                                                                                                                                                                              | $\frac{t_{SI}}{^\circ\text{C}} = \left( \frac{t_{IP}}{^\circ\text{F}} - 32 \right) \times \frac{5}{9}$                                                                                                                                                                           | $^\circ\text{C}$                         | $^\circ\text{F}$                                |
| Air-specific internal energy<br>(moist air) $u$     | $(u = h - pv)$ $\frac{u_{IP}}{\frac{\text{Btu}}{\text{lb}_a}} = \frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}_a}} \times 0.4299226 + 7.68565365666$ $- \frac{p_{SI}}{\text{kPa}} \times 0.145037738 \cdot \frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}_a}} \times 16.018453$ | $(u = h - pv)$ $\frac{u_{SI}}{\frac{\text{kJ}}{\text{kg}_a}} = \left( \frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}_a}} - 7.68565365666 \right) \times 2.236$ $- \frac{p_{IP}}{\text{psi}} \times 6.894757293 \cdot \frac{v_{SIP}}{\frac{\text{ft}^3}{\text{lb}_a}} \times 0.062428$ | $\text{kJ}/\text{kg}_a$                  | $\text{Btu}/\text{lb}$                          |
| Air-specific volume<br>(moist air) $v$              | $\frac{v_{IP}}{\frac{\text{ft}^3}{\text{lb}_a}} = \frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}_a}} \times 16.018453$                                                                                                                                                    | $\frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}_a}} = \frac{v_{IP}}{\frac{\text{ft}^3}{\text{lb}_a}} \times 0.062428$                                                                                                                                                                 | $\text{m}^3/\text{kg}_a$                 | $\text{ft}^3/\text{lb}_a$                       |
| Specific volume<br>(water, water vapor, ice) $v_w$  | $\frac{v_{IP}}{\frac{\text{ft}^3}{\text{lb}}} = \frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}}} \times 16.018453$                                                                                                                                                        | $\frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}}} = \frac{v_{IP}}{\frac{\text{ft}^3}{\text{lb}}} \times 0.062428$                                                                                                                                                                     | $\text{m}^3/\text{kg}$                   | $\text{ft}^3/\text{lb}$                         |
| Humidity ratio $W$                                  | $W_{IP} = W_{SI}$                                                                                                                                                                                                                                                    | $W_{SI} = W_{IP}$                                                                                                                                                                                                                                                                | $\text{kg}_w/\text{kg}_a$                | $\text{lb}_w/\text{lb}_a$                       |
| Mass fraction $\zeta$                               | $\zeta_{IP} = \zeta_{SI}$                                                                                                                                                                                                                                            | $\zeta_{SI} = \zeta_{IP}$                                                                                                                                                                                                                                                        | $\text{kg}_w/\text{kg}$                  | $\text{lb}_w/\text{lb}$                         |
| Compression factor $Z$                              | $Z_{IP} = Z_{SI}$                                                                                                                                                                                                                                                    | $Z_{SI} = Z_{IP}$                                                                                                                                                                                                                                                                | -                                        | -                                               |

## 1.3 Calculation Algorithms

### 1.3.1 Algorithms for Real Moist Air

The properties of moist air are calculated from the modified Hyland-Wexler model given in Herrmann, Kretschmar, and Gatley (HKG) [1], [2]. The modifications incorporate:

- the value for the universal molar gas constant from the CODATA standard by Mohr and Taylor [22]
- the value for the molar mass of dry air from Gatley et al. [17] and that of water from IAPWS-95 [5], [6]
- the calculation of the ideal-gas parts of the heat capacity, enthalpy, and entropy for dry air from the fundamental equation of Lemmon et al. [14]
- the calculation of the ideal-gas parts of the heat capacity, enthalpy, and entropy for water vapor from IAPWS-IF97 [7], [8], [9] for  $t \geq 32^\circ\text{F}$  and from IAPWS-95 [5], [6] for  $t \leq 32^\circ\text{F}$
- the calculation of the vapor-pressure enhancement factor from the equation given by the models of Hyland and Wexler [21]
- the calculation of the second and third molar virial coefficients  $B_{aa}$  and  $C_{aaa}$  for dry air from the fundamental equation of Lemmon et al. [14]
- the calculation of the second and third molar virial coefficients  $B_{ww}$  and  $C_{www}$  for water and steam from IAPWS-95 [5], [6]
- the calculation of the air-water second molar cross-virial coefficient  $B_{aw}$  from Harvey and Huang [15]
- the calculation of the air-water third molar cross-virial coefficients  $C_{aaw}$  and  $C_{aww}$  from Nelson and Sauer [12], [13]
- the calculation of the saturation pressure of water from IAPWS-IF97 [7], [8], [9] for  $t \geq 32^\circ\text{F}$  and of the sublimation pressure of water from IAPWS-08 [11] for  $t \leq 32^\circ\text{F}$
- the calculation of the isothermal compressibility of saturated liquid water from IAPWS-IF97 [7], [8], [9] for  $t \geq 32^\circ\text{F}$  and that of ice from IAPWS-06 [10] for  $t \leq 32^\circ\text{F}$  in the determination of the vapor-pressure enhancement factor
- the calculation of Henry's constant from the IAPWS Guideline 2004 [16] in the determination of the enhancement factor. The mole fractions for the three main components of dry air were taken from Lemmon et al. [14]. Argon was not considered in the calculation of Henry's constant in the former research projects, but it is now the third component of dry air.

### 1.3.2 Algorithms for Steam and Water for Temperatures $t \geq 32^\circ\text{F}$

The  $p$ - $T$  diagram in Fig. 1 shows the formulations used for water and water vapor. The temperature range above  $32^\circ\text{F}$  is covered by IAPWS-IF97 [7], [8], [9]:

- The saturation line is calculated from the IAPWS-IF97 saturation pressure equation  $p_s^{97}(t)$  and saturation temperature equation  $t_s^{97}(p)$ .
- The properties in the liquid region including saturated-liquid line are calculated from the fundamental equation of the IAPWS-IF97 region 1.
- The properties in the vapor region including saturated-vapor line are calculated from the fundamental equation of the IAPWS-IF97 region 2.

### 1.3.3 Algorithms for Steam and Ice for Temperatures $t \leq 32^\circ\text{F}$

- The sublimation curve is covered by the IAPWS-08 sublimation pressure equation  $p_{\text{subl}}^{08}(t)$  [11] (see Fig. 1).
- The properties of ice including saturated ice are determined by the fundamental equation of the IAPWS-06 [10].
- The properties of vapor including saturated vapor are calculated from the fundamental equation of IAPWS-95 [5], [6].

### 1.3.4 Overview of the Applied Formulations for Steam, Water, and Ice

The following  $p$ - $T$  diagram shows the used IAPWS Formulations and the ranges where they are applied.

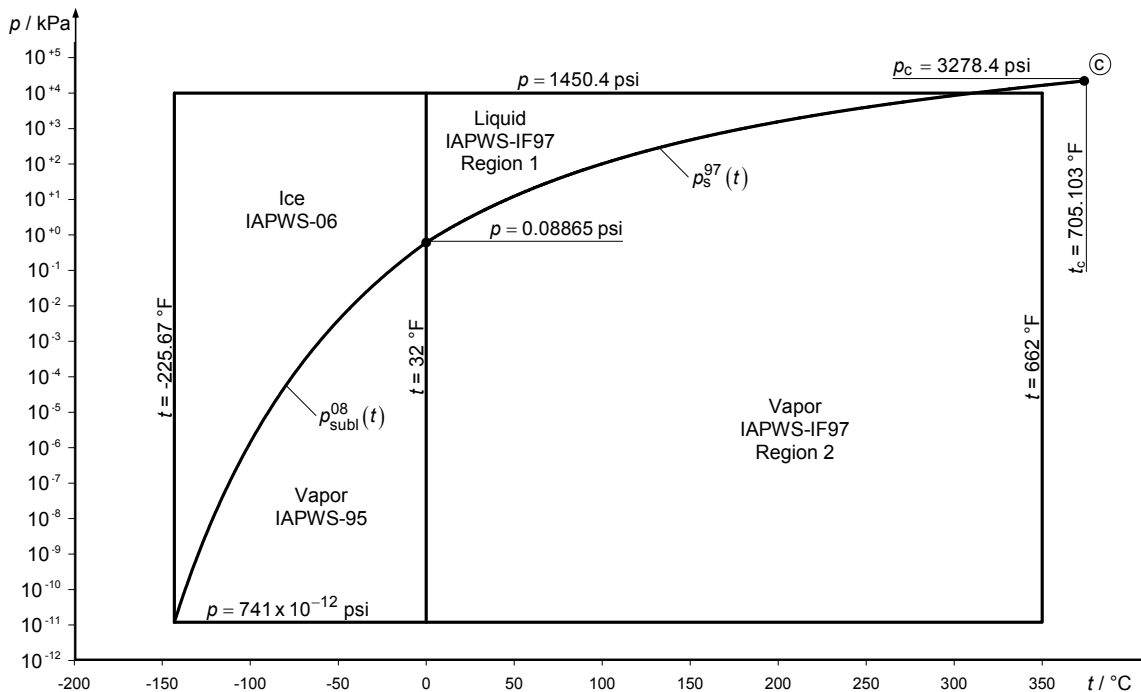


Figure 1:  $p$ - $T$  diagram with used IAPWS formulations for steam, water, and ice.

## 2 Add-In FluidDYM for DYMOLA<sup>®</sup> for ASHRAE-LibHuAirProp-IP

### 2.1 Installing FluidDYM

The FluidDYM Add-In has been developed to calculate thermophysical properties in DYMOLA<sup>®</sup> more conveniently. Within DYMOLA<sup>®</sup>, it enables the direct call of functions relating to real moist air, steam, water, and ice from the ASHRAE-LibHuAirProp-IP property library.

The 32-bit version of FluidDYM LibHuAirProp runs on both the 32-bit and 64-bit version of DYMOLA<sup>®</sup>.

#### 2.1.1 Installing FluidDYM including LibHuAirProp

In this section, the installation of FluidDYM and LibHuAirProp is described.

Before you begin, it is best to close any Windows<sup>®</sup> applications, since Windows<sup>®</sup> may need to be rebooted during the installation process.

After you have downloaded and extracted the zip-file

"CD\_FluidDYM\_ASHRE\_LibHuAirProp.zip," (32-bit version)

"CD\_FluidDYM\_ASHRE\_LibHuAirProp\_64.zip," (64-bit version)

you will see the folder

CD\_FluidDYM\_ASHRAE\_LibHuAirProp (32-bit version)

CD\_FluidDYM\_ASHRAE\_LibHuAirProp\_64 (64-bit version)

in your Windows Explorer<sup>®</sup>, Norton Commander<sup>®</sup> etc.

Now, open this folder by double-clicking on it.

Within the folder for the **32-bit version** you will see the following files

FluidDYM\_ASHRAE\_LibHuAirProp\_Users\_Guide.pdf

FluidDYM\_LibHuAirProp\_Setup.exe (32-bit version)

and the folder

"Users\_Guide."

Within the folder for the **64-bit version** you will see the following files

FluidDYM\_ASHRAE\_LibHuAirProp\_Users\_Guide.pdf

FluidDYM\_ASHRAE\_LibHuAirProp\_64\_Setup.msi

Setup.exe

and the folder

"Users\_Guide."

In order to run the installation of **32-bit** FluidDYM including the LibHuAirProp property library double-click the file

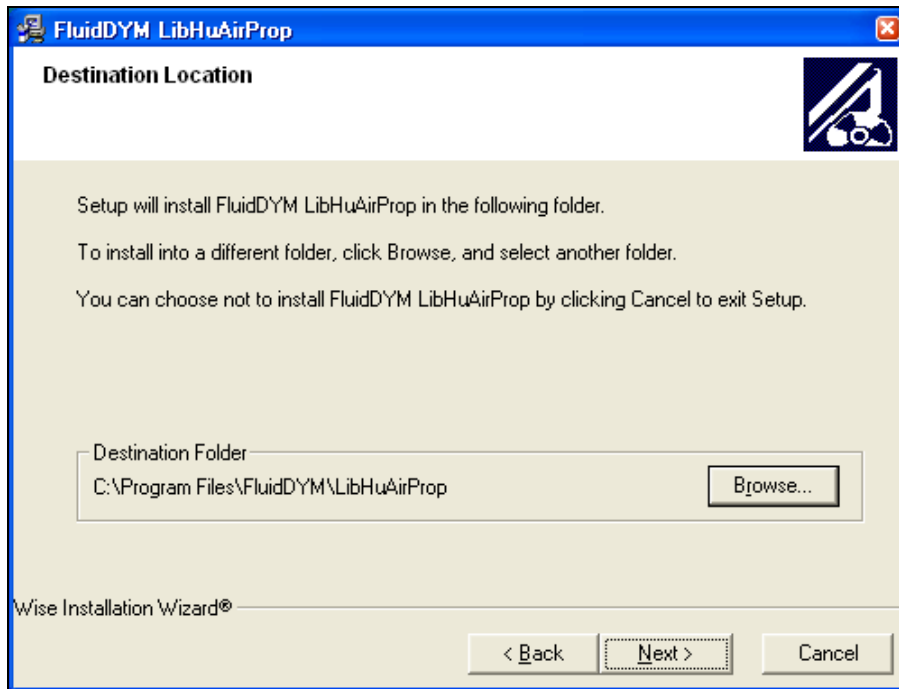
FluidDYM\_LibHuAirProp\_Setup.exe.

Installation may start with a window noting that all Windows® programs should be closed. When this is the case, the installation can be continued. Click the "Continue" button.

In the following dialog box, "Choose Destination Location," the default path offered automatically for the installation of FluidDYM is

C:\Program Files\FluidDYM\LibHuAirProp.

By clicking the "Browse..." button, you can change the installation directory before installation (see figure below).



**Figure 2.1.1:** "Choose Destination Location"

Finally, click on "Next >" to continue installation; click "Next >" again in the "Start Installation" window which follows in order to start the installation of FluidDYM.

After FluidDYM has been installed, you will see the sentence "FluidDYM LibHuAirProp has been successfully installed." Confirm this by clicking the "Finish" button.

The installation of FluidDYM 32-bit has been completed.

In order to run the installation of **64-bit** FluidDYM including the LibHuAirProp property library double-click the file

Setup.exe.

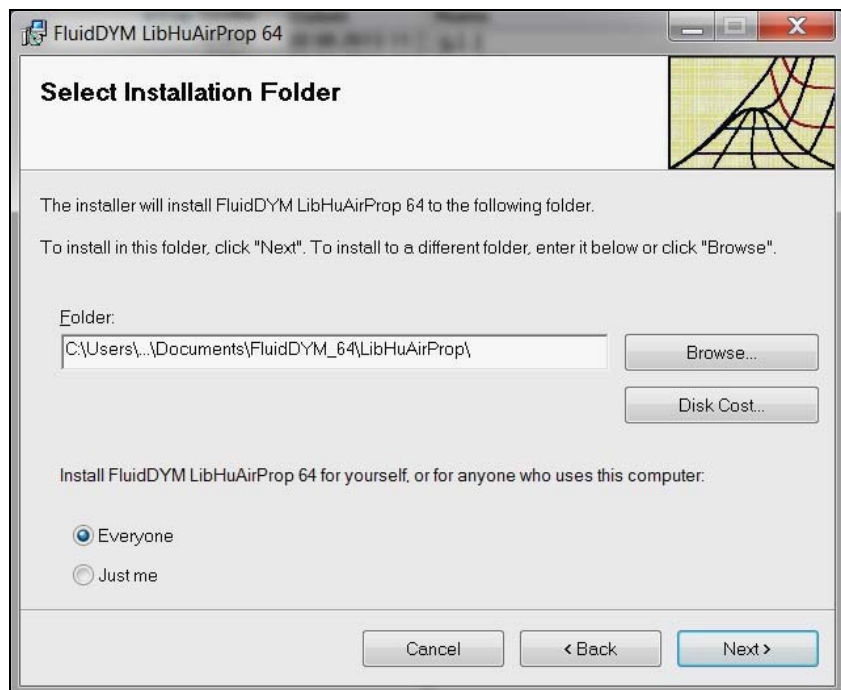
Installation may start with a window noting that all Windows® programs should be closed. When this is the case, the installation can be continued. Click the "Continue" button.

In the following dialog box, "Choose Destination Location," the default path offered automatically for the installation of FluidDYM is

C:\Users\...\Documents\FluidDYM\_64\LibHuAirProp.



By clicking the "Browse..." button, you can change the installation directory before installation (see figure below).



**Figure 2.1.2:** "Choose Destination Location"

Finally, click on "Next >" to continue installation; click "Next >" again in the "Start Installation" window which follows in order to start the installation of FluidDYM.

After FluidDYM has been installed, you will see the sentence "FluidDYM LibHuAirProp has been successfully installed." Confirm this by clicking the "Finish" button.

The installation of FluidDYM 64-bit has been completed.

The installation program has copied the following files for both the I-P and the SI version into the directory "C:\Program Files\FluidDYM\LibHuAirProp":

- Dynamic link libraries "LibHuAirProp\_IP.dll" and "LibHuAirProp\_SI.dll"
- Link up dynamic link libraries "LibHuAirProp\_IP\_Dymola.dll", "LibHuAirProp\_SI\_Dymola.dll" and other necessary system DLL files
- Library files "LibHuAirProp\_IP\_Dymola.lib" and "LibHuAirProp\_SI\_Dymola.lib"
- Header files "LibHuAirProp\_IP\_Dymola.h", "LibHuAirProp\_SI\_Dymola.h"
- Modelica file "FluidDYM\_LibHuAirProp\_IP.mo" including the following property functions:

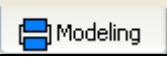
|                   |                 |
|-------------------|-----------------|
| a_ptW_HAP_IP      | v_ptW_HAP_IP    |
| alphap_ptW_HAP_IP | W_ptpH2O_HAP_IP |
| betap_ptW_HAP_IP  | W_ptphi_HAP_IP  |
| c_ptW_HAP_IP      | W_ptd_HAP_IP    |
| cp_ptW_HAP_IP     | W_pttwb_HAP_IP  |
| cv_ptW_HAP_IP     | Ws_pt_HAP_IP    |
| f_pt_HAP_IP       | XiAir_W_HAP_IP  |
| h_ptW_HAP_IP      | XiH2O_W_HAP_IP  |
| Eta_ptW_HAP_IP    | Z_ptW_HAP_IP    |
| Kappa_ptW_HAP_IP  | hliq_pt_97_IP   |
| Lambda_ptW_HAP_IP | hliqs_t_97_IP   |
| Ny_ptW_HAP_IP     | hvaps_t_97_IP   |
| p_tsW_HAP_IP      | ps_t_97_IP      |
| p_zele_HAP_IP     | sliq_pt_97_IP   |
| pAIR_ptW_HAP_IP   | sliqs_t_97_IP   |
| pH2O_ptW_HAP_IP   | svaps_t_97_IP   |
| pH2Os_pt_HAP_IP   | ts_p_97_IP      |
| phi_ptW_HAP_IP    | vliq_pt_97_IP   |
| Pr_ptW_HAP_IP     | vliqs_t_97_IP   |
| PsiAir_W_HAP_IP   | vvaps_t_97_IP   |
| PsiH2O_W_HAP_IP   | hicesub_t_06_IP |
| Rho_ptW_HAP_IP    | hvapsub_t_95_IP |
| s_ptW_HAP_IP      | pmel_t_08_IP    |
| t_phW_HAP_IP      | psub_t_08_IP    |
| t_psW_HAP_IP      | sicesub_t_06_IP |
| t_ptwbW_HAP_IP    | svapsub_t_95_IP |
| td_pW_HAP_IP      | tmel_p_08_IP    |
| ts_ppH2Os_HAP_IP  | tsub_p_08_IP    |
| twb_ptW_HAP_IP    | vicesub_t_06_IP |
| u_ptW_HAP_IP      | vvapsub_t_95_IP |

- Modelica file "FluidDYM\_LibHuAirProp\_SI.mo" including the following property functions:

|                   |                 |
|-------------------|-----------------|
| a_ptW_HAP_SI      | v_ptW_HAP_SI    |
| alphap_ptW_HAP_SI | W_ptpH2O_HAP_SI |
| betap_ptW_HAP_SI  | W_ptphi_HAP_SI  |
| c_ptW_HAP_SI      | W_ptd_HAP_SI    |
| cp_ptW_HAP_SI     | W_pttwb_HAP_SI  |
| cv_ptW_HAP_SI     | Ws_pt_HAP_SI    |
| f_pt_HAP_SI       | XiAir_W_HAP_SI  |
| h_ptW_HAP_SI      | XiH2O_W_HAP_SI  |
| Eta_ptW_HAP_SI    | Z_ptW_HAP_SI    |
| Kappa_ptW_HAP_SI  | hliq_pt_97_SI   |
| Lambda_ptW_HAP_SI | hliqs_t_97_SI   |
| Ny_ptW_HAP_SI     | hvaps_t_97_SI   |
| p_tsW_HAP_SI      | ps_t_97_SI      |
| p_zele_HAP_SI     | sliq_pt_97_SI   |
| pAIR_ptW_HAP_SI   | sliqs_t_97_SI   |
| pH2O_ptW_HAP_SI   | svaps_t_97_SI   |
| pH2Os_pt_HAP_SI   | ts_p_97_SI      |
| phi_ptW_HAP_SI    | vliq_pt_9_SI    |
| PR_ptW_HAP_SI     | vliqs_t_97_SI   |
| PsiAir_W_HAP_SI   | vvaps_t_97_SI   |
| PsiH2O_W_HAP_SI   | hicesub_t_06_SI |
| Rho_ptW_HAP_SI    | hvapsub_t_95_SI |
| s_ptW_HAP_SI      | pmel_t_08_SI    |
| t_phW_HAP_SI      | psub_t_08_SI    |
| t_psW_HAP_SI      | sicesub_t_06_SI |
| t_ptwbW_HAP_SI    | svapsub_t_95_SI |
| td_pW_HAP_SI      | tmel_p_08_SI    |
| ts_ppH2Os_HAP_SI  | tsub_p_08_SI    |
| twb_ptW_HAP_SI    | vicesub_t_06_SI |
| u_ptW_HAP_SI      | vvapsub_t_95_SI |

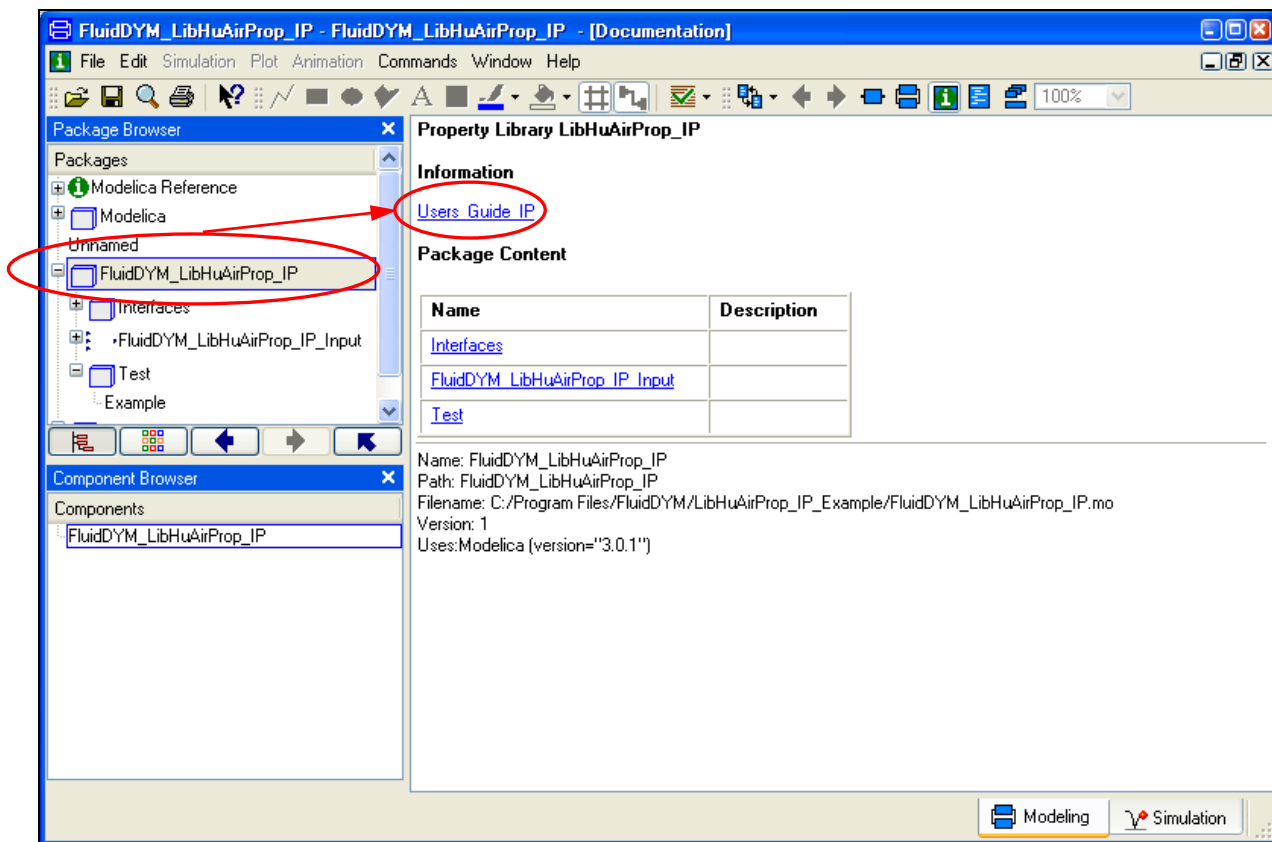
### 2.1.2 The FluidDYM Help System

Dymola® provides detailed help functions. You can choose to read the program documentation or the help page of a specific property function, as desired.

Within the "Modeling-Mode"  the help may be accessed via two different steps.

First we will show you how to access the program documentation of the property library.

- Make sure Dymola is set to the "Modeling-Mode".
- Now click the  button in the Dymola menu bar to choose the "Documentation Mode".
- Double-click on the "FluidDYM\_LibHuAirProp\_IP" block on the left and then click on "Users\_Guide" (see Figure 2.1.3).

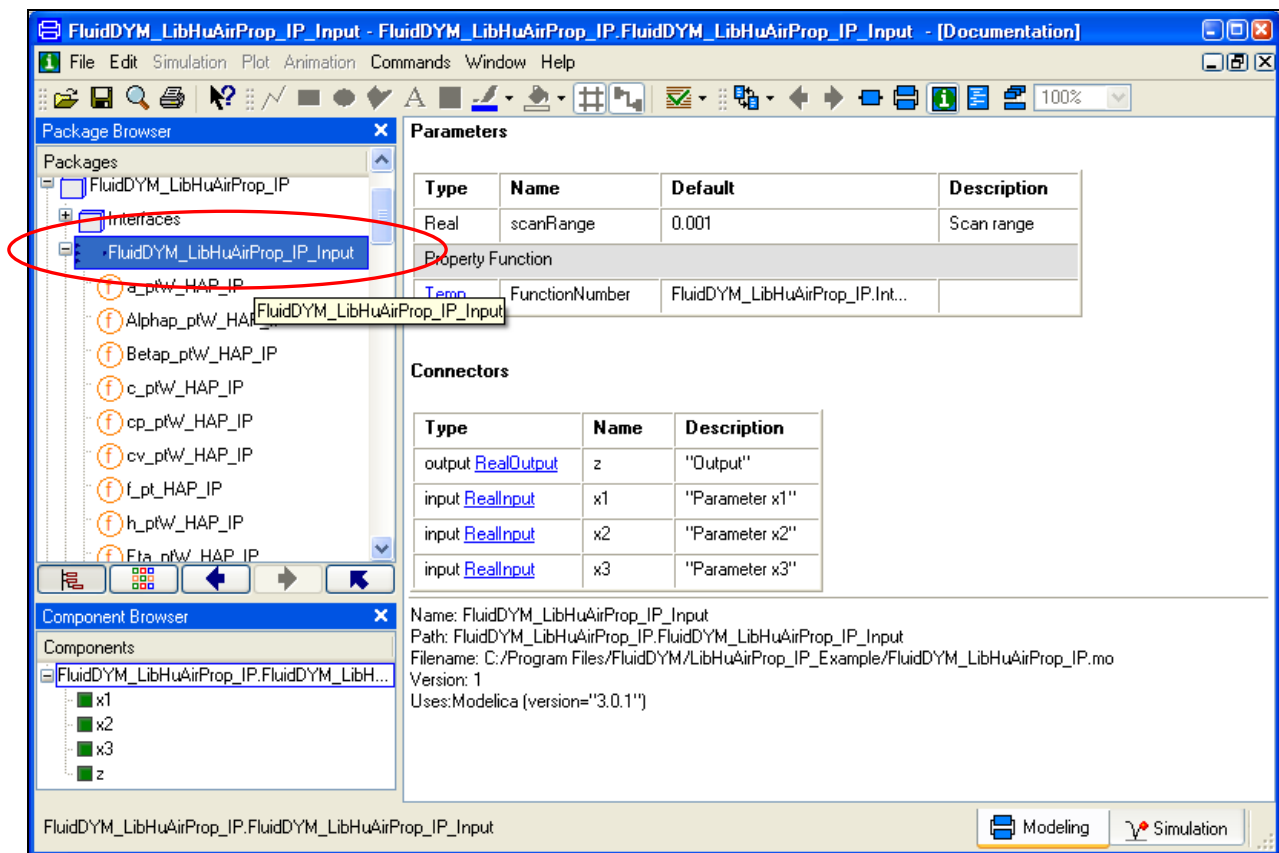


**Figure 2.1.3:** Selecting the "Users\_Guide"

- The program documentation will be displayed within your default web browser.

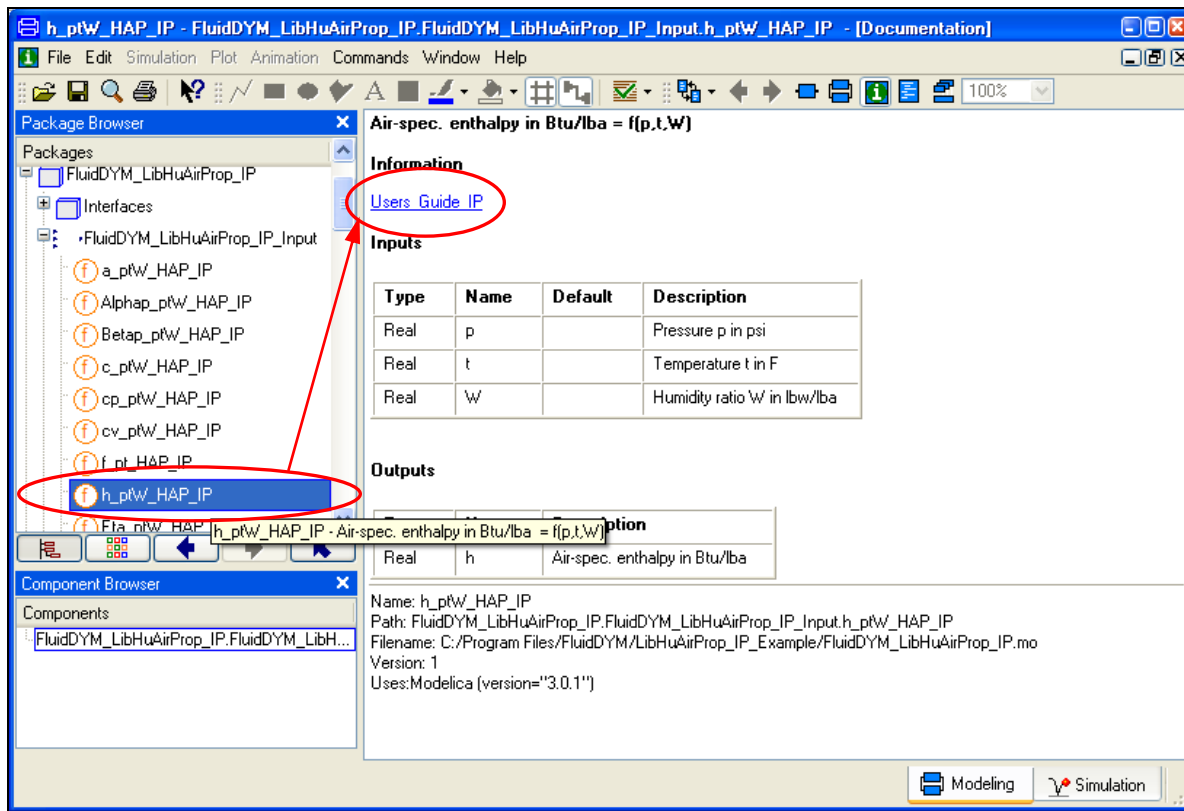
Now, we will show you how to access the help page of a specific property function.

- Make sure Dymola is set to the "Modeling-Mode".
- Now click the  button in the Dymola menu bar to choose the "Documentation Mode".
- Double-click on the "FluidDYM\_LibHuAirProp\_IP\_Input" block on the left (see Figure 2.1.4).



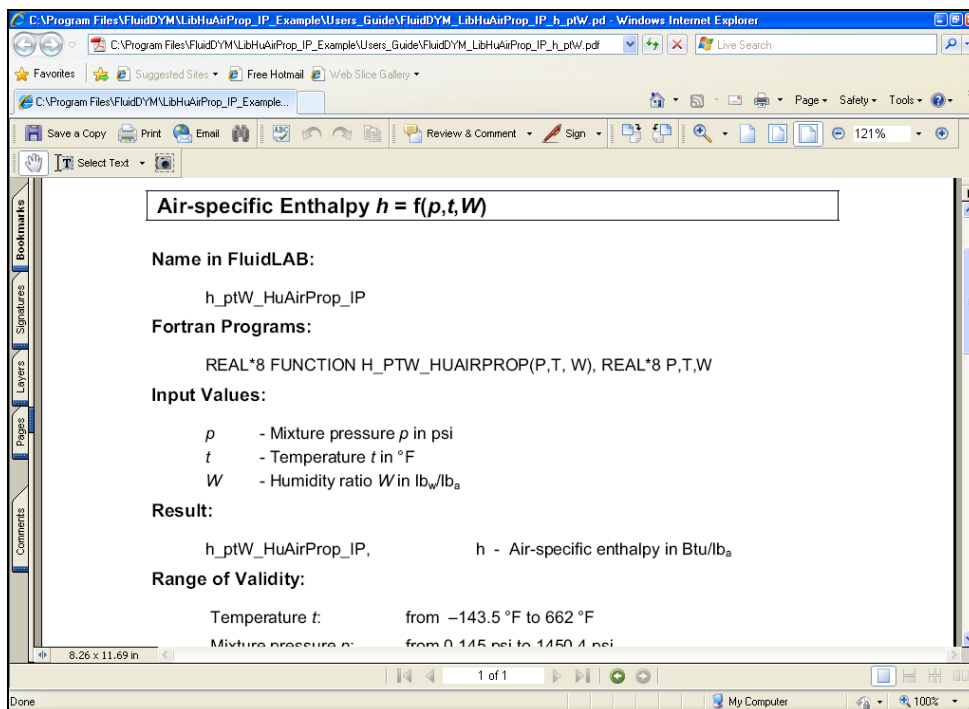
**Figure 2.1.4:** Selected "FluidDYM\_LibHuAirProp\_IP\_Input" Block

- Below "FluidDYM\_LibHuAirProp\_IP\_Input" you will see all functions of the LibHuAirProp\_IP property function.
- Now select a function, e.g. "h\_ptW\_HAP\_IP", and then click on "Users\_Guide" (see Figure 2.1.5).



**Figure 2.1.5:** Marking the "h\_ptW\_HAP\_IP" function and selecting the "Users\_Guide"

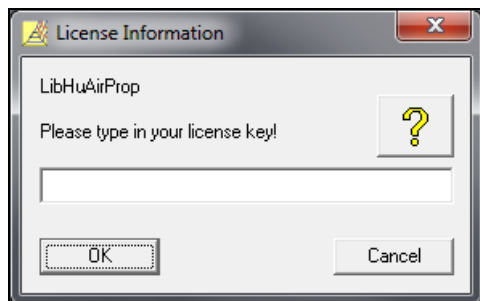
- You will now see the help page of the selected function, here "h\_ptW\_HAP\_IP", in your default web browser (see Figure 2.1.6).



**Figure 2.1.6:** Help page of the function "h\_ptW\_HAP\_IP" in the web browser

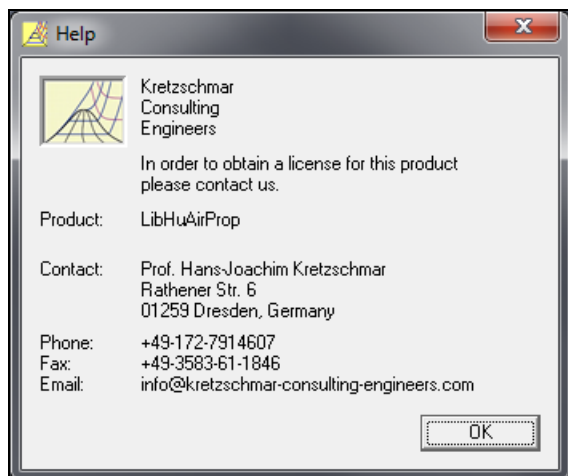
## 2.2 Licensing the LibHuAirProp Property Library

The licensing procedure must be carried out when the FluidDYM prompt message appears. In this case, you will see the "License Information" window for LibHuAirProp (see figure below).



**Figure 2.2.1:** "License Information" window

Here you are asked to type in the license key which you have obtained from Kretzschmar Consulting Engineers. If you do not have this, or have any questions, you will find contact information on the "Content" page of this User's Guide or by clicking the yellow question mark in the "License Information" window. Then the following window will appear:



**Figure 2.2.2:** "Help" window

If you do not enter a valid license it is still possible to use DYMOLA<sup>®</sup> by clicking "Cancel". In this case, the LibHuAirProp property library will display the result "-11111111" for every calculation.

The "License Information" window will appear every time you use FluidDYM LibHuAirProp until you enter a license code to complete registration. If you decide not to use FluidDYM LibHuAirProp, you can uninstall the program following the instructions given in section 2.1.5 of this User's Guide.

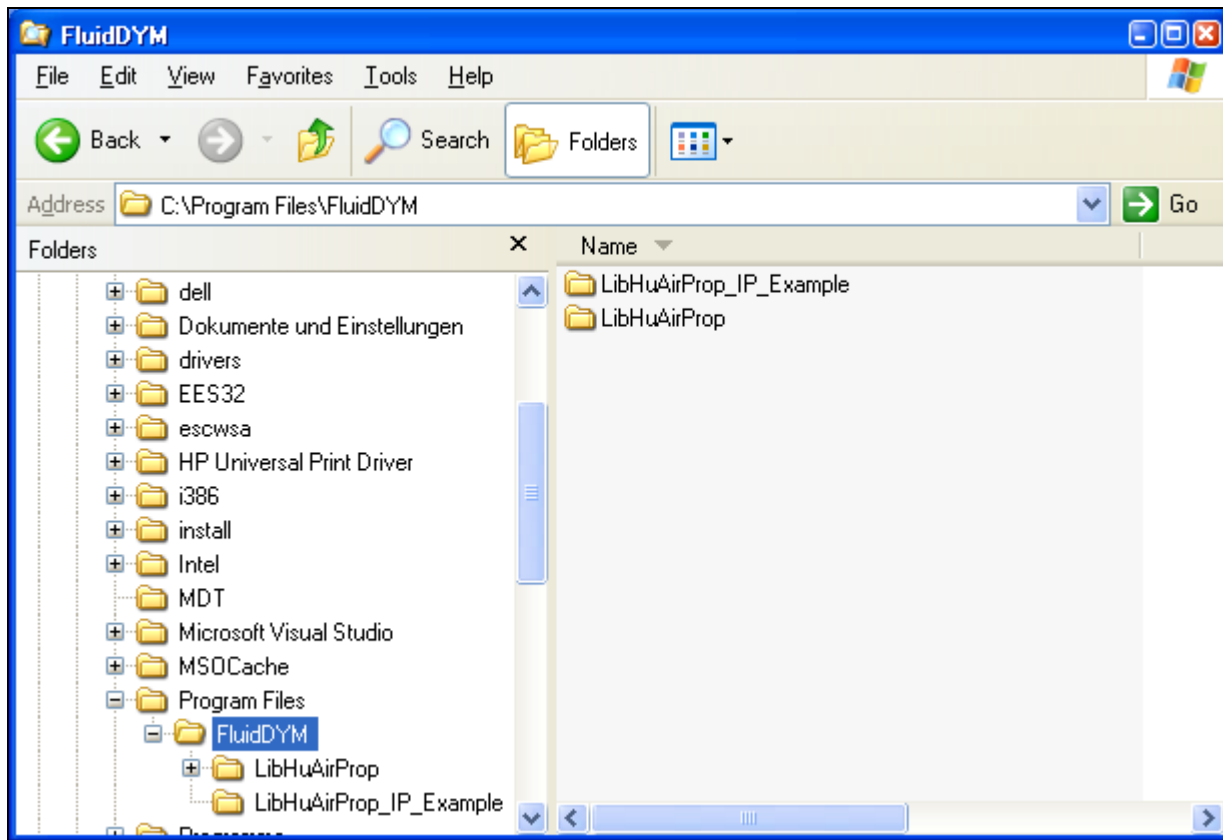
With this procedure both the LibHuAirProp-IP and LibHuAirProp-SI property libraries have been licensed.

## 2.3 Example: Calculation of $h = f(p, t, W)$

Now we will calculate, step by step, the specific enthalpy  $h$  of moist air as a function of pressure  $p$ , temperature  $t$  and humidity ratio  $W$ , using Dymola®.

Please carry out the following instructions:

- Start Windows Explorer®, Total Commander®, My Computer or another file manager program. The description here refers to Windows Explorer
- Your Windows Explorer should be set to Details for a better view. Click the "View" button and select "Details".
- Switch into the program directory of FluidDYM in which you will find the folder "\LibHuAirProp;" the standard location is:  
"C:\Program Files\FluidDYM\LibHuAirProp"
- Create the folder "\LibHuAirProp\_IP\_Example" by clicking on "File" in the Explorer menu, then "New" in the menu which appears, and then selecting "Folder". Name the new folder "\LibHuAirProp\_IP\_Example".
- You will see the following window:

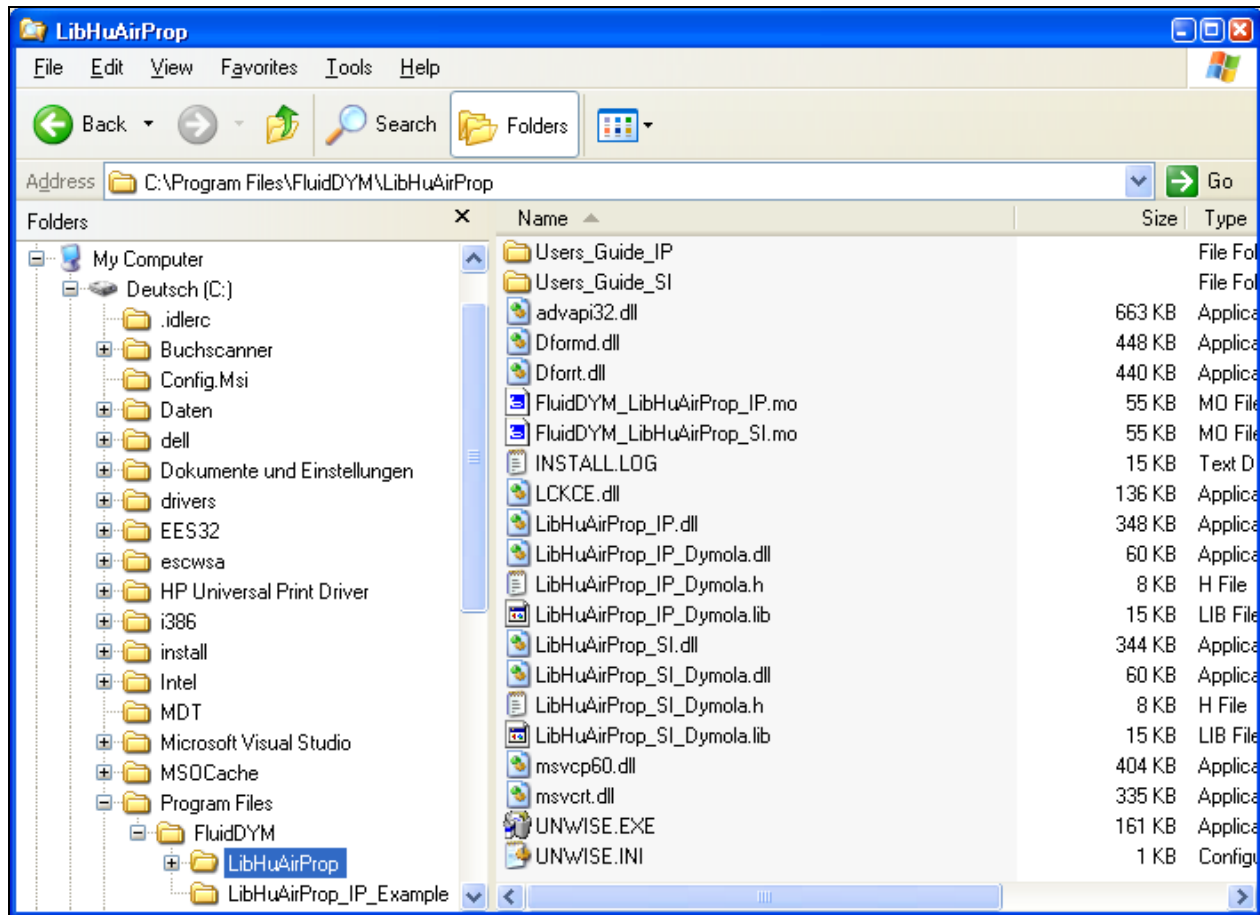


**Figure 2.3.1:** Highlighted *LibHuAirProp\_IP\_Example* directory in Program Files

- Switch into the directory "\LibHuAirProp" within "\FluidDYM", the standard being:  
"C:\Program Files\FluidDYM\LibHuAirProp".



- You will see the following window:



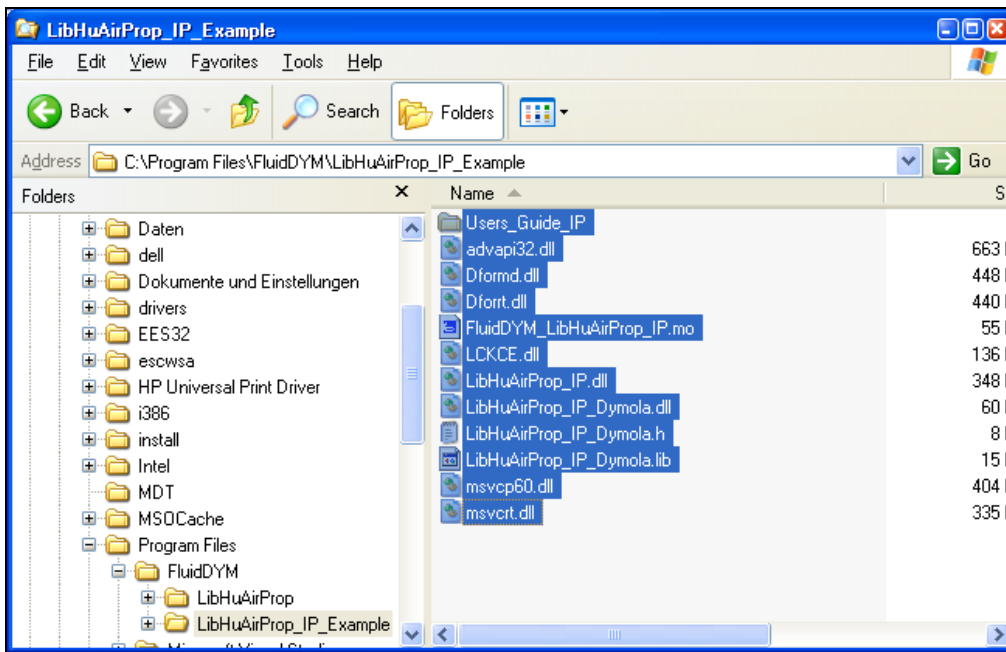
**Figure 2.3.2:** *LibHuAirProp\_IP* directory including installed files

In order to calculate the function  $h = f(p, t, W)$ , the following files are necessary. Copy these into the directory "C:\Program Files\FluidDYM\LibHuAirProp\_IP\_Example":

- "advapi32.dll"
  - "Dfortt.dll"
  - "Dformd.dll"
  - "FluidDYM\_HuAirProp\_IP.mo"
  - "LCKCE.dll"
  - "LibHuAirProp\_IP.dll"
  - "LibHuAirProp\_IP\_Dymola.dll"
  - "LibHuAirProp\_IP\_Dymola.h"
  - "LibHuAirProp\_IP\_Dymola.lib"
  - "msvcp60.dll"
  - "msvcr7.dll"
  - the folder "Users\_Guide"
- Mark up these files, then click "Edit" in the upper menu bar and select "Copy".
  - Switch into the directory "C:\Program Files\FluidDYM\LibHuAirProp\_IP\_Example", click "Edit"

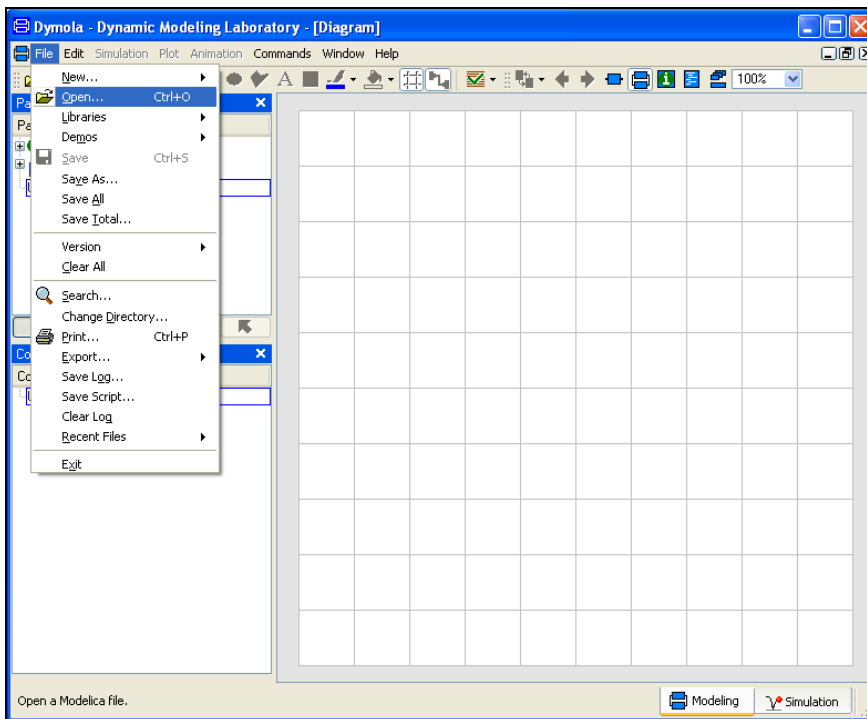
and then "Paste".

- You will see the following window:



**Figure 2.3.3:** *LibHuAirProp\_IP\_Example* directory including the newly-copied files

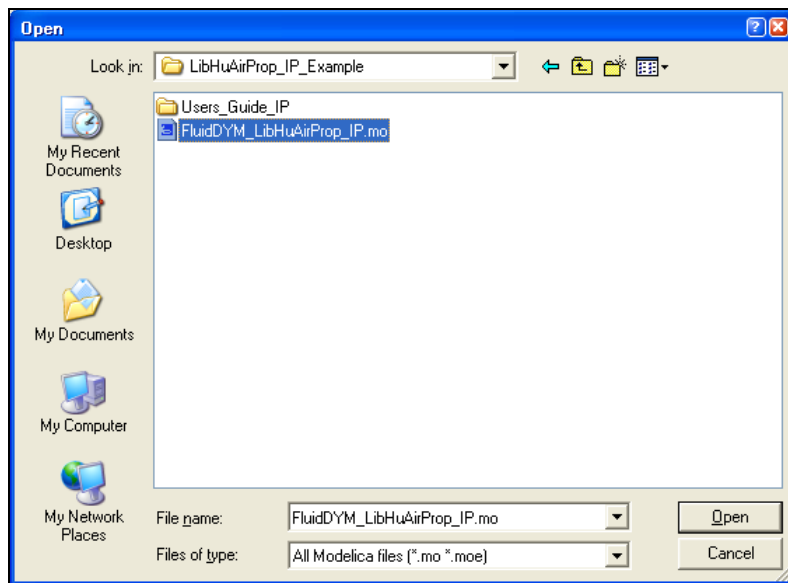
- Start Dymola®.
- Now click on "File" in the Dymola menu bar and select "Open" (see Figure 2.3.4).



**Figure 2.3.4:** Selecting the menu entry "Open"

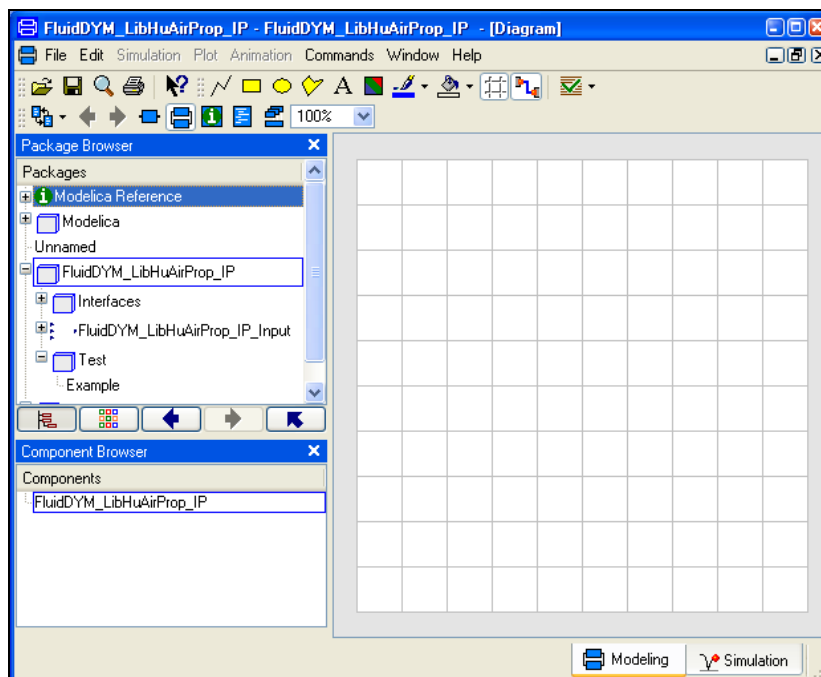
- Search and click on the directory "C:\Program Files\FluidDYM\LibHuAirProp\_IP\_Example" in the menu that appears.

- Select the "FluidDYM\_LibHuAirProp\_IP.mo" file and click on the "Open" button (see Figure 2.3.5)



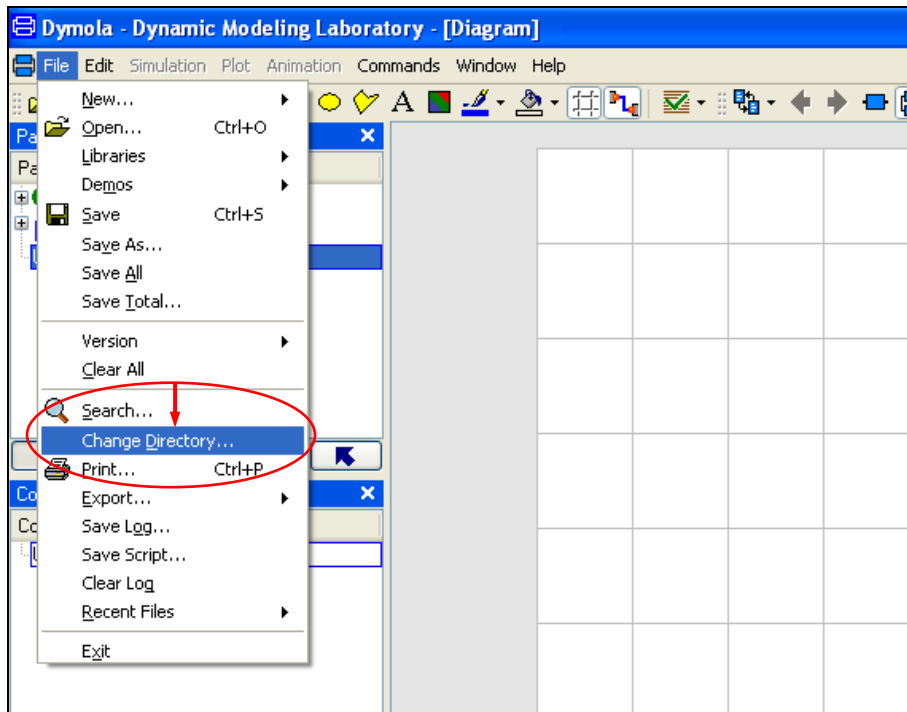
**Figure 2.3.5:** Selecting the *FluidDYM\_HuAirProp\_IP.mo* file

- The library will be loaded by Dymola which may take a few seconds.
- After Dymola has finished loading the LibHuAirProp\_IP library, you will see the window shown in Figure 2.3.6.



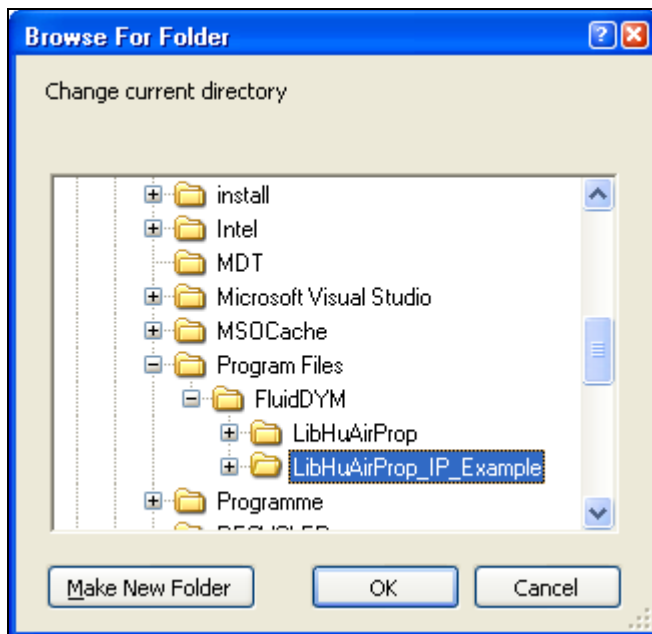
**Figure 2.3.6:** Dymola window after loading the *LibHuAirProp\_IP* library

- Now, click on "File" in the Dymola menu bar and select "Change Directory..." in order to open the folder "\LibHuAirProp\_IP\_Example" (see Figure 2.3.7).



**Figure 2.3.7:** Selecting the menu entry "Change Directory..."

- Search and click on the directory "C:\Program Files\FluidDYM\LibHuAirProp\_IP\_Example" in the menu that appears (see figure below).

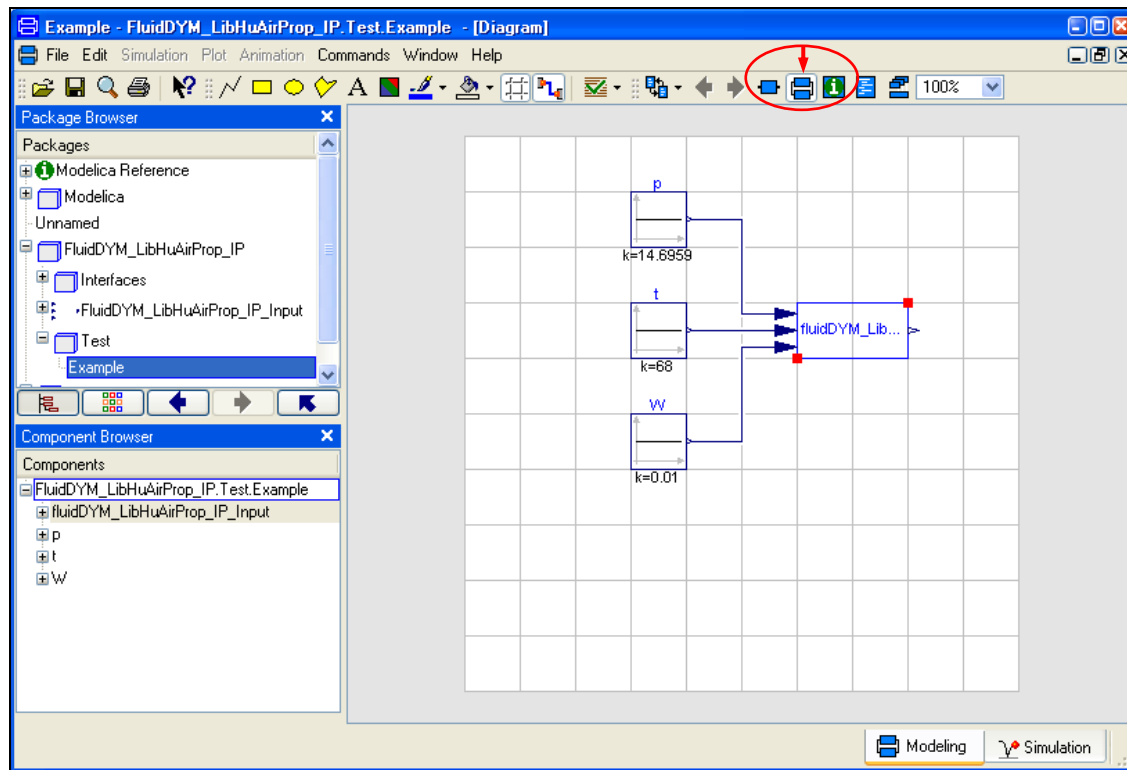


**Figure 2.3.8:** Selecting the *LibHuAirProp\_IP\_Example* directory

- Confirm your selection by clicking the "OK" button.

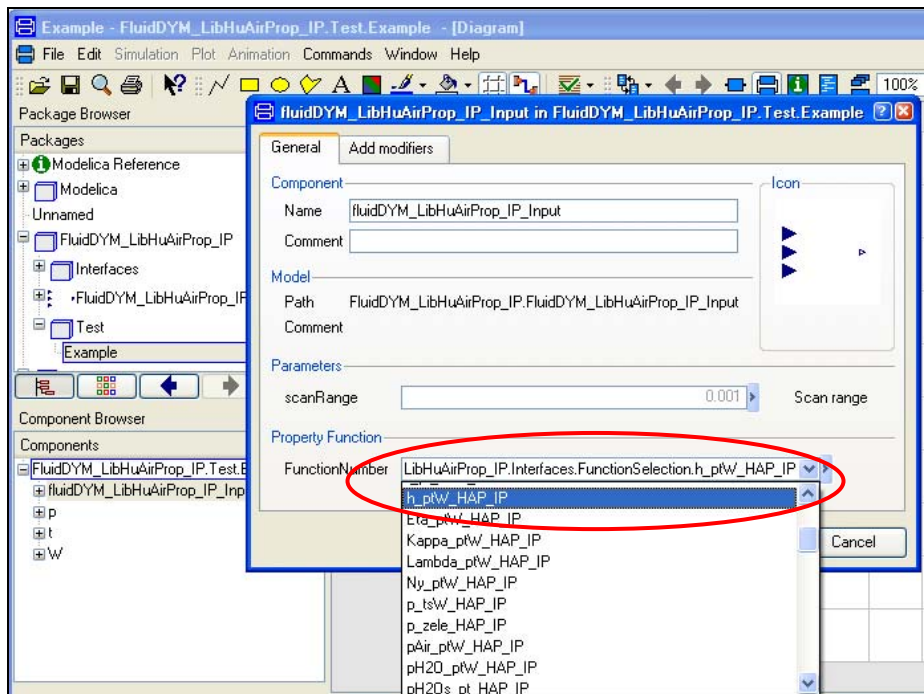
As indicated in the table of property functions in Chapter 1, you have to call up the function "h\_ptW\_HAP\_IP" as follows for calculating  $h = f(p, t, W)$ .

- Click on the Dymola-Block "Test," which can be found in the FluidDYM\_HuAirProp\_IP package in the "Package Browser" on the left hand side of the Dymola window. Here choose Example by double-clicking on it.
- Now click on the  button in the Dymola menu bar in order to switch to the Diagram Mode. You will see the following window:



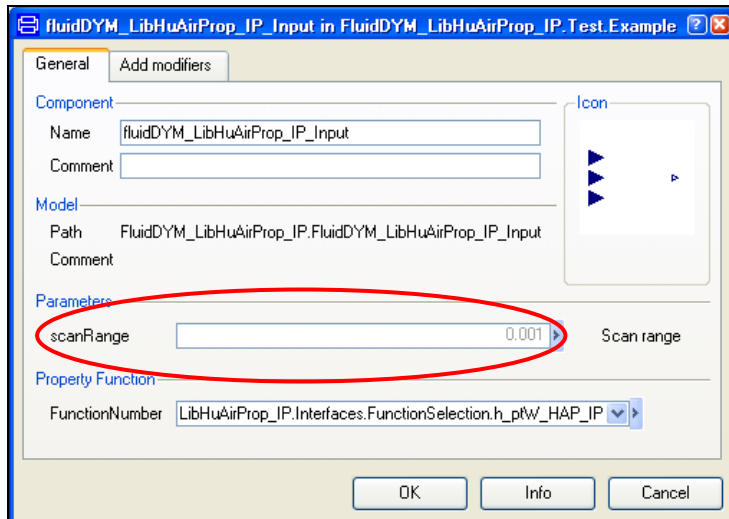
**Figure 2.3.9:** Dymola in Diagram Mode

- Now double-click on the "fluidDYM\_LibHuAirProp\_IP\_Input" block on the right hand side of the Dymola window.
- Search and click the "h\_ptW\_HAP\_IP" function next to "Function Number" in the menu that appears (see figure below).



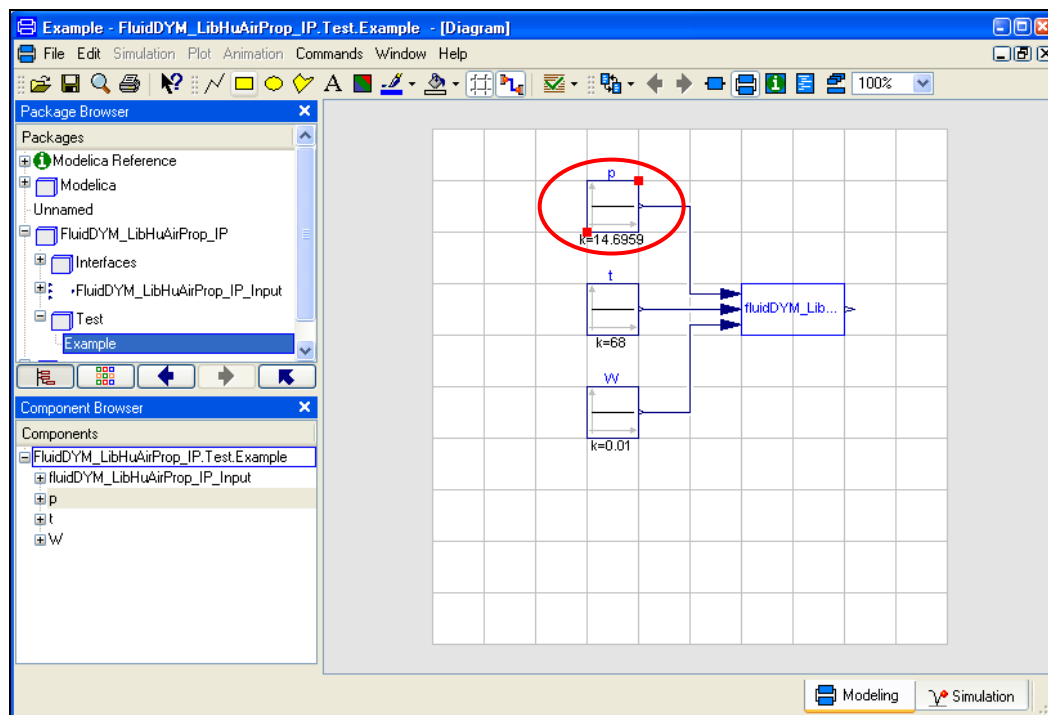
**Figure 2.3.10:** Choosing the function  $h_{ptW\_HAP\_IP}$

- You can set the scan range (how many times the property will be calculated per second) next to "scanRange". The preset value 0.001 means that the property will be calculated 1000 times per second. If you enter the value 1, for example, the property will be calculated once per second. Do not change the preset value of 0.001 for our example calculation.



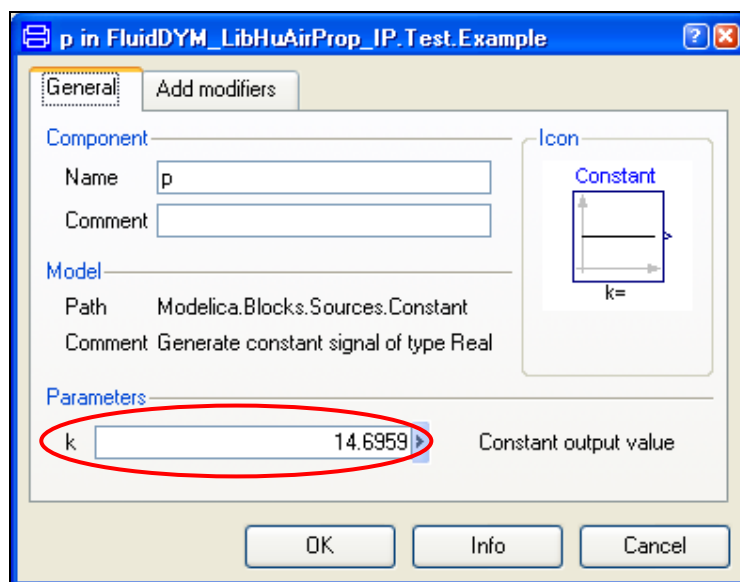
**Figure 2.3.11:** Setting the scan range

- Now we will configure the input parameters  $p$ ,  $t$ , and  $W$ . When calculating a function with only two input parameters, the third input parameter will not be defined.
- First, double click on the "p" block which represents the first input parameter, here the pressure  $p$  in psi (see Figure 2.3.12).



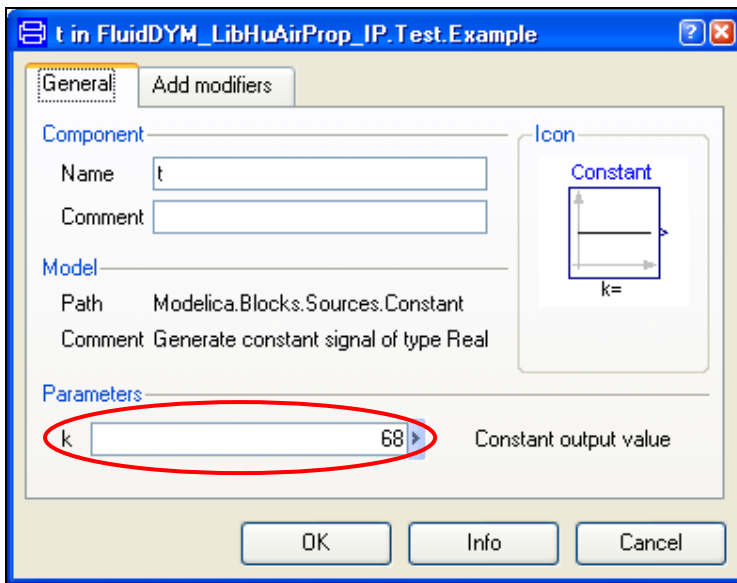
**Figure 2.3.12:** "Parameter  $p$  in psi" block in Dymola

- Enter the value 14.6959 on the line next to "k" in the dialog window which appears and then click the "OK" button (see Figure 2.3.13).



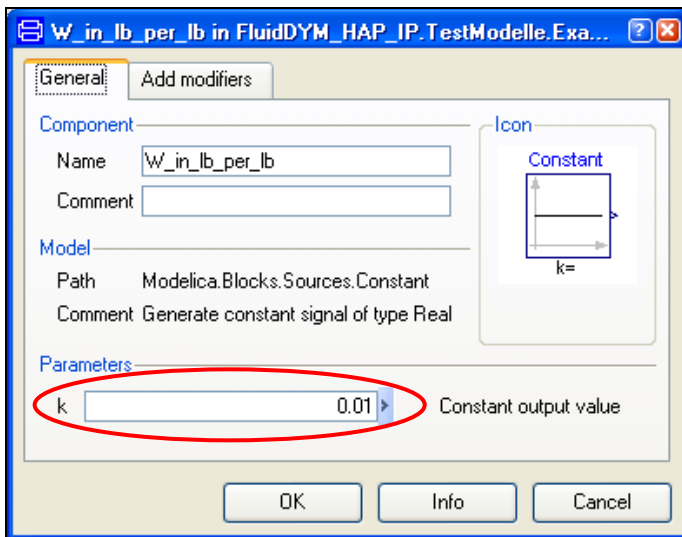
**Figure 2.3.13:** Entering the value for the pressure  $p$

- Now, double click on the "t" block which represents the second input parameter, here the temperature  $t$  in °F.
- Enter the value 68 on the line next to "k" in the dialog window which appears and then click the "OK" button (see Figure 2.3.14).



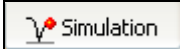
**Figure 2.3.14:** Entering the value for the temperature  $t$

- Now, double click on the "W" block which represents the third input parameter, here the humidity ratio  $W$  in  $\text{lb}_w/\text{lb}_a$ .
- Enter the value 0.01 on the line next to "k" in the dialog window which appears and then click the "OK" button (see Figure 2.3.15).



**Figure 2.3.15:** Entering the value for the humidity ratio  $W$

All parameters have now been defined.

- Click on the  button in the lower right area of Dymola in order to switch into the "Simulation Mode".

In Figure 2.3.16 you can see what the Dymola "Simulation Mode" looks like.



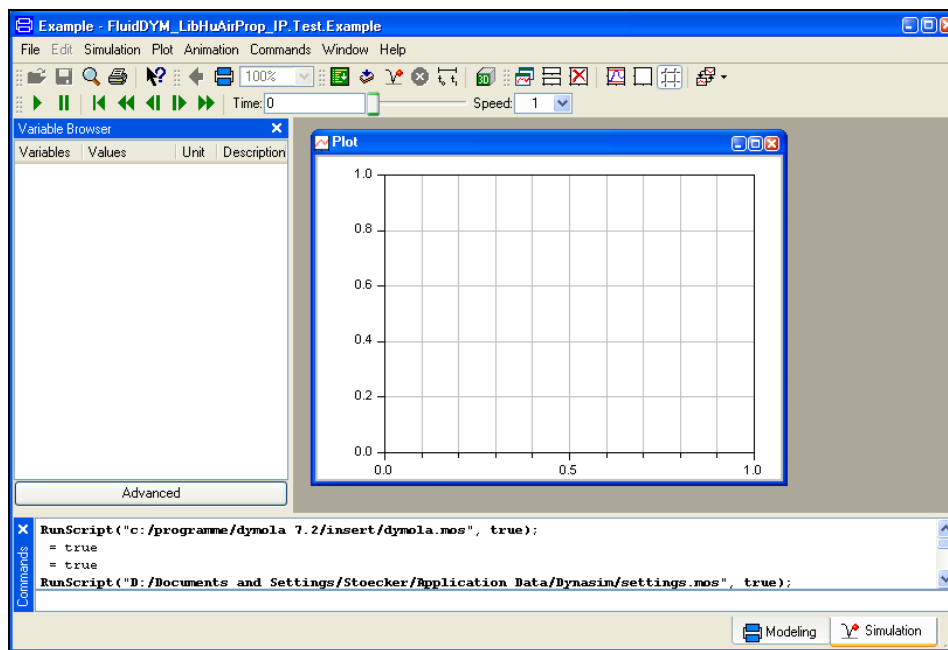


Figure 2.3.16: "Simulation Mode" window

### **IMPORTANT NOTICE:**

Per default the 64-bit version of Dymola creates a 32-bit simulation process. If you want to create a 64-bit simulation process you must have installed the 64-bit version of FluidDYM LibHuAirProp and you now need to enter the following command into the command line of Dymola and confirm your entry by pressing the Enter key:

**"Advanced.CompileWith64=2"**

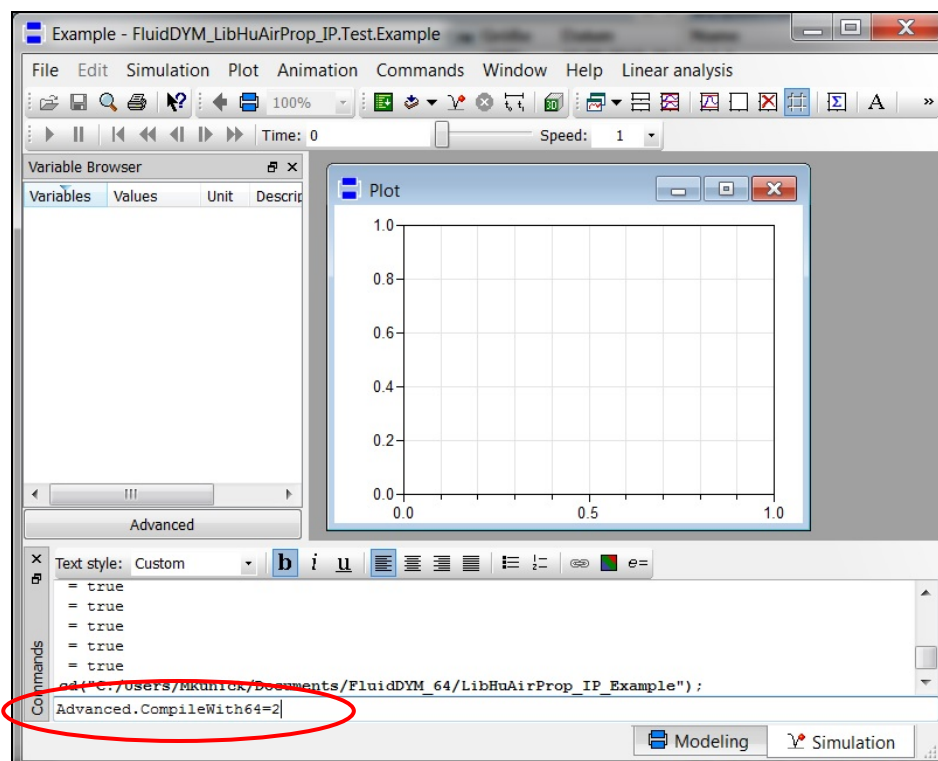


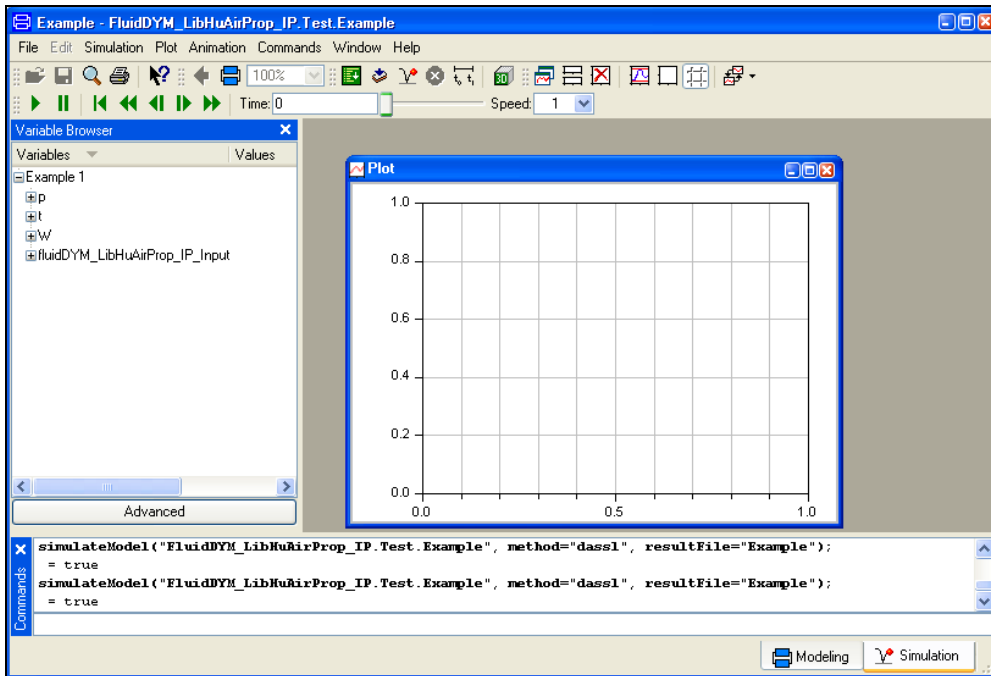
Figure 2.3.17: "Simulation Mode" window with 64-bit command

Now, your 64-bit Dymola creates 64-bit simulation processes with FluidDYM LibHuAirProp.

Please note that if you restart Dymola and want to create 64-bit simulation processes again, you will always have to enter this command anew.

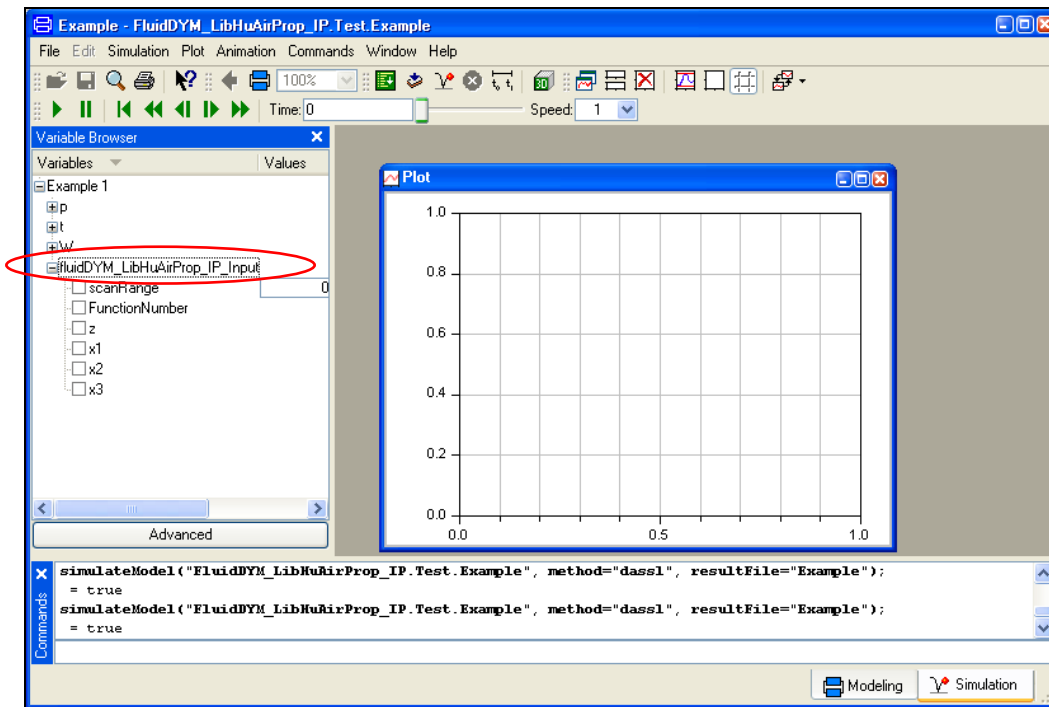
For further information concerning this matter, please see the Dymola user's guide.

- Click on the "Simulate" Button  in the Dymola menu bar to start the calculation. Now the model will be compiled and the simulation started.
- Afterwards you will see the following entries within the "Variable Browser" window in Dymola (see Figure 2.3.18):



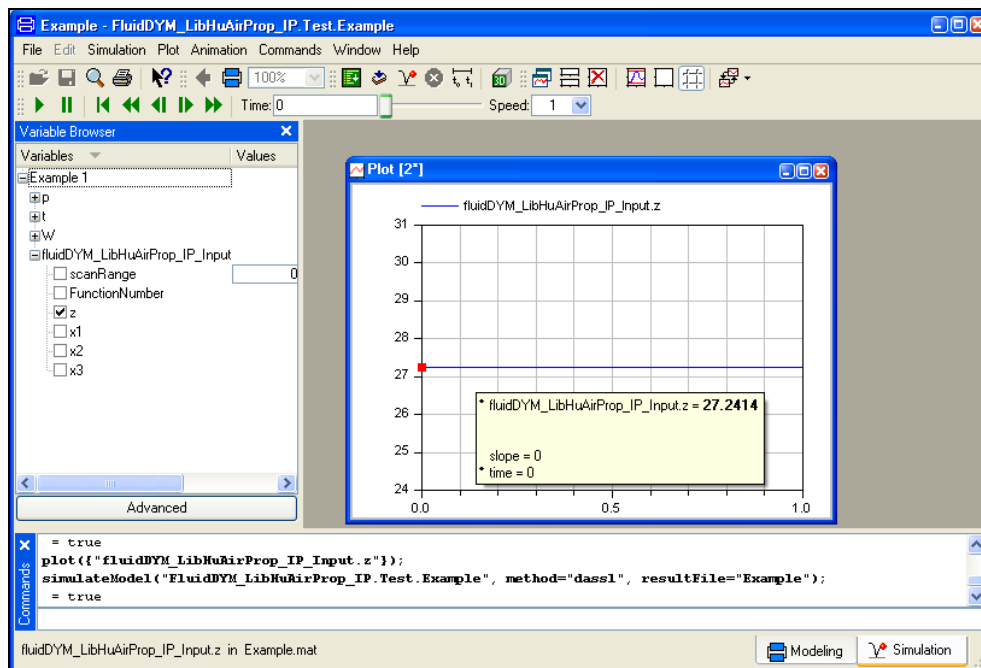
**Figure 2.3.18:** "Variable Browser" with new entries

- By clicking on the "NewPlotWindow" button , a new diagram window will be opened.
- Click on "fluidDYM\_LibHuAirProp\_IP\_Input" within the "Variable Browser"; then you will see the input and output parameters "scanRange", "FunctionNumber", "z", "x1", "x2", and "x3" (see Figure 2.3.19).



**Figure 2.3.19:** Parameters of *fluidDYM\_LibHuAirProp\_IP\_Input*

- After clicking on the output parameter "z", the calculated property will be represented graphically in the "PlotWindow".
- Move the mouse over the curve to see the result of the Simulation at a specific point in time (see Figure 2.3.20).



**Figure 2.3.20:** "DiagramWindow" showing the result

The result for *h* appears in the "DiagramWindow"

⇒ The result in our sample calculation here is: " $h = 27.2414$ ". The corresponding unit is Btu/lb<sub>a</sub> (see table of the property functions in Chapter 1).

- Now click on the Modeling button  in the lower right area of Dymola in order to switch into the "Modeling Mode". Here you can arbitrarily change the values for  $p$ ,  $t$ , or  $W$  in the appropriate blocks.

## 2.4 Removing FluidDYM including LibHuAirProp

In order to remove the property library LibHuAirProp from your hard drive in Windows<sup>®</sup>, click "Start" in the lower task bar, then "Settings" and "Control Panel".

Afterwards double-click on "Add or Remove Programs".

In the list box of the "Add or Remove Programs" menu which appears, select "FluidDYM LibHuAirProp" by clicking on it and then clicking the "Change/Remove" button.

In the following dialogue box click "Automatic" and then "Next>".

Confirm the "Perform Uninstall" menu which appears by clicking the "Finish" button.

Finally, close the "Add or Remove Programs" and "Control Panel" windows. "FluidDYM LibHuAirProp" has now been removed.

If LibHuAirProp is the only library installed, the directory "FluidDYM" will be removed as well.

## **3 Property Functions of ASHRAE-LibHuAirProp-IP**

### **3.1 Functions for Real Moist Air**

**Thermal Diffusivity  $a = f(p, t, W)$** **Function Name:**

a\_ptW\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION A\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**a\_ptW\_HAP\_IP - Thermal diffusivity of humid air in ft<sup>2</sup>/s**Range of Validity:**

Temperature  $t$ : from -99.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq W_s$

**Comments:**

- Thermal diffusivity  $a = \frac{\lambda}{\rho \cdot c_p}$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

a\_ptW\_HAP\_IP = -1000

**References:**

$\lambda(p, t, W)$  Herrmann et al. [3], [4]  
 $\rho(p, t, W)$  Herrmann et al. [1], [2]  
 $c_p(p, t, W)$  Herrmann et al. [1], [2]

**Relative Pressure Coefficient  $\alpha_p = f(p, t, W)$** 
**Function Name:**

alphap\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  ALPHAP_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

alphap\_ptW\_HAP\_IP - Relative pressure coefficient of humid air in 1/°R

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq W_s$

**Comments:**

- Relative pressure coefficient  $\alpha_p = \frac{1}{p} \left( \frac{\partial p}{\partial T} \right)_v$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

alphap\_ptW\_HAP\_IP = -1000

**References:**

$\alpha_p(p, t, W)$  Herrmann et al. [1], [2]

**Isothermal Stress Coefficient  $\beta_p = f(p, t, W)$** 
**Function Name:**

betap\_ptW\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION BETAP\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**betap\_ptW\_HAP\_IP - Isothermal stress coefficient of humid air in lb/ft<sup>3</sup>**Range of Validity:**

Temperature  $t$ : from -225.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq W_s$

**Comments:**

- Isothermal stress coefficient  $\beta_p = -\frac{1}{p} \left( \frac{\partial p}{\partial v} \right)_T$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

betap\_ptW\_HAP\_IP = -1000

**References:** $\beta_p(p, t, W)$  Herrmann et al. [1], [2]



**Speed of Sound  $c = f(p, t, W)$** 
**Function Name:**

c\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION C_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

c\_ptW\_HAP\_IP - Speed of sound of humid air in ft/s

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Speed of sound  $c = v \sqrt{-\left(\frac{\partial p}{\partial v}\right)_s}$

- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

c\_ptW\_HAP\_IP = -1000

**References:**

$c(p, t, W)$  Herrmann et al. [1], [2]

**Isobaric Heat Capacity  $c_p = f(p, t, W)$** 
**Function Name:**

cp\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION CP_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in psi  
 $t$        -    Temperature  $t$  in °F  
 $W$       -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

cp\_ptW\_HAP\_IP - Isobaric heat capacity of humid air in Btu/(lb °R)

**Range of Validity:**

Temperature  $t$ :                from -225.67°F to 662°F  
 Total pressure  $p$ :            from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :             $0 \leq W \leq W_s$

**Comments:**

- Isobaric heat capacity  $c_p = \left( \frac{\partial h}{\partial T} \right)_p$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

cp\_ptW\_HAP\_IP = -1000

**References:**

$c_p(p, t, W)$     Herrmann et al. [1], [2]

**Isochoric Heat Capacity  $c_v = f(p, t, W)$** 
**Function Name:**

cv\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION CV_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in psi  
 $t$        -    Temperature  $t$  in °F  
 $W$       -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

cv\_ptW\_HAP\_IP - Isochoric heat capacity of humid air in Btu/(lb °R)

**Range of Validity:**

Temperature  $t$ :                      from -225.67°F to 662°F  
 Total pressure  $p$ :                    from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :                    $0 \leq W \leq W_s$

**Comments:**

- Isochoric heat capacity  $c_v = \left( \frac{\partial u}{\partial T} \right)_v$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

cv\_ptW\_HAP\_IP = -1000

**References:**

$c_v(p, t, W)$     Herrmann et al. [3], [4]

**Enhancement Factor  $f = f(p,t)$** 
**Function Name:**

f\_pt\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  F_PT_HUAIRPROP(P,T), REAL*8 P,T
```

**Input Values:**

$p$      -   Total pressure  $p$  in psi  
 $t$      -   Temperature  $t$  in °F

**Result:**

f\_pt\_HAP\_IP - Enhancement factor of water (decimal ratio)

**Range of Validity:**

Temperature  $t$ :               from -225.67°F to 662°F  
Total pressure  $p$ :            from 0.00145 psi to 1450.4 psi

**Comments:**

- Enhancement factor  $f = \frac{\rho_{\text{H}_2\text{O},s}}{\rho_s(t)}$   
with  $\rho_s(t)$    for  $t \geq 32^\circ\text{F}$  - Steam pressure of water  
                  for  $t < 32^\circ\text{F}$  - Sublimation pressure of water
- Describes the enhancement of the saturation pressure of water in the air atmosphere under elevated pressure
- Derived iteratively from the isothermal compressibility of liquid water, from Henry's constant [15], [16] and from the virial coefficients of air, water, and the air-water mixture

**Result for Wrong Input Values:**

f\_pt\_HAP\_IP = -1000

**References:**

$f(p,t)$        Herrmann et al. [1], [2]

**Air-Specific Enthalpy  $h = f(p, t, W)$** 
**Function Name:**

h\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION H_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

h\_ptW\_HAP\_IP - Air-specific enthalpy in Btu/lb<sub>a</sub>

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

h\_ptW\_HAP\_IP = -1000

**References:**

$h(p, t, W)$  Herrmann et al. [1], [2]  
 $h_w(p, t)$  IAPWS-IF97 [7], [8] and IAPWS-06 [11]  
 $h_a(t)$  Lemmon et al. [14]

**Dynamic Viscosity  $\eta = f(p, t, W)$** 
**Function Name:**

Eta\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  ETA_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in psi  
 $t$      -    Temperature  $t$  in °F  
 $W$     -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

Eta\_ptW\_HAP\_IP - Dynamic viscosity of humid air in (lb s/ft<sup>2</sup>)

**Range of Validity:**

Temperature  $t$ :                from -99.67°F to 662°F  
 Total pressure  $p$ :            from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :             $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- A new very accurate algorithm is implemented between 32°F and 662°F
- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

Eta\_ptW\_HAP\_IP = -1000

**References:**

$\eta(p, t, W)$      Herrmann et al. [3], [4]  
 $\eta_w(p, t)$      IAPWS-IF97 [7], [8] and IAPWS-06 [19]  
 $\eta_a(t)$         Lemmon et al. [18]

**Isentropic Exponent  $\kappa = f(p, t, W)$** 
**Function Name:**

Kappa\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION KAPPA_PTW_HUAIRPROP(P,T, W), REAL*8 P,T,W
```

**Input Values:**

$p$     -    Total pressure  $p$  in psi  
 $t$     -    Temperature  $t$  in °F  
 $W$     -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

Kappa\_ptW\_HAP\_IP - Isentropic exponent

**Range of Validity:**

Temperature  $t$ :                      from -225.67°F to 662°F  
 Total pressure  $p$ :                    from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :                     $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Isentropic exponent  $\kappa = -\frac{v}{p} \left( \frac{\partial p}{\partial v} \right)_s$
- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets homogeneously mixed) is applied for  $t \geq 32^\circ\text{F}$ . For temperatures below (ice fog) the value of the saturated state is applied.

**Result for Wrong Input Values:**

Kappa\_ptW\_HAP\_IP = -1000

**References:** $v(p, t, W)$  Herrmann et al. [1], [2]

**Thermal Conductivity  $\lambda = f(p, t, W)$** 
**Function Name:**

Lambda\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  LAMBDA_PTW_HUAIRPROP(P,T, W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

Lambda\_ptW\_HAP\_IP - Thermal conductivity in Btu/(h ft °R)

**Range of Validity:**

Temperature  $t$ : from -99.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- A new very accurate algorithm is implemented between 32°F and 662°F
- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

Lambda\_ptW\_HAP\_IP = -1000

**References:**

$\lambda(p, t, W)$  Herrmann et al. [3], [4]  
 $\lambda_w(p, t)$  IAPWS-IF97 [7], [8] and IAPWS-08 [20]  
 $\lambda_a(t)$  Lemmon et al. [18]



**Kinematic Viscosity  $\nu = f(p, t, W)$** 
**Function Name:**

Ny\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  NY_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in psi  
 $t$      -    Temperature  $t$  in °F  
 $W$      -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

Ny\_ptW\_HAP\_IP - Kinematic viscosity in ft<sup>2</sup>/s

**Range of Validity:**

Temperature  $t$ :                      from -99.67°F to 662°F  
 Total pressure  $p$ :                    from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :                     $0 \leq W \leq W_s$

**Comments:**

- Kinematic Viscosity  $\nu = \frac{\eta}{\rho}$

**Result for Wrong Input Values:**

Ny\_ptW\_HAP\_IP = -1000

**References:**

$\eta(p, t, W)$     Herrmann et al. [3], [4]  
 $\rho(p, t, W)$     Herrmann et al. [1], [2]

**Backward Function: Pressure  $p = f(t,s,W)$** **Function Name:**

p\_tsW\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION P\_TSW\_HUAIRPROP(T,S,W), REAL\*8 T,S,W

**Input Values:**

$t$  - Temperature  $t$  in °F  
 $s$  - Air-specific entropy  $s$  in Btu/(lb<sub>a</sub> °R)  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

p\_tsW\_HAP\_IP - Total pressure of humid air in psi

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 662°F  
 Air-specific entropy  $s$ : from -6.32 Btu/(lb<sub>a</sub> °R) to 9.32877 Btu/(lb<sub>a</sub> °R)  
 Humidity ratio  $W$ :  $0 \leq W \leq 10$  lb<sub>w</sub>/lb<sub>a</sub>

**Comments:**- Iteration of total pressure  $p$  from  $s = f(p,t,W)$ **Result for Wrong Input Values:**

p\_tsW\_HAP\_IP = -1000

**References:** $s(p,t,W)$  Herrmann et al. [1], [2]

**Pressure  $p = f(z_{\text{ele}})$** **Function Name:**

p\_zele\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION P\_ZELE\_HUAIRPROP(ZELE), REAL\*8 ZELE

**Input Values:**z<sub>ele</sub> - Elevation z<sub>ele</sub> in ft**Result:**

p\_zele\_HAP\_IP - Pressure of humid air in psi

**Range of Validity:**Elevation z<sub>ele</sub> from -16,404 ft to 36,089 ft**Comments:**

- Pressure of humid air from elevation

$$- p(z_{\text{ele}}) = 14.696 \text{ psi} \cdot \left( 1 - 6.8754 \cdot 10^{-6} \cdot \frac{z_{\text{ele}}}{\text{ft}} \right)^{5.256}$$

**Result for Wrong Input Values:**

p\_zele\_HAP\_IP = -1000

**References:**p(z<sub>ele</sub>) ASHRAE [23]

**Partial Pressure of Air  $p_{\text{Air}} = f(p, t, W)$** 
**Function Name:**

pAir\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION PAIR_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in psi  
 $t$      -    Temperature  $t$  in °F  
 $W$      -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

pAir\_ptW\_HAP\_IP - Partial pressure of (dry) air in humid air in psi

**Range of Validity:**

Temperature  $t$ :                from -225.67°F to 662°F  
 Total pressure  $p$ :            from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :             $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Partial pressure of (dry) air in humid air  $p_{\text{Air}} = 1 - p_{\text{H}_2\text{O}}$
- Partial pressure of water vapor at saturation is calculated in case of supersaturated humid air ( $W > W_s(p, t)$ )
- The temperature value is used to calculate the saturation state

**Result for Wrong Input Values:**

pAir\_ptW\_HAP\_IP = -1000

**References:**
 $p_{\text{H}_2\text{O}}(p, W)$     Herrmann et al. [1], [2]

**Partial Pressure of Water Vapor  $p_{\text{H}_2\text{O}} = f(p, t, W)$** 
**Function Name:**

pH2O\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION PH2O_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -     Total pressure  $p$  in psi  
 $t$      -     Temperature  $t$  in °F  
 $W$      -     Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

pH2O\_ptW\_HAP\_IP - Partial pressure of water vapor in humid air in psi

**Range of Validity:**

Temperature  $t$ :                      from -225.67°F to 662°F  
 Total pressure  $p$ :                    from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :                     $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Partial pressure of water vapor in humid air  $p_{\text{H}_2\text{O}} = \frac{W \cdot p}{\left(\frac{R_a}{R_w} + W\right)}$
- Partial pressure of water vapor at saturation is calculated in case of supersaturated humid air ( $W > W_s(p, t)$ )
- The temperature value is used to calculate the saturation state

**Result for Wrong Input Values:**

pH2O\_ptW\_HAP\_IP = -1000

**References:**
 $p_{\text{H}_2\text{O}}(p, W)$      Herrmann et al. [1], [2]

**Partial Sat. Pressure of Water Vapor in Humid Air  $p_{\text{H}_2\text{O},s} = f(p, t)$** 
**Function Name:**

pH2Os\_pt\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION PH2OS\_PT\_HUAIRPROP(P,T), REAL\*8 P,T

**Input Values:** $p$  - Total pressure  $p$  in psi $t$  - Temperature  $t$  in °F**Result:**

pH2Os\_pt\_HAP\_IP - Partial saturation pressure of water vapor in humid air in psi

**Range of Validity:**Temperature  $t$ : from -225.67°F to 662°FTotal pressure  $p$ : from 0.00145 psi to 1450.4 psi**Comments:**- Partial pressure of water vapor at saturation  $p_{\text{H}_2\text{O},s} = f \cdot p_s(t)$ with  $p_s(t)$  for  $t \geq 32^\circ\text{F}$  - Steam pressure of waterfor  $t < 32^\circ\text{F}$  - Sublimation pressure of water**Result for Wrong Input Values:**

pH2Os\_pt\_HAP\_IP = -1000

**References:** $f(p, t)$  Herrmann et al. [1], [2] $p_s(t)$  for  $t \geq 32^\circ\text{F}$  IAPWS-IF97 [7], [8]for  $t < 32^\circ\text{F}$  IAPWS-08 [11]

## Relative Humidity $\phi = f(p, t, W)$

### Function Name:

phi\_ptW\_HAP\_IP

### Fortran Program:

```
REAL*8 FUNCTION PHI_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

### Input Values:

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

### Result:

phi\_ptW\_HAP\_IP - Relative humidity (decimal ratio)

### Range of Validity:

Temperature  $t$ : from -225.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq 10$  lb<sub>w</sub>/lb<sub>a</sub>

### Comments:

- Relative humidity  $\phi = \frac{p_{\text{H}_2\text{O}}}{p_{\text{H}_2\text{O},s}}$
- This equation is valid for  $p_{\text{H}_2\text{O}} \leq p_{\text{H}_2\text{O},s}$  and for  $0 \leq \phi \leq 1$

### Result for Wrong Input Values:

phi\_ptW\_HAP\_IP = -1000

### References:

$\phi(p, t, W)$  Herrmann et al. [1], [2]

**Prandtl Number  $Pr = f(p, t, W)$** 
**Function Name:**

Pr\_ptW\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION PR\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

Pr\_ptW\_HAP\_IP - Prandtl number

**Range of Validity:**

Temperature  $t$ : from -99.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Prandtl number  $Pr = \frac{\eta \cdot c_p}{\lambda}$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

Pr\_ptW\_HAP\_IP = -1000

**References:**

$\eta(p, t, W)$  Herrmann et al. [3], [4]  
 $c_p(p, t, W)$  Herrmann et al. [3], [4]  
 $\lambda(p, t, W)$  Lemmon et al. [20]



**Mole Fraction of Air  $\psi_{\text{Air}} = f(W)$** 
**Function Name:**

PsiAir\_W\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION PSIAIR\_W\_HUAIRPROP(W), REAL\*8 W

**Input Values:** $W$  - Humidity ratio  $W$  in  $\text{lb}_w/\text{lb}_a$ **Result:**PsiAir\_W\_HAP\_IP - Mole fraction of (dry) air in humid air in  $\text{mol}_a/\text{mol}$ **Range of Validity:**Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$ **Comments:**

- Mole fraction of air  $\psi_{\text{Air}} = 1 - \psi_{\text{H}_2\text{O}} = 1 - \left( \frac{W}{\frac{R_a}{R_{\text{H}_2\text{O}}} + W} \right)$

**Result for Wrong Input Values:**

PsiAir\_W\_HAP\_IP = -1000

**References:** $\psi_{\text{Air}}(W)$  Herrmann et al. [1], [2]

**Mole Fraction of Water  $\psi_{\text{H}_2\text{O}} = f(W)$** 
**Function Name:**

PsiH2O\_W\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION PSIH2O_W_HUAIRPROP(W), REAL*8 W
```

**Input Values:**

$W$  - Humidity ratio  $W$  in  $\text{lb}_w/\text{lb}_a$

**Result:**

PsiH2O\_W\_HAP\_IP - Mole fraction of water in humid air in  $\text{mol}_w/\text{mol}$

**Range of Validity:**

Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Mole fraction of water  $\psi_{\text{H}_2\text{O}} = \frac{W}{\frac{R_a}{R_{\text{H}_2\text{O}}} + W}$

**Result for Wrong Input Values:**

PsiH2O\_W\_HAP\_IP = -1000

**References:**

$\psi_{\text{H}_2\text{O}}(W)$  Herrmann et al. [1], [2]

**Density  $\rho = f(p, t, W)$** **Function Name:**

Rho\_ptW\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION RHO\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$     -    Total pressure  $p$  in psi  
 $t$     -    Temperature  $t$  in °F  
 $W$     -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**Rho\_ptW\_HAP\_IP - Density of humid air in lb/ft<sup>3</sup>**Range of Validity:**

Temperature  $t$ :                      from -225.67°F to 662°F  
 Total pressure  $p$ :                    from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :                     $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Density of humid air obtained from air-specific volume:  $\rho = \frac{1+W}{v}$

**Result for Wrong Input Values:**

Rho\_ptW\_HAP\_IP = -1000

**References:** $\rho(p, t, W)$  Herrmann et al. [1], [2]

**Air-Specific Entropy  $s = f(p, t, W)$** **Function Name:**

s\_ptW\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION S\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**s\_ptW\_HAP\_IP - Air-specific entropy in Btu/(lb<sub>a</sub> · °R)**Range of Validity:**

Temperature  $t$ : from -225.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

s\_ptW\_HAP\_IP = -1000

**References:** $s(p, t, W)$  Herrmann et al. [1], [2]

**Backward Function: Temperature  $t = f(p, h, \varphi)$** 
**Function Name:**

t\_phphi\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  T_PHPHI_HUAIRPROP(P,H,PHI), REAL*8 P,H,PHI
```

**Input Values:**

$p$      -    Total pressure  $p$  in psi  
 $h$      -    Air-specific enthalpy  $h$  in Btu/lb<sub>a</sub>  
 $\varphi$     -    Relative humidity  $\varphi$  (decimal ratio)

**Result:**

t\_phphi\_HAP\_IP - Temperature from pressure, enthalpy, and relative humidity in °F

**Range of Validity:**

Total pressure  $p$ :                from 0.00145 psi to 1450.4 psi  
 Air-specific enthalpy  $h$ :        from -2469.22 Btu/lb<sub>a</sub> to 12772.088 Btu/lb<sub>a</sub>  
 Relative humidity  $\varphi$ :         $0 \leq \varphi \leq 1$

**Comments:**

- Iteration of temperature  $t$  from  $h = f(p, t, W)$  using  $W = f(p, t, \varphi)$

**Result for Wrong Input Values:**

t\_phphi\_HAP\_IP = -1000

**References:**

$h(p, t, W)$     Herrmann et al. [1], [2]

**Backward Function: Temperature  $t = f(p, h, W)$** **Function Name:**

t\_phW\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION T\_PHW\_HUAIRPROP(P,H,W), REAL\*8 P,H,W

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $h$  - Air-specific enthalpy  $h$  in Btu/lb<sub>a</sub>  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

t\_phW\_HAP\_IP - Temperature from pressure, enthalpy, and humidity ratio in °F

**Range of Validity:**

Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Air-specific enthalpy  $h$ : from -2469.22 Btu/lb<sub>a</sub> to 12772.088 Btu/lb<sub>a</sub>  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**- Iteration of temperature  $t$  from  $h = f(p, t, W)$ **Result for Wrong Input Values:**

t\_phW\_HAP\_IP = -1000

**References:** $h(p, t, W)$  Herrmann et al. [1], [2]

**Backward Function: Temperature  $t = f(p,s,W)$** 
**Function Name:**

t\_psW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION T_PSW_HUAIRPROP(P,S,W), REAL*8 P,S,W
```

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $s$  - Air-specific entropy in Btu/(lb<sub>a</sub> · °R)  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

t\_psW\_HAP\_IP - Temperature from pressure, entropy, and humidity ratio in °F

**Range of Validity:**

Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Air-specific entropy  $s$ : from -6.32 Btu/(lb<sub>a</sub> °R) to 9.32877 Btu/(lb<sub>a</sub> °R)  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Iteration of temperature  $t$  from  $s = f(p,t,W)$

**Result for Wrong Input Values:**

t\_psW\_HAP\_IP = -1000

**References:**

$s(p,t,W)$  Herrmann et al. [1], [2]

## Backward Function: Temperature $t = f(p, t_{wb}, W)$

### Function Name:

`t_ptwbW_HAP_IP`

### Fortran Program:

```
REAL*8 FUNCTION T_PTWWBW_HUAIRPROP(P,TWB,W), REAL*8 P,TWB,W
```

### Input Values:

$p$  - Total pressure  $p$  in psi  
 $t_{wb}$  - Wet-bulb temperature in °F  
 $W$  - Humidity ratio  $W$  in  $\text{lb}_w/\text{lb}_a$

### Result:

`t_ptwbW_HAP_IP` - Temperature from pressure, wet bulb temperature and humidity ratio in °F

### Range of Validity:

Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
Wet bulb temperature  $t_{wb}$ : from -225.67°F to 662°F  
Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

### Comments:

- Iteration of temperature  $t$  from  $t_{wb} = f(p, t, W)$

### Result for Wrong Input Values:

`t_ptwbW_HAP_IP` = -1000

### References:

$t_{wb}(p, t, W)$  Herrmann et al. [1], [2]



**Dew-Point/Frost-Point Temperature  $t_d = f(p, W)$** 
**Function Name:**

td\_pW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION TD_PW_HUAIRPROP(P,W), REAL*8 P,W
```

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

td\_pW\_HAP\_IP - Dew-point/frost-point temperature in °F

**Range of Validity:**

Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

Dew-point temperature  $t_d = t_s(p_{\text{H}_2\text{O}})$  for  $t \geq 32^\circ\text{F}$  (saturation temperature of water in humid air)

$t_d = t_{\text{sub}}(p_{\text{H}_2\text{O}})$  for  $t \leq 32^\circ\text{F}$  (sublimation temperature of water in humid air)

**Result for Wrong Input Values:**

td\_pW\_HAP\_IP = -1000

**References:**

|                                          |                                 |                           |
|------------------------------------------|---------------------------------|---------------------------|
| $t_s(p_{\text{H}_2\text{O}})$            | for $t_d \geq 32^\circ\text{F}$ | IAPWS-IF97 [7], [8]       |
| $t_{\text{sub}}(p_{\text{H}_2\text{O}})$ | for $t_d \leq 32^\circ\text{F}$ | IAPWS-08 [11]             |
| $p_{\text{H}_2\text{O}}$                 |                                 | Herrmann et. al. [1], [2] |

## Saturation Temperature $t_s = f(p, p_{H_2O})$

### Function Name:

ts\_ppH2O\_HAP\_IP

### Fortran Program:

```
REAL*8 FUNCTION TS_PPH2O_HUAIRPROP(P,PH2O), REAL*8 P,PH2O
```

### Input Values:

$p$  - Total pressure  $p$  in psi  
 $p_{H_2O}$  - Partial saturation pressure of water  $p_{H_2O}$  in psi

### Result:

ts\_ppH2O\_HAP\_IP - Saturation temperature of water in humid air in °F

### Range of Validity:

Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Partial pressure  $p_{H_2O}$ : from 0.00145 psi to 1450.4 psi

### Comments:

- Iteration of saturation temperature  $t_s$  from  $p_{H_2O,s} = f(p, t)$

### Result for Wrong Input Values:

ts\_ppH2O\_HAP\_IP = -1000

### References:

$p_{H_2O,s}$  Herrmann et. al. [1], [2]

**Wet-Bulb/Ice-Bulb Temperature  $t_{wb} = f(p, t, W)$** 
**Function Name:**

twb\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION TWB_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in psi  
 $t$        -    Temperature  $t$  in °F  
 $W$       -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

twb\_ptW\_HAP\_IP - Wet-bulb/ice-bulb temperature in °F

**Range of Validity:**

Temperature  $t$ :                      from -225.67°F to 662°F  
 Total pressure  $p$ :                    from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :                    $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Iteration of wet-bulb temperature  $t_{wb}$  from  $h^{\text{unsaturated}}(p, t, W) = h^{\text{fog}}(p, t_{wb}, W)$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

twb\_ptW\_HAP\_IP = -1000

**References:** $t_{wb}(p, t, W)$  Herrmann et al. [1], [2]

**Air-Specific Internal Energy  $u = f(p, t, W)$** 
**Function Name:**

u\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  U_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in psi  
 $t$      -    Temperature  $t$  in °F  
 $W$      -    Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

u\_ptW\_HAP\_IP    -    Air-specific internal energy in Btu/lb<sub>a</sub>

**Range of Validity:**

Temperature  $t$ :                    from -225.67°F to 662°F  
 Total pressure  $p$ :                from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :                 $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Internal energy  $u = h - pv$

**Result for Wrong Input Values:**

u\_ptW\_HAP\_IP = -1000

**References:**

$u(p, t, W)$     Herrmann et al. [1], [2]

**Air-Specific Volume  $v = f(p, t, W)$** 
**Function Name:**

v\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION V_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

v\_ptW\_HAP\_IP - Air-specific volume in ft<sup>3</sup>/lb<sub>a</sub>

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 662°F  
 Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Humidity ratio  $W$ :  $0 \leq W \leq 10$  lb<sub>w</sub>/lb<sub>a</sub>

**Comments:**

- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

v\_ptW\_HAP\_IP = -1000

**References:**

$v(p, t, W)$  Herrmann et al. [1], [2]

## Humidity Ratio from Partial Pressure of Water Vapor $W = f(p, t, p_{\text{H}_2\text{O}})$

### Function Name:

W\_ptpH2O\_HAP\_IP

### Fortran Program:

```
REAL*8 FUNCTION W_PTPH2O_HUAIRPROP(P,T,PH2O), REAL*8 P,T,PH2O
```

### Input Values:

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $p_{\text{H}_2\text{O}}$  - Partial pressure of water  $p_{\text{H}_2\text{O}}$  in psi

### Result:

W\_ptpH2O\_HAP\_IP - Humidity ratio from pressure, temperature and partial pressure of water vapor in  $\text{lb}_w/\text{lb}_a$

### Range of Validity:

Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Temperature  $t$ : from -225.67°F to 662°F  
 Partial pressure  $p_{\text{H}_2\text{O}}$ : from 0.00145 psi to 1450.4 psi

### Comments:

- Iteration of humidity ratio  $W$  from  $p_{\text{H}_2\text{O}} = f(p, t, W)$
- Result for supersaturated humid air is  $W_s$

### Result for Wrong Input Values:

W\_ptpH2O\_HAP\_IP = -1000

### References:

$p_{\text{H}_2\text{O}}(p, t, W)$  Herrmann et al. [1], [2]

## Humidity Ratio from Relative Humidity $W = f(p, t, \varphi)$

### Function Name:

W\_ptphi\_HAP\_IP

### Fortran Program:

```
REAL*8 FUNCTION W_PTPHI_HUAIRPROP(P,T,PHI), REAL*8 P,T,PHI
```

### Input Values:

$p$      -    Total pressure  $p$  in psi  
 $t$        -    Temperature  $t$  in °F  
 $\varphi$       -    Relative humidity (decimal ratio)

### Result:

W\_ptphi\_HAP\_IP    -    Humidity ratio from pressure, temperature and relative humidity in  $\text{lb}_w/\text{lb}_a$

### Range of Validity:

Temperature  $t$ :                      from -225.67°F to 662°F  
 Total pressure  $p$ :                    from 0.00145 psi to 1450.4 psi  
 Relative humidity  $\varphi$ :                 $0 \leq \varphi \leq 1$

### Comments:

- Iteration of humidity ratio  $W$  from  $\varphi = f(p, t, W)$

### Result for Wrong Input Values:

W\_ptphi\_HAP\_IP = -1000

### References:

$\varphi(p, t, W)$     Herrmann et al. [1], [2]

## Humidity Ratio from Dew-Point Temperature $W = f(p, t_d)$

### Function Name:

W\_ptd\_HAP\_IP

### Fortran Program:

```
REAL*8 FUNCTION W_PTD_HUAIRPROP(P,TD), REAL*8 P,TD
```

### Input Values:

$p$  - Total pressure  $p$  in psi  
 $t_d$  - Dew-point temperature  $t_d$  in °F

### Result:

W\_ptd\_HAP\_IP - Humidity ratio from pressure and dew-point temperature  
in lb<sub>w</sub>/lb<sub>a</sub>

### Range of Validity:

Dew point temperature  $t_d$ : from -225.67°F to 662°F  
Total pressure  $p$ : from 0.00145 psi to 1450.4 psi

### Comments:

- Iteration of humidity ratio  $W$  from  $t_d = f(p, W)$

### Result for Wrong Input Values:

W\_ptd\_HAP\_IP = -1000

### References:

$t_d(p, W)$  Herrmann et al. [1], [2]



## Humidity Ratio from Wet-Bulb Temperature $W = f(p, t, t_{wb})$

### Function Name:

W\_pttwb\_HAP\_IP

### Fortran Program:

```
REAL*8 FUNCTION W_PTTWB_HUAIRPROP(P,T,TWB), REAL*8 P,T,TWB
```

### Input Values:

$p$      -    Total pressure  $p$  in psi  
 $t$        -    Temperature  $t$  in °F  
 $t_{wb}$    -    Wet-bulb temperature in °F

### Result:

W\_pttwb\_HAP\_IP    -    Humidity ratio from pressure, temperature and wet-bulb temperature in  $\text{lb}_w/\text{lb}_a$

### Range of Validity:

Total pressure  $p$ :                      from 0.00145 psi to 1450.4 psi  
 Temperature  $t$ :                        from -225.67°F to 662°F  
 Wet-bulb temperature  $t_{wb}$ :        from -225.67°F to 662°F

### Comments:

- Iteration of humidity ratio  $W$  from  $t_{wb} = f(p, t, W)$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

### Result for Wrong Input Values:

W\_pttwb\_HAP\_IP = -1000

### References:

$t_{wb}(p, t, W)$     Herrmann et al. [1], [2]

## Saturation Humidity Ratio $W_s = f(p, t)$

### Function Name:

Ws\_pt\_HAP\_IP

### Fortran Program:

```
REAL*8 FUNCTION WS_PT_HUAIRPROP(P,T), REAL*8 P,T
```

### Input Values:

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F

### Result:

Ws\_pt\_HAP\_IP - Saturation humidity ratio in  $\text{lb}_w/\text{lb}_a$

### Range of Validity:

Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Temperature  $t$ : from -225.67°F to 662°F

### Comments:

- Calculation of saturation humidity ratio  $W_s$  from  $W_s = \frac{M_{\text{H}_2\text{O}}}{M_a} \frac{p_{\text{H}_2\text{O},s}}{(p - p_{\text{H}_2\text{O},s})}$

### Result for Wrong Input Values:

Ws\_pt\_HAP\_IP = -1000

### References:

$p_{\text{H}_2\text{O},s}$  Herrmann et al. [1], [2]

**Mass Fraction of Air  $\xi_{\text{Air}} = f(W)$** 
**Function Name:**

XiAir\_W\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  XIAIR_W_HUAIRPROP(W), REAL*8 W
```

**Input Values:**

$W$  - Humidity ratio  $W$  in  $\text{lb}_w/\text{lb}_a$

**Result:**

XiAir\_W\_HAP\_IP - Mass fraction of (dry) air in humid air in  $\text{lb}_a/\text{lb}$

**Range of Validity:**

Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$

**Comments:**

- Mass fraction of (dry) air  $\xi_{\text{Air}} = 1 - \xi_{\text{H}_2\text{O}} = 1 - \frac{W}{1 + W}$

**Result for Wrong Input Values:**

XiAir\_W\_HAP\_IP = -1000

**References:**

$\xi_{\text{Air}}(W)$  Herrmann et al. [1], [2]

**Mass Fraction of Water Vapor in Humid Air  $\xi_{\text{H}_2\text{O}} = f(W)$** 
**Function Name:**

XiH2O\_W\_HAP\_IP

**Fortran Program:**

REAL\*8 FUNCTION XIH2O\_W\_HUAIRPROP(W), REAL\*8 W

**Input Values:** $W$  - Humidity ratio  $W$  in  $\text{lb}_w/\text{lb}_a$ **Result:**XiH2O\_W\_HAP\_IP - Mass fraction of water vapor in humid air in  $\text{lb}_w/\text{lb}$ **Range of Validity:**Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ lb}_w/\text{lb}_a$ **Comments:**- Mass fraction of water  $\xi_{\text{H}_2\text{O}} = \frac{W}{1+W}$ **Result for Wrong Input Values:**

XiH2O\_W\_HAP\_IP = -1000

**References:** $\xi_{\text{H}_2\text{O}}(W)$  Herrmann et al. [1], [2]

**Compression Factor  $Z = f(p, t, W)$** 
**Function Name:**

Z\_ptW\_HAP\_IP

**Fortran Program:**

```
REAL*8 FUNCTION Z_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F  
 $W$  - Humidity ratio  $W$  in lb<sub>w</sub>/lb<sub>a</sub>

**Result:**

Z\_ptW\_HAP\_IP - Compression factor (decimal ratio)

**Range of Validity:**

Total pressure  $p$ : from 0.00145 psi to 1450.4 psi  
 Temperature  $t$ : from -225.67°F to 662°F  
 Humidity ratio  $W$ :  $0 \leq W \leq W_s$

**Comments:**

- Compression factor  $Z = 1 + \frac{B_m}{\bar{v}} + \frac{C_m}{\bar{v}^2}$

with  $\bar{v} = \frac{M}{\rho} = \frac{M v}{1 + W}$

and  $M$  is the molar mass of humid air

- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

Z\_ptW\_HAP\_IP = -1000

**References:**

$B_m(t, W), C_m(t, W)$  Herrmann et al. [1], [2]

$\rho(p, t, W), v(p, t, W)$  Herrmann et al. [1], [2]

## **3.2 Functions for Steam and Water for Temperatures $t \geq 32^{\circ}\text{F}$**

**Specific Enthalpy of Liquid Water  $h_{\text{liq}} = f(p, t)$** 
**Function Name:**

hliq\_pt\_97\_IP

**Fortran Program:**

REAL\*8 FUNCTION HLIQ\_PT\_97(P,T), REAL\*8 P,T

**Input Values:**

$p$  - Pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F

**Result:**

hliq\_pt\_97\_IP - Specific enthalpy of liquid water in Btu/lb

**Range of Validity:**

Pressure  $p$ : from  $p_s(32^\circ\text{F}) = 0.08865$  psi to 1450.4 psi  
 Temperature  $t$ : from 32°F to 662°F

**Comments:**- Specific enthalpy of liquid water  $h_{\text{liq}} = h^{97}(p, t)$  (Region 1)**Result for Wrong Input Values:**

hliq\_pt\_97\_IP = -1000

**References:** $h^{97}(p, t)$  IAPWS-IF97 [7], [8]

**Specific Enthalpy of Saturated Liquid Water  $h_{\text{liq},s} = f(t)$** 
**Function Name:**

hliqs\_t\_97\_IP

**Fortran Program:**

REAL\*8 FUNCTION HLIQS\_T\_97(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °F**Result:**

hliqs\_t\_97\_IP - Specific enthalpy of saturated liquid water in Btu/lb

**Range of Validity:**Temperature  $t$ : from 32°F to 662°F**Comments:**- Specific enthalpy of liquid water  $h_{\text{liq},s} = h^{97}(p_s, t)$  (Region 1)with  $p_s = p_s^{97}(t)$ **Result for Wrong Input Values:**

hliqs\_t\_97\_IP = -1000

**References:** $h^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]



## Specific Enthalpy of Saturated Water Vapor $h_{\text{vap},s} = f(t)$

**Function Name:**

hvaps\_t\_97\_IP

**Fortran Program:**

```
REAL*8 FUNCTION HVAPS_T_97(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

hvaps\_t\_97\_IP - Specific enthalpy of saturated water vapor in Btu/lb

**Range of Validity:**

Temperature  $t$ : from 32°F to 662°F

**Comments:**

- Specific enthalpy of saturated water vapor  $h_{\text{vap},s} = h^{97}(p_s, t)$  (Region 2)  
with  $p_s = p_s^{97}(t)$

**Result for Wrong Input Values:**

hvaps\_t\_97\_IP = -1000

**References:**

$h^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

## Saturation Pressure of Water $p_s = f(t)$

**Function Name:**

ps\_t\_97\_IP

**Fortran Program:**

```
REAL*8 FUNCTION PS_T_97(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

ps\_t\_97\_IP - Saturation pressure of water in psi

**Range of Validity:**

Temperature  $t$ : from 32°F to 662°F

**Comments:**

- Saturation pressure of water  $p_s = p_s^{97}(t)$  (Region 4)

**Result for Wrong Input Values:**

ps\_t\_97\_IP -1000

**References:**

$p_s^{97}(t)$  IAPWS-IF97 [7], [8]

## Specific Entropy of Liquid Water $s_{\text{liq}} = f(p, t)$

### Function Name:

sliq\_pt\_97\_IP

### Fortran Program:

```
REAL*8 FUNCTION SLIQ_PT_97(P,T), REAL*8 P,T
```

### Input Values:

$p$      -    Pressure  $p$  in psi  
 $t$      -    Temperature  $t$  in °F

### Result:

sliq\_pt\_97\_IP - Specific entropy of liquid water in Btu/(lb °R)

### Range of Validity:

Pressure  $p$ :                      from  $p_s(32^\circ\text{F}) = 0.08865$  psi to 1450.4 psi  
 Temperature  $t$ :                from 32°F to 662°F

### Comments:

- Specific entropy of liquid water  $s_{\text{liq}} = s^{97}(p, t)$  (Region 1)

### Result for Wrong Input Values:

sliq\_pt\_97\_IP = -1000

### References:

$s^{97}(p, t)$      IAPWS-IF97 [7], [8]

**Specific Entropy of Saturated Liquid Water  $s_{\text{liq},s} = f(t)$** 
**Function Name:**

sliqs\_t\_97\_IP

**Fortran Program:**

REAL\*8 FUNCTION SLIQS\_T\_97(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °F**Result:**

sliqs\_t\_97\_IP - Specific entropy of saturated liquid water in Btu/(lb °R)

**Range of Validity:**Temperature  $t$ : from 32°F to 662°F**Comments:**- Specific entropy of liquid water  $s_{\text{liq},s} = s^{97}(p_s, t)$  (Region 1)with  $p_s = p_s^{97}(t)$ **Result for Wrong Input Values:**

sliqs\_t\_97\_IP = -1000

**References:** $s^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

## Specific Entropy of Saturated Water Vapor $s_{\text{vap},s} = f(t)$

**Function Name:**

svaps\_t\_97\_IP

**Fortran Program:**

```
REAL*8 FUNCTION SVAPS_T_97(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

svaps\_t\_97\_IP - Specific entropy of saturated water vapor in Btu/(lb °R)

**Range of Validity:**

Temperature  $t$ : from 32°F to 662°F

**Comments:**

- Specific entropy of saturated water vapor  $s_{\text{vap},s} = s^{97}(p_s, t)$  (Region 2)

with  $p_s = p_s^{97}(t)$

**Result for Wrong Input Values:**

svaps\_t\_97\_IP = -1000

**References:**

$s^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

## Saturation Temperature of Water $t_s = f(p)$

### Function Name:

ts\_p\_97\_IP

### Fortran Program:

```
REAL*8 FUNCTION TS_P_97(P), REAL*8 P
```

### Input Values:

$p$  - Pressure  $p$  in psi

### Result:

ts\_p\_97\_IP - Saturation temperature of water in °F

### Range of Validity:

Pressure  $p$ : from 0.08865 psi to 1450.4 psi

### Comments:

- Saturation temperature of water  $t_s = t_s^{97}(p)$  (Region 4)

### Result for Wrong Input Values:

ts\_p\_97\_IP = -1000

### References:

$t_s^{97}(p)$  IAPWS-IF97 [7], [8]

**Specific Volume of Liquid Water  $v_{\text{liq}} = f(p, t)$** 
**Function Name:**

vliq\_pt\_97\_IP

**Fortran Program:**

```
REAL*8 FUNCTION VLIQ_PT_97(P,T), REAL*8 P,T
```

**Input Values:**

$p$  - Pressure  $p$  in psi  
 $t$  - Temperature  $t$  in °F

**Result:**

vliq\_pt\_97\_IP - Specific volume of liquid water in ft<sup>3</sup>/lb

**Range of Validity:**

Pressure  $p$ : from  $p_s(32^\circ\text{F}) = 0.08865$  psi to 1450.4 psi  
 Temperature  $t$ : from 32°F to 662°F

**Comments:**

- Specific volume of liquid water  $v_{\text{liq}} = v^{97}(p, t)$  (Region 1)

**Result for Wrong Input Values:**

vliq\_pt\_97\_IP = -1000

**References:**

$v^{97}(p, t)$  IAPWS-IF97 [7], [8]

**Specific Volume of Saturated Liquid Water  $v_{\text{liq},s} = f(t)$** 
**Function Name:**

vliqs\_t\_97\_IP

**Fortran Program:**

REAL\*8 FUNCTION VLIQS\_T\_97(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °F**Result:**vliqs\_t\_97\_IP - Specific volume of saturated liquid water in ft<sup>3</sup>/lb**Range of Validity:**Temperature  $t$ : from 32°F to 662°F**Comments:**- Specific volume of liquid water  $v_{\text{liq},s} = v^{97}(p_s, t)$  (Region 1)with  $p_s = p_s^{97}(t)$ **Result for Wrong Input Values:**

vliqs\_t\_97\_IP = -1000

**References:** $v^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]



**Specific Volume of Saturated Water Vapor  $v_{\text{vap},s} = f(t)$** 
**Function Name:**

vvaps\_t\_97\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  VVAPS_T_97(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

vvaps\_t\_97\_IP - Specific volume of saturated water vapor in ft<sup>3</sup>/lb

**Range of Validity:**

Temperature  $t$ : from 32°F to 662°F

**Comments:**

- Specific volume of saturated water vapor  $v_{\text{vap},s} = v^{97}(p_s, t)$  (Region 2)  
with  $p_s = p_s^{97}(t)$

**Result for Wrong Input Values:**

vvaps\_t\_97\_IP = -1000

**References:**

$v^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

### **3.3 Functions for Steam and Water for Temperatures $t \leq 32^{\circ}\text{F}$**

**Specific Enthalpy of Saturated Ice  $h_{\text{ice,sub}} = f(t)$** 
**Function Name:**

hicesub\_t\_06\_IP

**Fortran Program:**

```
REAL*8 FUNCTION HICESUB_T_06(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

hicesub\_t\_06\_IP - Specific enthalpy of saturated ice in Btu/lb

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 32°F

**Comments:**

- Specific enthalpy of saturated ice  $h_{\text{ice,sub}} = h^{06}(\rho_{\text{sub}}, t)$   
 with  $\rho_{\text{sub}} = \rho_{\text{sub}}^{08}(t)$

**Result for Wrong Input Values:**

hicesub\_t\_06\_IP = -1000

**References:**

$h^{06}(p, t)$  IAPWS-06 [10]

$\rho_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

**Specific Enthalpy of Saturated Water Vapor  $h_{\text{vap,sub}} = f(t)$** 
**Function Name:**

hvapsub\_t\_95\_IP

**Fortran Program:**

```
REAL*8 FUNCTION HVAPSUB_T_95(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

hvapsub\_t\_95\_IP - Specific enthalpy of saturated water vapor in Btu/lb

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 32°F

**Comments:**

- Specific enthalpy of saturated water vapor  $h_{\text{vap,sub}} = h^{95}(p_{\text{sub}}, t)$

with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$

**Result for Wrong Input Values:**

hvapsub\_t\_95\_IP = -1000

**References:**

$h^{95}(p, t)$  IAPWS-95 [5], [6]

$p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

## Melting Pressure of Ice $p_{\text{mel}} = f(t)$

**Function Name:**

pmel\_t\_08\_IP

**Fortran Program:**

```
REAL*8 FUNCTION PMEL_T_08 (T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

pmel\_t\_08\_IP - Melting pressure of ice in psi

**Range of Validity:**

Temperature  $t$ : from -7.573°F to 32°F

**Result for Wrong Input Values:**

pmel\_t\_08\_IP = -1000

**References:**

$p_{\text{mel}}^{08}(t)$  IAPWS-08 [11]

## Sublimation Pressure of Ice $p_{\text{sub}} = f(t)$

### Function Name:

psub\_t\_08\_IP

### Fortran Program:

```
REAL*8 FUNCTION PSUB_T_08 (T), REAL*8 T
```

### Input Values:

$t$  - Temperature  $t$  in °F

### Result:

psub\_t\_08\_IP - Sublimation pressure of ice in psi

### Range of Validity:

Temperature  $t$ : from -225.67°F to 32°F

### Result for Wrong Input Values:

psub\_t\_08\_IP = -1000

### References:

$p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

## Specific Entropy of Saturated Ice $s_{\text{ice,sub}} = f(t)$

**Function Name:**

sicesub\_t\_06\_IP

**Fortran Program:**

```
REAL*8 FUNCTION SICESUB_T_06(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

sicesub\_t\_06\_IP - Specific entropy of saturated ice in Btu/(lb °R)

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 32°F

**Comments:**

- Specific entropy of saturated ice  $s_{\text{ice,sub}} = s^{06}(p_{\text{sub}}, t)$   
 with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$

**Result for Wrong Input Values:**

sicesub\_t\_06\_IP = -1000

**References:**

$s^{06}(p, t)$  IAPWS-06 [10]

$p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

**Specific Entropy of Saturated Water Vapor  $s_{\text{vap,sub}} = f(t)$** 
**Function Name:**

svapsub\_t\_95\_IP

**Fortran Program:**

REAL\*8 FUNCTION SVAPSUB\_T\_95(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °F**Result:**

svapsub\_t\_95\_IP - Specific entropy of saturated water vapor in Btu/(lb °R)

**Range of Validity:**Temperature  $t$ : from -225.67°F to 32°F**Comments:**- Specific entropy of saturated water vapor  $s_{\text{vap,sub}} = s^{95}(p_{\text{sub}}, t)$ with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$ **Result for Wrong Input Values:**

svapsub\_t\_95\_IP = -1000

**References:** $s^{95}(p, t)$  IAPWS-95 [7], [8] $p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]



## Melting Temperature of Ice $t_{\text{mel}} = f(p)$

**Function Name:**

tmel\_p\_08\_IP

**Fortran Program:**

```
REAL*8 FUNCTION TMEL_P_08(P), REAL*8 P
```

**Input Values:**

$p$  - Pressure  $p$  in psi

**Result:**

tmel\_p\_08\_IP - Melting temperature of ice in °F

**Range of Validity:**

Pressure  $p$ : from  $p_s$  (32°F) = 0.08865 psi to 1450.4 psi

**Result for Wrong Input Values:**

tmel\_p\_08\_IP = -1000

**References:**

$t_{\text{mel}}^{08}(p)$  IAPWS-08 [11]

**Sublimation Temperature of Ice  $t_{\text{sub}} = f(p)$** 
**Function Name:**

tsub\_p\_08\_IP

**Fortran Program:**

```
REAL*8 FUNCTION TSUB_P_08(P), REAL*8 P
```

**Input Values:**

$p$  - Pressure  $p$  in psi

**Result:**

tsub\_p\_08\_IP - Sublimation temperature of ice in °F

**Range of Validity:**

Pressure  $p$ : from  $p_{\text{subl}}(-225.67^\circ\text{F}) = 1.7407 \times 10^{-12}$  psi to  $p_{\text{subl}}(32^\circ\text{F}) = 0.08865$  psi

**Result for Wrong Input Values:**

tsub\_p\_08\_IP = -1000

**References:**

$t_{\text{sub}}^{08}(p)$  IAPWS-08 [11]

**Specific Volume of Saturated Ice  $v_{\text{ice,sub}} = f(t)$** 
**Function Name:**

vicesub\_t\_06\_IP

**Fortran Program:**

REAL\*8 FUNCTION VICESUB\_T\_06(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °F**Result:**vicesub\_t\_06\_IP - Specific volume of saturated ice in ft<sup>3</sup>/lb**Range of Validity:**Temperature  $t$ : from -225.67°F to 32°F**Comments:**- Specific volume of saturated ice  $v_{\text{ice,sub}} = v^{06}(p_{\text{sub}}, t)$ with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$ **Result for Wrong Input Values:**

vicesub\_t\_06\_IP = -1000

**References:** $v^{06}(p, t)$  IAPWS-06 [10] $p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

**Specific Volume of Saturated Water Vapor  $v_{\text{vap,sub}} = f(t)$** 
**Function Name:**

vvapsub\_t\_95\_IP

**Fortran Program:**

```
REAL*8 FUNCTION  VVAPSUB_T_95(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °F

**Result:**

vvapsub\_t\_95\_IP - Specific volume of saturated water vapor in ft<sup>3</sup>/lb

**Range of Validity:**

Temperature  $t$ : from -225.67°F to 32°F

**Comments:**

- Specific volume of saturated water vapor  $v_{\text{vap,sub}} = v^{95}(p_{\text{sub}}, t)$

with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$

**Result for Wrong Input Values:**

vvapsub\_t\_95\_IP = -1000

**References:**

$v^{95}(p, t)$  IAPWS-95 [7], [8]

$p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]



## 4. Property Libraries for Calculating Heat Cycles, Boilers, Turbines and Refrigerators

### Water and Steam

#### Library LibIF97

- Industrial Formulation IAPWS-IF97 (Revision 2007)
- Supplementary Standards
  - IAPWS-IF97-S01
  - IAPWS-IF97-S03rev
  - IAPWS-IF97-S04
  - IAPWS-IF97-S05
- IAPWS Revised Advisory Note No. 3 on Thermodynamic Derivatives (2008)

### Humid Combustion Gas Mixtures

#### Library LibHuGas

Model: Ideal mixture of the real fluids:  
 $\text{CO}_2$  - Span and Wagner     $\text{O}_2$  - Schmidt and Wagner  
 $\text{H}_2\text{O}$  - IAPWS-95    Ar - Tegeler et al.  
 $\text{N}_2$  - Span et al.  
 and of the ideal gases:  
 $\text{SO}_2$ , CO, Ne (Scientific Formulation of Bückner et al.)  
 Consideration of:  
 Dissociation from VDI 4670 and Poynting effect

### Humid Air

#### Library LibHuAir

Model: Ideal mixture of the real fluids:  
 • Dry air from Lemmon et al.  
 • Steam, water and ice from IAPWS-IF97 and IAPWS-06  
 Consideration of:  
 • Condensation and freezing of steam  
 • Dissociation from the VDI 4670  
 • Poynting effect from ASHRAE RP-1485

### Carbon Dioxide Including Dry Ice

#### Library LibCO2

Formulation of Span and Wagner (1996)

### Seawater

#### Library LibSeaWa

IAPWS Industrial Formulation 2013

### Ice

#### Library LibICE

Ice from IAPWS-06, Melting and sublimation pressures from IAPWS-08, Water from IAPWS-IF97, Steam from IAPWS-95 and -IF97

### Ideal Gas Mixtures

#### Library LibIdGasMix

Model: Ideal mixture of the ideal gases:  

|               |                      |               |            |
|---------------|----------------------|---------------|------------|
| Ar            | NO                   | He            | Propylene  |
| Ne            | $\text{H}_2\text{O}$ | $\text{F}_2$  | Propane    |
| $\text{N}_2$  | $\text{SO}_2$        | $\text{NH}_3$ | Iso-Butane |
| $\text{O}_2$  | $\text{H}_2$         | Methane       | n-Butane   |
| CO            | $\text{H}_2\text{S}$ | Ethane        | Benzene    |
| $\text{CO}_2$ | OH                   | Ethylene      | Methanol   |
| Air           |                      |               |            |

Consideration of:  
 • Dissociation from the VDI Guideline 4670

#### Library LibIDGAS

Model: Ideal gas mixture from VDI Guideline 4670

Consideration of:  
 • Dissociation from the VDI Guideline 4670

### Humid Air

#### Library ASHRAE LibHuAirProp

Model: Virial Equation from ASHRAE Report RP-1485 for real mixture of the real fluids:  
 - Dry air  
 - Steam

Consideration of:  
 • Enhancement of the partial saturation pressure of water vapor at elevated total pressures  
[www.ashrae.org/bookstore](http://www.ashrae.org/bookstore)

### Dry Air Including Liquid Air

#### Library LibRealAir

Formulation of Lemmon et al. (2000)

### Refrigerants

#### Ammonia

#### Library LibNH3

Formulation of Tillner-Roth et al. (1993)

#### R134a

#### Library LibR134a

Formulation of Tillner-Roth and Baehr (1994)

#### Iso-Butane

#### Library LibButane\_Iso

Formulation of Bückner and Wagner (2006)

#### n-Butane

#### Library LibButane\_n

Formulation of Bückner and Wagner (2006)

### Mixtures for Absorption Processes

#### Ammonia/Water Mixtures

#### Library LibAmWa

IAPWS Guideline 2001 of Tillner-Roth and Friend (1998)  
 Helmholtz energy equation for the mixing term  
 (also useable for calculating Kalina Cycle)

#### Water/Lithium Bromide Mixtures

#### Library LibWaLi

Formulation of Kim and Infante Ferreira (2004)  
 Gibbs energy equation for the mixing term

### Liquid Coolants

#### Liquid Secondary Refrigerants

#### Library LibSecRef

Liquid solutions of water with

|                                   |                     |
|-----------------------------------|---------------------|
| $\text{C}_2\text{H}_6\text{O}_2$  | Ethylene glycol     |
| $\text{C}_3\text{H}_8\text{O}_2$  | Propylene glycol    |
| $\text{C}_2\text{H}_5\text{OH}$   | Ethyl alcohol       |
| $\text{CH}_3\text{OH}$            | Methyl alcohol      |
| $\text{C}_3\text{H}_8\text{O}_3$  | Glycerol            |
| $\text{K}_2\text{CO}_3$           | Potassium carbonate |
| $\text{CaCl}_2$                   | Calcium chloride    |
| $\text{MgCl}_2$                   | Magnesium chloride  |
| NaCl                              | Sodium chloride     |
| $\text{C}_2\text{H}_3\text{KO}_2$ | Potassium acetate   |

Formulation of the International Institute of Refrigeration (1997)

**Ethanol****Library LibC2H5OH**

Formulation of Schroeder (2012)

**Methanol****Library LibCH3OH**Formulation of  
de Reuck and Craven (1993)**Propane****Library LibPropane**Formulation of  
Lemmon et al. (2009)**Siloxanes as ORC Working Fluids**Octamethylcyclotetrasiloxane  $C_8H_{24}O_4Si_4$  **Library LibD4**Decamethylcyclopentasiloxane  $C_{10}H_{30}O_5Si_5$  **Library LibD5**Tetradecamethylhexasiloxane  $C_{14}H_{42}O_6Si_6$  **Library LibMD4M**Hexamethyldisiloxane  $C_6H_{18}OSi_2$  **Library LibMM**

Formulation of Colonna et al. (2006)

Dodecamethylcyclohexasiloxane  $C_{12}H_{36}O_6Si_6$  **Library LibD6**Decamethyltetrasiloxane  $C_{10}H_{30}O_3Si_4$  **Library LibMD2M**Dodecamethylpentasiloxane  $C_{12}H_{36}O_4Si_5$  **Library LibMD3M**Octamethyltrisiloxane  $C_8H_{24}O_2Si_3$  **Library LibMDM**

Formulation of Colonna et al. (2008)

**Nitrogen****Library LibN2**Formulation of  
Span et al. (2000)**Hydrogen****Library LibH2**Formulation of  
Leachman et al. (2009)**Helium****Library LibHe**

Formulation of Arp et al. (1998)

**Hydrocarbons**Decane  $C_{10}H_{22}$  **Library LibC10H22**Isopentane  $C_5H_{12}$  **Library LibC5H12\_ISO**Neopentane  $C_5H_{12}$  **Library LibC5H12\_NEO**Isohexane  $C_6H_{14}$  **Library LibC6H14**Toluene  $C_7H_8$  **Library LibC7H8**

Formulation of Lemmon and Span (2006)

**Further Fluids**Carbon monoxide  $CO$  **Library LibCO**Carbonyl sulfide  $COS$  **Library LibCOS**Hydrogen sulfide  $H_2S$  **Library LibH2S**Dinitrogen monoxide  $N_2O$  **Library LibN2O**Sulfur dioxide  $SO_2$  **Library LibSO2**Acetone  $C_3H_6O$  **Library LibC3H6O**

Formulation of Lemmon and Span (2006)

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**The following thermodynamic and transport properties can be calculated<sup>a</sup>:****Thermodynamic Properties**

- Vapor pressure  $p_s$
- Saturation temperature  $T_s$
- Density  $\rho$
- Specific volume  $v$
- Enthalpy  $h$
- Internal energy  $u$
- Entropy  $s$
- Exergy  $e$
- Isobaric heat capacity  $c_p$
- Isochoric heat capacity  $c_v$
- Isentropic exponent  $\kappa$
- Speed of sound  $w$
- Surface tension  $\sigma$

**Transport Properties**

- Dynamic viscosity  $\eta$
- Kinematic viscosity  $\nu$
- Thermal conductivity  $\lambda$
- Prandtl number  $Pr$

**Backward Functions**

- $T, v, s(p, h)$
- $T, v, h(p, s)$
- $p, T, v(h, s)$
- $p, T(v, h)$
- $p, T(v, u)$

**Thermodynamic Derivatives**

- Partial derivatives can be calculated.

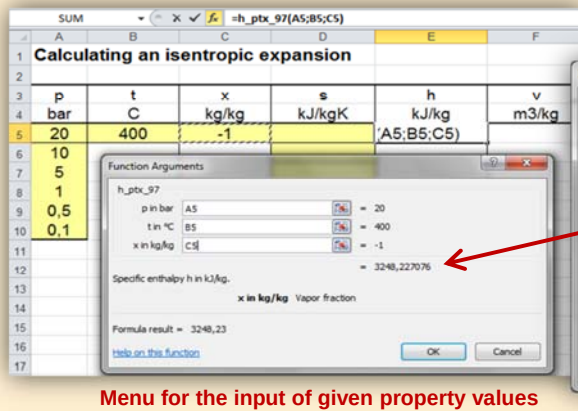
<sup>a</sup> Not all of these property functions are available in all property libraries.



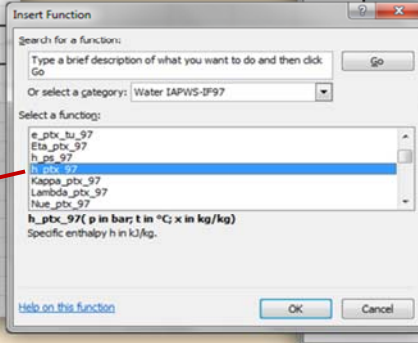


## Property Software for Calculating Heat Cycles, Boilers, Turbines and Refrigerators

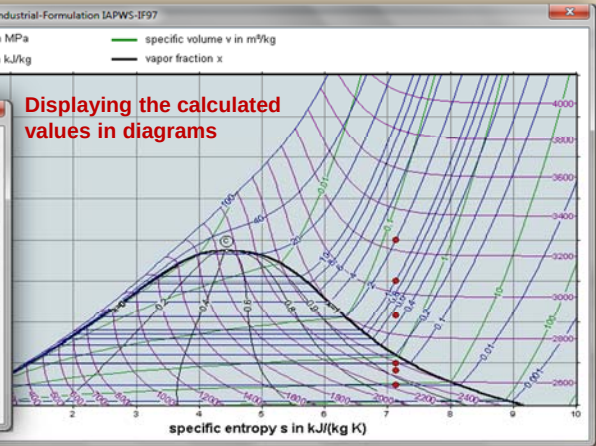
### Add-In FluidEXL<sup>Graphics</sup> for Excel<sup>®</sup>



Choosing a property library and a function

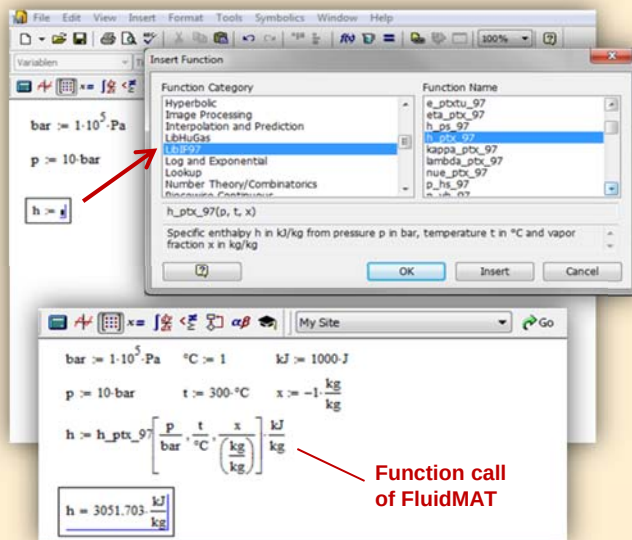


Displaying the calculated values in diagrams



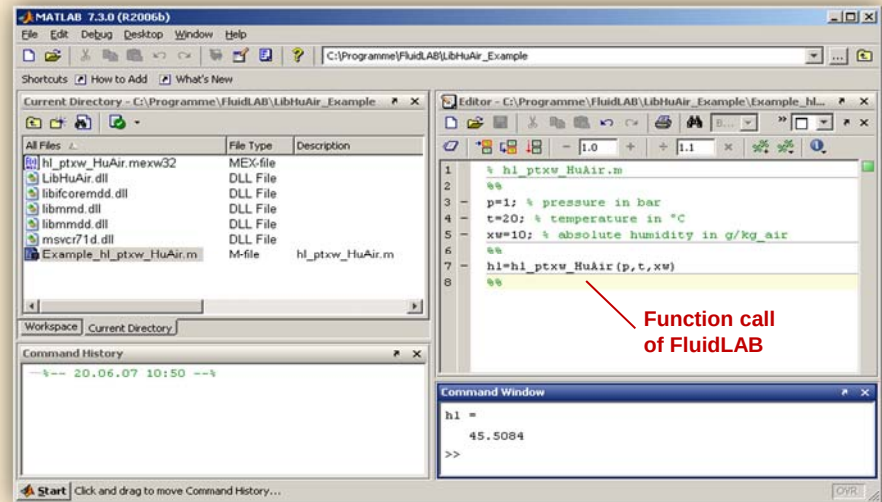
### Add-In FluidMAT<sup>®</sup> for Mathcad<sup>®</sup>

The property libraries can be used in Mathcad<sup>®</sup>.



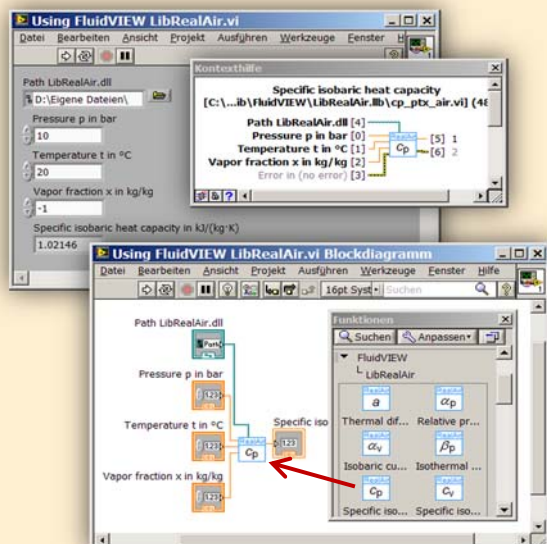
### Add-In FluidLAB<sup>®</sup> for MATLAB<sup>®</sup>

Using the Add-In FluidLAB the property functions can be called in MATLAB<sup>®</sup>.



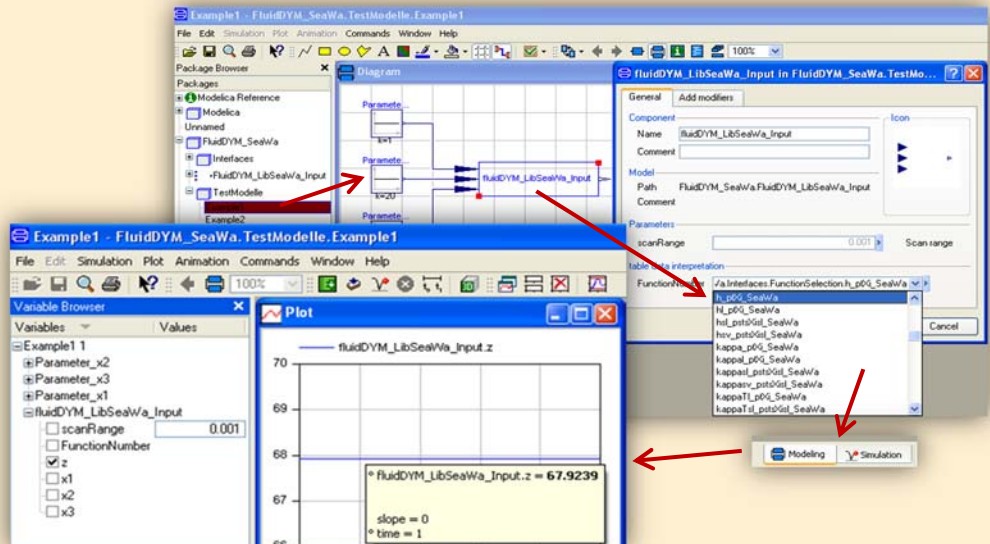
### Add-On FluidVIEW<sup>®</sup> for LabVIEW<sup>®</sup>

The property functions can be calculated in LabVIEW<sup>®</sup>.

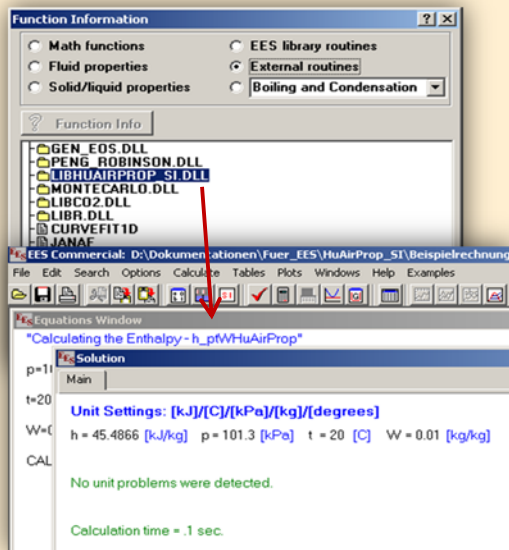


### Add-In FluidDYM<sup>®</sup> for DYMOLA<sup>®</sup> (Modelica) and SimulationX<sup>®</sup>

The property functions can be called in DYMOLA<sup>®</sup> and SimulationX<sup>®</sup>.



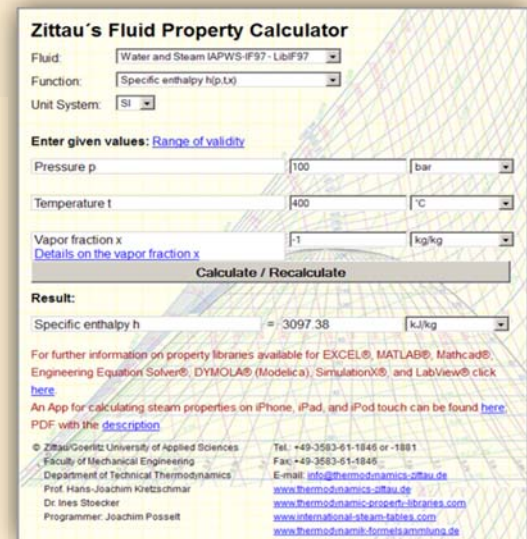
## Add-In FluidEES for Engineering Equation Solver®



## App International Steam Tables for iPhone, iPad, iPod touch, Android smart phones and tablets



## Online Property Calculator at [www.thermodynamics-zittau.de](http://www.thermodynamics-zittau.de)



## Property Software for Pocket Calculators

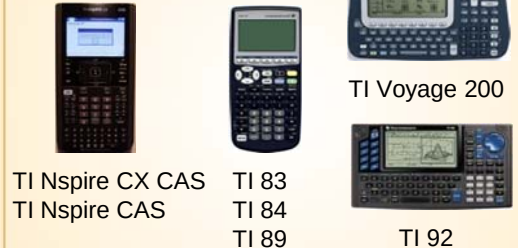
### FluidCasio



### FluidHP



### FluidTI



## For more information please contact:

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The following thermodynamic and transport properties<sup>a</sup> can be calculated in Excel®, MATLAB®, Mathcad®, Engineering Equation Solver® EES, DYMOLA® (Modelica), SimulationX®, and LabVIEW®:

### Thermodynamic Properties

- Vapor pressure  $p_s$
- Saturation temperature  $T_s$
- Density  $\rho$
- Specific volume  $v$
- Enthalpy  $h$
- Internal energy  $u$
- Entropy  $s$
- Exergy  $e$
- Isobaric heat capacity  $c_p$
- Isochoric heat capacity  $c_v$
- Isentropic exponent  $\kappa$
- Speed of sound  $w$
- Surface tension  $\sigma$

### Transport Properties

- Dynamic viscosity  $\eta$
- Kinematic viscosity  $\nu$
- Thermal conductivity  $\lambda$
- Prandtl-number  $Pr$

### Backward Functions

- $T, v, s(p, h)$
- $T, v, h(p, s)$
- $p, T, v(h, s)$
- $p, T(v, h)$
- $p, T(v, u)$

### Thermodynamic Derivatives

- Partial derivatives can be calculated.

<sup>a</sup> Not all of these property functions are available in all property libraries.



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# Part SI Units

# 1 Property Library ASHRAE-LibHuAirProp-SI

## 1.1 Function Overview

### 1.1.1 Function Overview for Real Moist Air

| Functional Dependence                 | Function Name     | Property or Function                         | Unit of the Result | Page |
|---------------------------------------|-------------------|----------------------------------------------|--------------------|------|
| $a = f(p, t, W)$                      | a_ptW_HAP_SI      | Thermal diffusivity                          | m <sup>2</sup> /s  | 3/2  |
| $\alpha_p = f(p, t, W)$               | alphap_ptW_HAP_SI | Relative pressure coefficient                | 1/K                | 3/3  |
| $\beta_p = f(p, t, W)$                | betap_ptW_HAP_SI  | Isothermal stress coefficient                | kg/m <sup>3</sup>  | 3/4  |
| $c = f(p, t, W)$                      | c_ptW_HAP_SI      | Speed of sound                               | m/s                | 3/5  |
| $c_p = f(p, t, W)$                    | cp_ptW_HAP_SI     | Specific isobaric heat capacity              | kJ/(kg·K)          | 3/6  |
| $c_v = f(p, t, W)$                    | cv_ptW_HAP_SI     | Specific isochoric heat capacity             | kJ/(kg·K)          | 3/7  |
| $f = f(p, t)$                         | f_pt_HAP_SI       | Enhancement factor (decimal ratio)           | -                  | 3/8  |
| $h = f(p, t, W)$                      | h_ptW_HAP_SI      | Air-specific enthalpy                        | kJ/kg <sub>a</sub> | 3/9  |
| $\eta = f(p, t, W)$                   | Eta_ptW_HAP_SI    | Dynamic viscosity                            | Pa·s               | 3/10 |
| $\kappa = f(p, t, W)$                 | Kappa_ptW_HAP_SI  | Isentropic exponent                          | -                  | 3/11 |
| $\lambda = f(p, t, W)$                | Lambda_ptW_HAP_SI | Thermal conductivity                         | W/(m·K)            | 3/12 |
| $\nu = f(p, t, W)$                    | Ny_ptW_HAP_SI     | Kinematic viscosity                          | m <sup>2</sup> /s  | 3/13 |
| $p = f(t, s, W)$                      | p_tsW_HAP_SI      | Pressure of humid air                        | kPa                | 3/14 |
| $p = f(z_{\text{ele}})$               | p_zele_HAP_SI     | Pressure of humid air from elevation         | kPa                | 3/15 |
| $p_{\text{Air}} = f(p, t, W)$         | pAIR_ptW_HAP_SI   | Partial pressure of dry air in moist air     | kPa                | 3/16 |
| $p_{\text{H}_2\text{O}} = f(p, t, W)$ | pH2O_ptW_HAP_SI   | Partial pressure of water vapor in moist air | kPa                | 3/17 |
| $p_{\text{H}_2\text{O}s} = f(p, t)$   | pH2Os_pt_HAP_SI   | Partial saturation pressure of water vapor   | kPa                | 3/18 |

| Functional Dependence   | Function Name   | Property or Function                                                                                       | Unit of the Result               | Page |
|-------------------------|-----------------|------------------------------------------------------------------------------------------------------------|----------------------------------|------|
| $\phi = f(p, t, W)$     | phi_ptW_HAP_SI  | Relative humidity (decimal ratio)                                                                          | -                                | 3/19 |
| $Pr = f(p, t, W)$       | Pr_ptW_HAP_SI   | PRANDTL number                                                                                             | -                                | 3/20 |
| $\psi_{Air} = f(W)$     | PsiAir_W_HAP_SI | Mole fraction of dry air in moist air                                                                      | mol <sub>a</sub> /mol            | 3/21 |
| $\psi_{H_2O} = f(W)$    | PsiH2O_W_HAP_SI | Mole fraction of water vapor in moist air                                                                  | mol <sub>w</sub> /mol            | 3/22 |
| $\rho = f(p, t, W)$     | Rho_ptW_HAP_SI  | Density                                                                                                    | kg/m <sup>3</sup>                | 3/23 |
| $s = f(p, t, W)$        | s_ptW_HAP_SI    | Air-specific entropy                                                                                       | kJ/(kg <sub>a</sub> ·K)          | 3/24 |
| $t = f(p, h, \phi)$     | t_phphi_HAP_SI  | Backward function: temperature from total pressure, air-specific enthalpy and relative humidity            | °C                               | 3/25 |
| $t = f(p, h, W)$        | t_phW_HAP_SI    | Backward function: temperature from total pressure, air-specific enthalpy and humidity ratio               | °C                               | 3/26 |
| $t = f(p, s, W)$        | t_psW_HAP_SI    | Backward function: temperature from total pressure, air-specific entropy and humidity ratio                | °C                               | 3/27 |
| $t = f(p, t_{wb}, W)$   | t_ptwbW_HAP_SI  | Backward function: temperature from total pressure, wet-bulb temperature and humidity ratio                | °C                               | 3/28 |
| $t_d = f(p, W)$         | td_pW_HAP_SI    | Dew-point/frost-point temperature                                                                          | °C                               | 3/29 |
| $t_s = f(p, p_{H_2O})$  | ts_ppH2O_HAP_SI | Backward function: saturation temperature of water from total pressure and partial pressure of water vapor | °C                               | 3/30 |
| $t_{wb} = f(p, t, W)$   | twb_ptW_HAP_SI  | Wet-bulb/ice-bulb temperature                                                                              | °C                               | 3/31 |
| $u = f(p, t, W)$        | u_ptW_HAP_SI    | Air-specific internal energy                                                                               | kJ/kg <sub>a</sub>               | 3/32 |
| $v = f(p, t, W)$        | v_ptW_HAP_SI    | Air-specific volume                                                                                        | m <sup>3</sup> /kg <sub>a</sub>  | 3/33 |
| $W = f(p, t, p_{H_2O})$ | W_ptpH2O_HAP_SI | Humidity ratio from total pressure, temperature, and partial pressure of water vapor                       | kg <sub>w</sub> /kg <sub>a</sub> | 3/34 |
| $W = f(p, t, \phi)$     | W_ptphi_HAP_SI  | Humidity ratio from total pressure, temperature, and relative humidity                                     | kg <sub>w</sub> /kg <sub>a</sub> | 3/35 |
| $W = f(p, t_d)$         | W_ptd_HAP_SI    | Humidity ratio from total pressure and dew-point temperature                                               | kg <sub>w</sub> /kg <sub>a</sub> | 3/36 |

| Functional Dependence | Function Name  | Property or Function                                                                 | Unit of the Result               | Page |
|-----------------------|----------------|--------------------------------------------------------------------------------------|----------------------------------|------|
| $W = f(p, t, t_{wb})$ | W_pttwb_HAP_SI | Humidity ratio from total pressure, (dry bulb) temperature, and wet-bulb temperature | kg <sub>w</sub> /kg <sub>a</sub> | 3/37 |
| $W_s = f(p, t)$       | Ws_pt_HAP_SI   | Saturation humidity ratio                                                            | kg <sub>w</sub> /kg <sub>a</sub> | 3/38 |
| $\xi_{Air} = f(W)$    | XiAir_W_HAP_SI | Mass fraction of dry air in moist air                                                | kg <sub>a</sub> /kg              | 3/39 |
| $\xi_{H_2O} = f(W)$   | XiH2O_W_HAP_SI | Mass fraction of water vapor in moist air                                            | kg <sub>w</sub> /kg              | 3/40 |
| $Z = f(p, t, W)$      | Z_ptW_HAP_SI   | Compression factor (decimal ratio)                                                   | -                                | 3/41 |

### Range of Validity of Thermodynamic Properties

| Property               | Range of Validity                                   |
|------------------------|-----------------------------------------------------|
| Pressure:              | $0.01 \leq p \leq 10\,000$ kPa                      |
| Temperature:           | $-143.15 \leq t \leq 350$ °C                        |
| Humidity ratio:        | $0 \leq W \leq 10$ kg <sub>w</sub> /kg <sub>a</sub> |
| Relative humidity:     | $0 \leq \varphi \leq 1$ (decimal ratio)             |
| Dew-point temperature: | $-143.15 \leq t_d \leq 350$ °C                      |
| Wet-bulb temperature:  | $-143.15 \leq t_{wb} \leq 350$ °C                   |

### Units

| Symbol    | Quantity              | Unit                                                     |
|-----------|-----------------------|----------------------------------------------------------|
| $p$       | Pressure              | kPa                                                      |
| $t$       | Temperature           | °C                                                       |
| $W$       | Humidity ratio        | kg <sub>w</sub> /kg <sub>a</sub> (kg water / kg dry air) |
| $\varphi$ | Relative humidity     | (decimal ratio)                                          |
| $t_d$     | Dew point temperature | °C                                                       |
| $t_{wb}$  | Wet bulb temperature  | °C                                                       |

### Range of Validity of Transport Properties

| Property           | Range of Validity                                   |
|--------------------|-----------------------------------------------------|
| Pressure:          | $0.01 \leq p \leq 10\,000$ kPa                      |
| Temperature:       | $-73.15 \leq t \leq 350$ °C                         |
| Humidity ratio:    | $0 \leq W \leq 10$ kg <sub>w</sub> /kg <sub>a</sub> |
| Relative humidity: | $0 \leq \varphi \leq 1$ (decimal ratio)             |

### Molar Masses

| Component | Molar Mass        | Reference |
|-----------|-------------------|-----------|
| Dry Air   | 28.966 kg/kmol    | [17]      |
| Water     | 18.015268 kg/kmol | [5], [6]  |

### Reference States

| Property    | Dry Air     | Steam, Water, and Ice                    |
|-------------|-------------|------------------------------------------|
| Pressure    | 101.325 kPa | $p_s(0.01^\circ\text{C}) = 0.611657$ kPa |
| Temperature | 0°C         | 0.01°C                                   |
| Enthalpy    | 0 kJ/kg     | 0.000611782 kJ/kg                        |
| Entropy     | 0 kJ/(kg K) | 0 kJ/(kg K)                              |

### 1.1.2 Function Overview for Steam and Water for Temperatures $t \geq 0^\circ\text{C}$

| Functional Dependence      | Function Name | Property                                    | Unit of the Result     | Page |
|----------------------------|---------------|---------------------------------------------|------------------------|------|
| $h_{\text{liq}} = f(p, t)$ | hliq_pt_97_SI | Specific enthalpy of liquid water           | kJ/kg                  | 3/43 |
| $h_{\text{liq,s}} = f(t)$  | hliqs_t_97_SI | Specific enthalpy of saturated liquid water | kJ/kg                  | 3/44 |
| $h_{\text{vap,s}} = f(t)$  | hvaps_t_97_SI | Specific enthalpy of saturated water vapor  | kJ/kg                  | 3/45 |
| $p_s = f(t)$               | ps_t_97_SI    | Saturation pressure of water                | kPa                    | 3/46 |
| $s_{\text{liq}} = f(p, t)$ | sliq_pt_97_SI | Specific entropy of liquid water            | kJ/(kg·K)              | 3/47 |
| $s_{\text{liq,s}} = f(t)$  | sliqs_t_97_SI | Specific entropy of saturated liquid water  | kJ/(kg·K)              | 3/48 |
| $s_{\text{vap,s}} = f(t)$  | svaps_t_97_SI | Specific entropy of saturated water vapor   | kJ/(kg·K)              | 3/49 |
| $t_s = f(p)$               | ts_p_97_SI    | Saturation temperature of water             | $^\circ\text{C}$       | 3/50 |
| $v_{\text{liq}} = f(p, t)$ | vliq_pt_97_SI | Specific volume of liquid water             | $\text{m}^3/\text{kg}$ | 3/51 |
| $v_{\text{liq,s}} = f(t)$  | vliqs_t_97_SI | Specific volume of saturated liquid water   | $\text{m}^3/\text{kg}$ | 3/52 |
| $v_{\text{vap,s}} = f(t)$  | vvaps_t_97_SI | Specific volume of saturated water vapor    | $\text{m}^3/\text{kg}$ | 3/53 |



**Range of Validity**

| Property     | Range of Validity                            |
|--------------|----------------------------------------------|
| Pressure:    | $0.01 \leq p \leq 10\,000 \text{ kPa}$       |
| Temperature: | $0 \leq t \leq 350 \text{ }^{\circ}\text{C}$ |

**Reference State**

| Property    | Water Vapor and Liquid Water                       |
|-------------|----------------------------------------------------|
| Pressure    | $p_s(0.01^{\circ}\text{C}) = 0.611657 \text{ kPa}$ |
| Temperature | $0.01^{\circ}\text{C}$                             |
| Enthalpy    | $0.000611782 \text{ kJ/kg}$                        |
| Entropy     | $0 \text{ kJ/(kg K)}$                              |

**Units**

| Symbol | Quantity    | Unit               |
|--------|-------------|--------------------|
| $p$    | Pressure    | kPa                |
| $t$    | Temperature | $^{\circ}\text{C}$ |

### 1.1.3 Function Overview for Steam and Ice for Temperatures $t \leq 0^\circ\text{C}$

| Functional Dependence       | Function Name   | Property                                   | Unit of the Result     | Page |
|-----------------------------|-----------------|--------------------------------------------|------------------------|------|
| $h_{\text{ice,sub}} = f(t)$ | hicesub_t_06_SI | Specific enthalpy of saturated ice         | kJ/kg                  | 3/55 |
| $h_{\text{vap,sub}} = f(t)$ | hvapsub_t_95_SI | Specific enthalpy of saturated water vapor | kJ/kg                  | 3/56 |
| $p_{\text{mel}} = f(t)$     | pmel_t_08_SI    | Melting pressure of ice                    | kPa                    | 3/57 |
| $p_{\text{sub}} = f(t)$     | psub_t_08_SI    | Sublimation pressure of ice                | kPa                    | 3/58 |
| $s_{\text{ice,sub}} = f(t)$ | sicesub_t_06_SI | Specific entropy of saturated ice          | kJ/(kg·K)              | 3/59 |
| $s_{\text{vap,sub}} = f(t)$ | svapsub_t_95_SI | Specific entropy of saturated water vapor  | kJ/(kg·K)              | 3/60 |
| $t_{\text{mel}} = f(p)$     | tmel_p_08_SI    | Melting temperature of ice                 | $^\circ\text{C}$       | 3/61 |
| $t_{\text{sub}} = f(p)$     | tsub_p_08_SI    | Sublimation temperature of ice             | $^\circ\text{C}$       | 3/62 |
| $v_{\text{ice,sub}} = f(t)$ | vicesub_t_06_SI | Specific volume of saturated ice           | $\text{m}^3/\text{kg}$ | 3/63 |
| $v_{\text{vap,sub}} = f(t)$ | vvapsub_t_95_SI | Specific volume of saturated water vapor   | $\text{m}^3/\text{kg}$ | 3/64 |

**Range of Validity**

| Property     | Range of Validity                                                                                |
|--------------|--------------------------------------------------------------------------------------------------|
| Pressure:    | $p_{\text{sub}}(-143.15^\circ\text{C}) = 1.2002 \times 10^{-11} \leq p \leq 10\,000 \text{ kPa}$ |
| Temperature: | $-143.15 \leq t \leq 0 \quad ^\circ\text{C}$                                                     |

**Units**

| Symbol | Quantity    | Unit             |
|--------|-------------|------------------|
| $p$    | Pressure    | kPa              |
| $t$    | Temperature | $^\circ\text{C}$ |

**Reference State**

| Property    | Water Vapor and Ice                              |
|-------------|--------------------------------------------------|
| Pressure    | $p_s(0.01^\circ\text{C}) = 0.611657 \text{ kPa}$ |
| Temperature | $0.01^\circ\text{C}$                             |
| Enthalpy    | $0.000611782 \text{ kJ/kg}$                      |
| Entropy     | $0 \text{ kJ/(kg K)}$                            |

## 1.2 Conversion of SI and I-P Units

| Property                                 | Conversion: SI Units → I-P Units                                                                           | Conversion: I-P Units → SI Units                                                                        | Units SI          | Units I-P            |
|------------------------------------------|------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------|-------------------|----------------------|
| Thermal diffusivity $a$                  | $\frac{a_{IP}}{\frac{ft^2}{s}} = \frac{a_{SI}}{\frac{m^2}{s}} \times 10.76391042$                          | $\frac{a_{SI}}{\frac{m^2}{s}} = \frac{a_{IP}}{\frac{ft^2}{s}} \times 0.0929304$                         | m <sup>2</sup> /s | ft <sup>2</sup> /s   |
| Relative pressure coefficient $\alpha_p$ | $\frac{\alpha_{p,IP}}{\frac{1}{^\circ R}} = \frac{\alpha_{p,SI}}{\frac{1}{K}} \times \frac{9}{5}$          | $\frac{\alpha_{p,SI}}{\frac{1}{K}} = \frac{\alpha_{p,IP}}{\frac{1}{^\circ R}} \times \frac{5}{9}$       | 1/K               | 1/°R                 |
| Isothermal stress coefficient $\beta_p$  | $\frac{\beta_{p,IP}}{\frac{lb}{ft^3}} = \frac{\beta_{p,SI}}{\frac{kg}{m^3}} \times 0.062428$               | $\frac{\beta_{p,SI}}{\frac{kg}{m^3}} = \frac{\beta_{p,IP}}{\frac{lb}{ft^3}} \times 16.018463$           | kg/m <sup>3</sup> | lb/ft <sup>3</sup>   |
| Speed of sound $c$                       | $\frac{c_{IP}}{\frac{ft}{s}} = \frac{c_{SI}}{\frac{m}{s}} \times 3.2808399$                                | $\frac{c_{SI}}{\frac{m}{s}} = \frac{c_{IP}}{\frac{ft}{s}} \times 0.3048$                                | m/s               | ft/s                 |
| Specific isobaric heat capacity $c_p$    | $\frac{c_{p,IP}}{\frac{Btu}{lb \cdot ^\circ R}} = \frac{c_{p,SI}}{\frac{kJ}{kg \cdot K}} \times 0.2388459$ | $\frac{c_{p,SI}}{\frac{kJ}{kg \cdot K}} = \frac{c_{p,IP}}{\frac{Btu}{lb \cdot ^\circ R}} \times 4.1868$ | kJ/(kg·K)         | Btu/(lb·°R)          |
| Specific isochoric heat capacity $c_v$   | $\frac{c_{v,IP}}{\frac{Btu}{lb \cdot ^\circ R}} = \frac{c_{v,SI}}{\frac{kJ}{kg \cdot K}} \times 0.2388459$ | $\frac{c_{v,SI}}{\frac{kJ}{kg \cdot K}} = \frac{c_{v,IP}}{\frac{Btu}{lb \cdot ^\circ R}} \times 4.1868$ | kJ/(kg·K)         | Btu/(lb·°R)          |
| Dynamic viscosity $\eta$                 | $\frac{\eta_{IP}}{\frac{lb \cdot s}{ft^2}} = \frac{\eta_{SI}}{\frac{Pa \cdot s}{s}} \times 0.02088543$     | $\frac{\eta_{SI}}{\frac{Pa \cdot s}{s}} = \frac{\eta_{IP}}{\frac{lb \cdot s}{ft^2}} \times 47.880259$   | Pa·s              | lb·s/ft <sup>2</sup> |
| Enhancement factor $f$                   | $f_{IP} = f_{SI}$                                                                                          | $f_{SI} = f_{IP}$                                                                                       | -                 | -                    |

| Property                                             | Conversion: SI Units → I-P Units                                                                                                                            | Conversion: I-P Units → SI Units                                                                                                                                        | Units SI                | Units I-P                 |
|------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------|---------------------------|
| Air-specific enthalpy<br>(moist air) $h$             | $\frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}_a}} = \frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}_a}} \times 0.4299226 + 7.68565365666$                             | $\frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}_a}} = \left( \frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}_a}} - 7.68565365666 \right) \times 2.326$                              | kJ/kg <sub>a</sub>      | Btu/lb <sub>a</sub>       |
| Specific enthalpy<br>(water, water vapor, ice) $h_w$ | $\frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}}} = \frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}}} \times 0.4299226$                                                 | $\frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}}} = \frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}}} \times 2.326$                                                                 | kJ/kg                   | Btu/lb                    |
| Isentropic exponent $\kappa$                         | $\kappa_{IP} = \kappa_{SI}$                                                                                                                                 | $\kappa_{SI} = \kappa_{IP}$                                                                                                                                             | -                       | -                         |
| Thermal conductivity $\lambda$                       | $\frac{\lambda_{IP}}{\frac{\text{Btu}}{\text{h ft } ^\circ\text{R}}} = \frac{\lambda_{SI}}{\frac{\text{W}}{\text{m K}}} \times 0.57778932$                  | $\frac{\lambda_{SI}}{\frac{\text{W}}{\text{m K}}} = \frac{\lambda_{IP}}{\frac{\text{Btu}}{\text{h ft } ^\circ\text{R}}} \times 1.73073467$                              | W/(m·K)                 | Btu/(h·ft·°R)             |
| Kinematic viscosity $\nu$                            | $\frac{\nu_{IP}}{\frac{\text{ft}^2}{\text{s}}} = \frac{\nu_{SI}}{\frac{\text{m}^2}{\text{s}}} \times 10.763910417$                                          | $\frac{\nu_{SI}}{\frac{\text{m}^2}{\text{s}}} = \frac{\nu_{IP}}{\frac{\text{ft}^2}{\text{s}}} \times 0.092903040$                                                       | m <sup>2</sup> /s       | ft <sup>2</sup> /s        |
| Pressure $p$                                         | $\frac{p_{IP}}{\text{psi}} = \frac{p_{SI}}{\text{kPa}} \times 0.14503774$                                                                                   | $\frac{p_{SI}}{\text{kPa}} = \frac{p_{IP}}{\text{psi}} \times 6.894757$                                                                                                 | kPa                     | psi                       |
| Relative humidity $\phi$                             | $\phi_{IP} = \phi_{SI}$                                                                                                                                     | $\phi_{SI} = \phi_{IP}$                                                                                                                                                 | -                       | -                         |
| Prandtl number $Pr$                                  | $Pr_{IP} = Pr_{SI}$                                                                                                                                         | $Pr_{SI} = Pr_{IP}$                                                                                                                                                     | -                       | -                         |
| Mole fraction $\psi$                                 | $\psi_{IP} = \psi_{SI}$                                                                                                                                     | $\psi_{SI} = \psi_{IP}$                                                                                                                                                 | mol/mol                 | mol/mol                   |
| Density $\rho$                                       | $\frac{\rho_{IP}}{\frac{\text{lb}}{\text{ft}^3}} = \frac{\rho_{SI}}{\frac{\text{kg}}{\text{m}^3}} \times 0.062428$                                          | $\frac{\rho_{SI}}{\frac{\text{kg}}{\text{m}^3}} = \frac{\rho_{IP}}{\frac{\text{lb}}{\text{ft}^3}} \times 16.018463$                                                     | kg/m <sup>3</sup>       | lb/ft <sup>3</sup>        |
| Air-specific entropy<br>(moist air) $s$              | $\frac{s_{IP}}{\frac{\text{Btu}}{\text{lb}_a } ^\circ\text{R}}} = \frac{s_{SI}}{\frac{\text{kJ}}{\text{kg}_a } \text{K}}} \times 0.2388459 + 0.01616365106$ | $\frac{s_{SI}}{\frac{\text{kJ}}{\text{kg}_a } \text{K}}} = \left( \frac{s_{IP}}{\frac{\text{Btu}}{\text{lb}_a } ^\circ\text{R}}} - 0.01616365106 \right) \times 4.1868$ | kJ/(kg <sub>a</sub> ·K) | Btu/(lb <sub>a</sub> ·°R) |

| Property                                            | Conversion: SI Units → I-P Units                                                                                                                                                                                                                                     | Conversion: I-P Units → SI Units                                                                                                                                                                                                                                                 | Units SI                                 | Units I-P                                       |
|-----------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------|-------------------------------------------------|
| Specific entropy<br>(water, water vapor, ice) $s_w$ | $\frac{s_{IP}}{\frac{\text{Btu}}{\text{lb}_a \cdot ^\circ\text{R}}} = \frac{s_{SI}}{\frac{\text{kJ}}{\text{kg}_a \cdot \text{K}}} \times 0.23884589$                                                                                                                 | $\frac{s_{SI}}{\frac{\text{kJ}}{\text{kg}_a \cdot \text{K}}} = \frac{s_{IP}}{\frac{\text{Btu}}{\text{lb}_a \cdot ^\circ\text{R}}} \times 4.1868$                                                                                                                                 | $\text{kJ}/(\text{kg}_a \cdot \text{K})$ | $\text{Btu}/(\text{lb}_a \cdot ^\circ\text{R})$ |
| Temperature $t$                                     | $\frac{t_{IP}}{^\circ\text{F}} = \frac{t_{SI}}{^\circ\text{C}} \times \frac{9}{5} + 32$                                                                                                                                                                              | $\frac{t_{SI}}{^\circ\text{C}} = \left( \frac{t_{IP}}{^\circ\text{F}} - 32 \right) \times \frac{5}{9}$                                                                                                                                                                           | $^\circ\text{C}$                         | $^\circ\text{F}$                                |
| Air-specific internal energy<br>(moist air) $u$     | $(u = h - pv)$ $\frac{u_{IP}}{\frac{\text{Btu}}{\text{lb}_a}} = \frac{h_{SI}}{\frac{\text{kJ}}{\text{kg}_a}} \times 0.4299226 + 7.68565365666$ $- \frac{p_{SI}}{\text{kPa}} \times 0.145037738 \cdot \frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}_a}} \times 16.018453$ | $(u = h - pv)$ $\frac{u_{SI}}{\frac{\text{kJ}}{\text{kg}_a}} = \left( \frac{h_{IP}}{\frac{\text{Btu}}{\text{lb}_a}} - 7.68565365666 \right) \times 2.236$ $- \frac{p_{IP}}{\text{psi}} \times 6.894757293 \cdot \frac{v_{SIP}}{\frac{\text{ft}^3}{\text{lb}_a}} \times 0.062428$ | $\text{kJ}/\text{kg}_a$                  | $\text{Btu}/\text{lb}$                          |
| Air-specific volume<br>(moist air) $v$              | $\frac{v_{IP}}{\frac{\text{ft}^3}{\text{lb}_a}} = \frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}_a}} \times 16.018453$                                                                                                                                                    | $\frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}_a}} = \frac{v_{IP}}{\frac{\text{ft}^3}{\text{lb}_a}} \times 0.062428$                                                                                                                                                                 | $\text{m}^3/\text{kg}_a$                 | $\text{ft}^3/\text{lb}_a$                       |
| Specific volume<br>(water, water vapor, ice) $v_w$  | $\frac{v_{IP}}{\frac{\text{ft}^3}{\text{lb}}} = \frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}}} \times 16.018453$                                                                                                                                                        | $\frac{v_{SI}}{\frac{\text{m}^3}{\text{kg}}} = \frac{v_{IP}}{\frac{\text{ft}^3}{\text{lb}}} \times 0.062428$                                                                                                                                                                     | $\text{m}^3/\text{kg}$                   | $\text{ft}^3/\text{lb}$                         |
| Humidity ratio $W$                                  | $W_{IP} = W_{SI}$                                                                                                                                                                                                                                                    | $W_{SI} = W_{IP}$                                                                                                                                                                                                                                                                | $\text{kg}_w/\text{kg}_a$                | $\text{lb}_w/\text{lb}_a$                       |
| Mass fraction $\zeta$                               | $\zeta_{IP} = \zeta_{SI}$                                                                                                                                                                                                                                            | $\zeta_{SI} = \zeta_{IP}$                                                                                                                                                                                                                                                        | $\text{kg}_w/\text{kg}$                  | $\text{lb}_w/\text{lb}$                         |
| Compression factor $Z$                              | $Z_{IP} = Z_{SI}$                                                                                                                                                                                                                                                    | $Z_{SI} = Z_{IP}$                                                                                                                                                                                                                                                                | -                                        | -                                               |

## 1.3 Calculation Algorithms

### 1.3.1 Algorithms for Real Moist Air

The properties of moist air are calculated from the modified Hyland-Wexler model given in Herrmann, Kretschmar, and Gatley (HKG) [1], [2]. The modifications incorporate:

- the value for the universal molar gas constant from the CODATA standard by Mohr and Taylor [22]
- the value for the molar mass of dry air from Gatley et al. [17] and that of water from IAPWS-95 [5], [6]
- the calculation of the ideal-gas parts of the heat capacity, enthalpy, and entropy for dry air from the fundamental equation of Lemmon et al. [14]
- the calculation of the ideal-gas parts of the heat capacity, enthalpy, and entropy for water vapor from IAPWS-IF97 [7], [8], [9] for  $t \geq 0^\circ\text{C}$  and from IAPWS-95 [5], [6] for  $t \leq 0^\circ\text{C}$
- the calculation of the vapor-pressure enhancement factor from the equation given by the models of Hyland and Wexler [21]
- the calculation of the second and third molar virial coefficients  $B_{aa}$  and  $C_{aaa}$  for dry air from the fundamental equation of Lemmon et al. [14]
- the calculation of the second and third molar virial coefficients  $B_{ww}$  and  $C_{www}$  for water and steam from IAPWS-95 [5], [6]
- the calculation of the air-water second molar cross-virial coefficient  $B_{aw}$  from Harvey and Huang [15]
- the calculation of the air-water third molar cross-virial coefficients  $C_{aaw}$  and  $C_{aww}$  from Nelson and Sauer [12], [13]
- the calculation of the saturation pressure of water from IAPWS-IF97 [7], [8], [9] for  $t \geq 0^\circ\text{C}$  and of the sublimation pressure of water from IAPWS-08 [11] for  $t \leq 0^\circ\text{C}$
- the calculation of the isothermal compressibility of saturated liquid water from IAPWS-IF97 [7], [8], [9] for  $t \geq 0^\circ\text{C}$  and that of ice from IAPWS-06 [10] for  $t \leq 0^\circ\text{C}$  in the determination of the vapor-pressure enhancement factor
- the calculation of Henry's constant from the IAPWS Guideline 2004 [16] in the determination of the enhancement factor. The mole fractions for the three main components of dry air were taken from Lemmon et al. [14]. Argon was not considered in the calculation of Henry's constant in the former research projects, but it is now the third component of dry air.

### 1.3.2 Algorithms for Steam and Water for Temperatures $t \geq 0^\circ\text{C}$

The  $p$ - $T$  diagram in Fig. 1 shows the formulations used for water and water vapor. The temperature range above  $0^\circ\text{C}$  is covered by IAPWS-IF97 [7], [8], [9]:

- The saturation line is calculated from the IAPWS-IF97 saturation pressure equation  $p_s^{97}(t)$  and saturation temperature equation  $t_s^{97}(p)$ .
- The properties in the liquid region including saturated-liquid line are calculated from the fundamental equation of the IAPWS-IF97 region 1.
- The properties in the vapor region including saturated-vapor line are calculated from the fundamental equation of the IAPWS-IF97 region 2.

### 1.3.3 Algorithms for Steam and Ice for Temperatures $t \leq 0^\circ\text{C}$

- The sublimation curve is covered by the IAPWS-08 sublimation pressure equation  $p_{\text{subl}}^{08}(t)$  [11] (see Fig. 1).
- The properties of ice including saturated ice are determined by the fundamental equation of the IAPWS-06 [10].
- The properties of vapor including saturated vapor are calculated from the fundamental equation of IAPWS-95 [5], [6].

### 1.3.4 Overview of the Applied Formulations for Steam, Water, and Ice

The following  $p$ - $T$  diagram shows the used IAPWS Formulations and the ranges where they are applied.

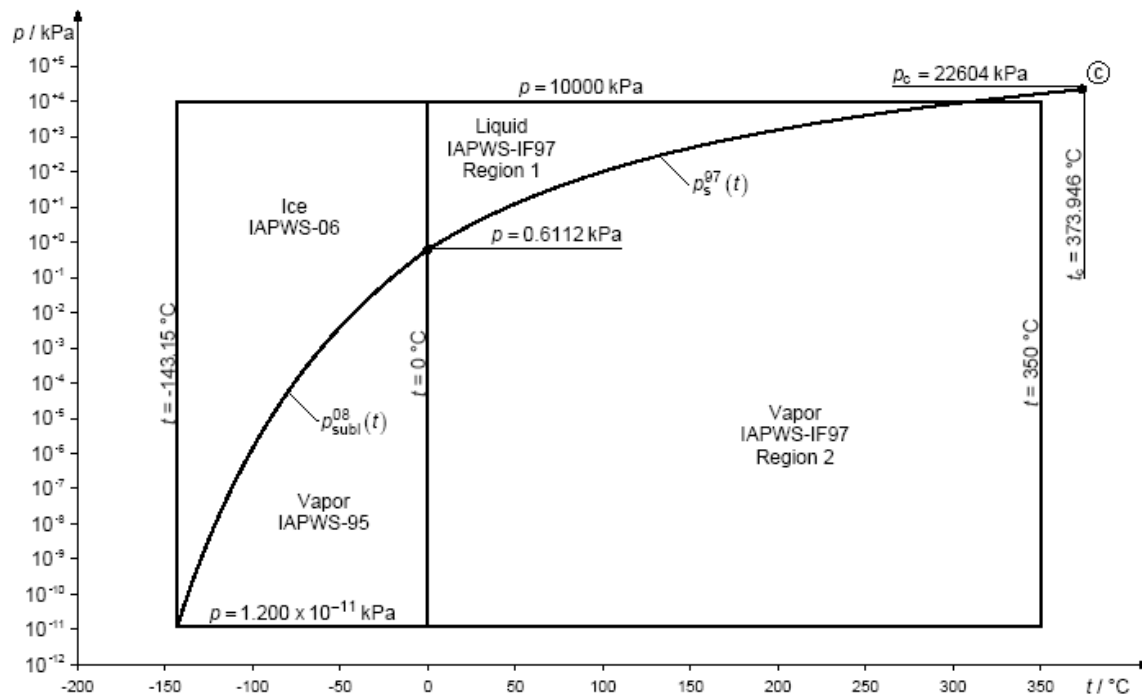


Figure 1:  $p$ - $T$  diagram with used IAPWS formulations for steam, water, and ice.



## 2 Add-In FluidDYM for DYMOLA<sup>®</sup> for ASHRAE-LibHuAirProp-SI

### 2.1 Installing FluidDYM

The FluidDYM Add-In has been developed to calculate thermodynamic properties in Dymola<sup>®</sup> more conveniently. Within Dymola it enables the direct call of functions relating to moist air from the ASHRAE-LibHuAirProp-SI property library. The 32-bit version of FluidDYM LibHuAirProp runs on both the 32-bit and 64-bit version of DYMOLA<sup>®</sup>.

#### 2.1.1 Installing FluidDYM including LibHuAirProp

The installation of FluidDYM and ASHRAE-LibHuAirProp\_SI is described in section 2.1.1 in "Part IP Units" of this User's Guide.

#### 2.1.2 The FluidDYM Help System

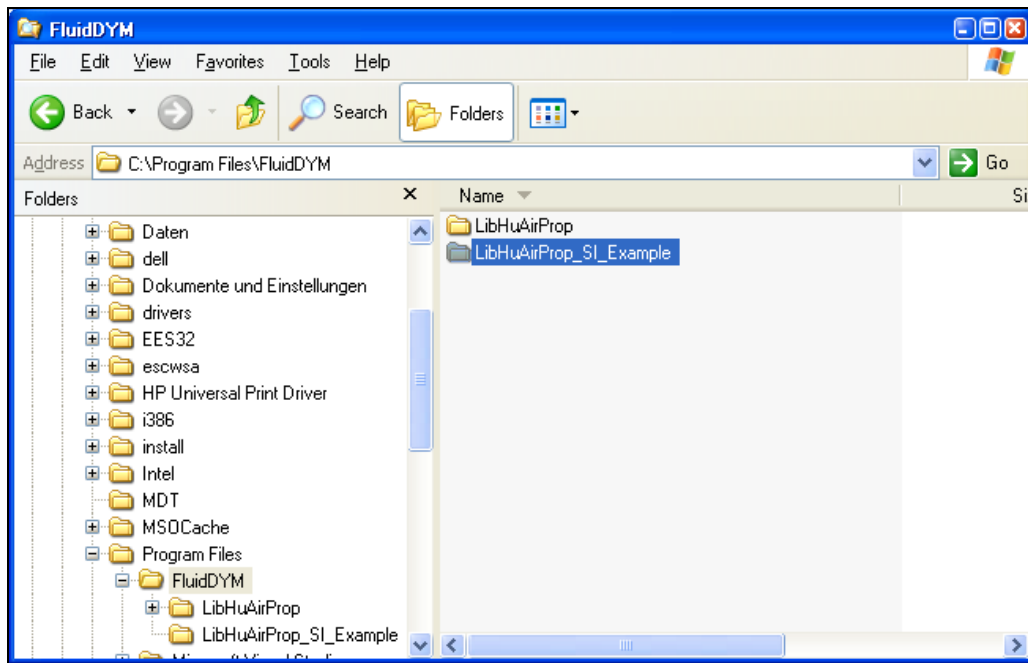
Dymola<sup>®</sup> provides detailed help functions which are described in in section 2.1.2 in "Part I-P Units" of this User's Guide.

### 2.2 Example: Calculation of $h = f(p, t, W)$

Now we will calculate, step by step, the specific enthalpy  $h$  of moist air as a function of pressure  $p$ , temperature  $t$  and humidity ratio  $W$ , using Dymola<sup>®</sup>.

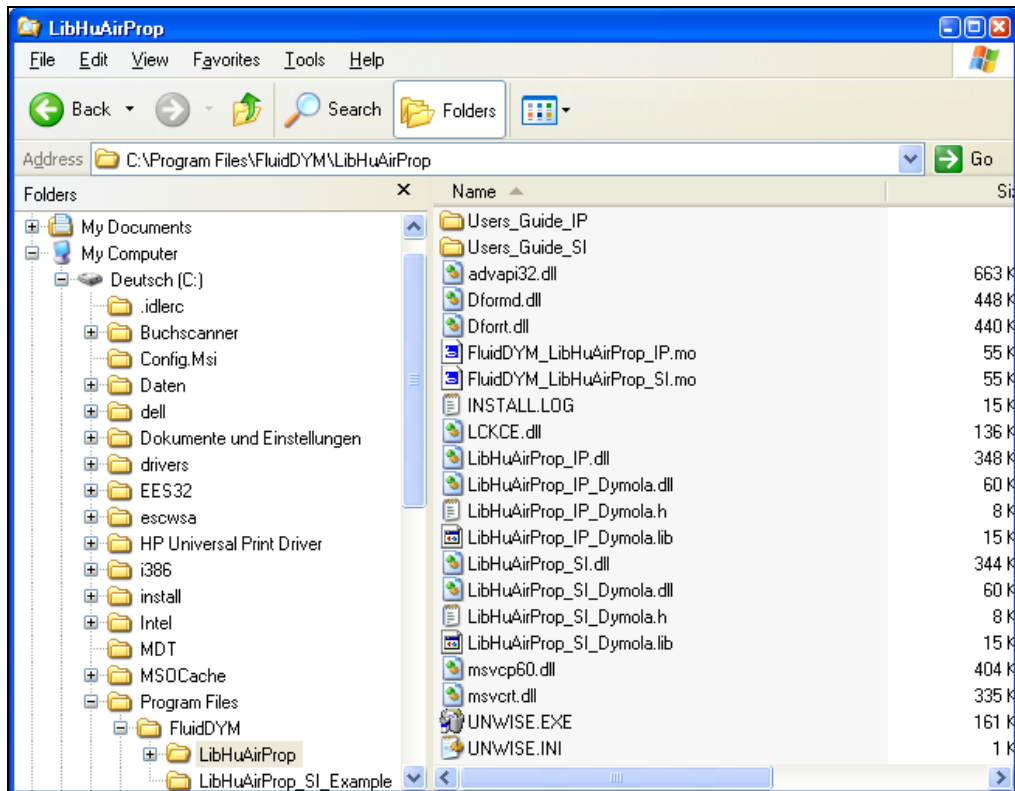
Please carry out the following instructions:

- Start Windows Explorer<sup>®</sup>, Total Commander<sup>®</sup>, My Computer or another file manager program. The description here refers to Windows Explorer
- Your Windows Explorer should be set to Details for a better view. Click the "View" (Ansicht) button and select "Details".
- Switch into the program directory of FluidDYM in which you will find the folder "\LibHuAirProp\_SI"; the standard location is:  
"C:\Program Files\FluidDYM\LibHuAirProp\_SI"
- Create the folder "\LibHuAirProp\_SI\_Example" by clicking on "File" in the Explorer menu, then "New" in the menu which appears, and then selecting "Folder". Name the new folder "\LibHuAirProp\_SI\_Example".
- You will see the following window:



**Figure 2.2.1:** Highlighted *LibHuAirProp\_SI\_Example* directory in Program Files

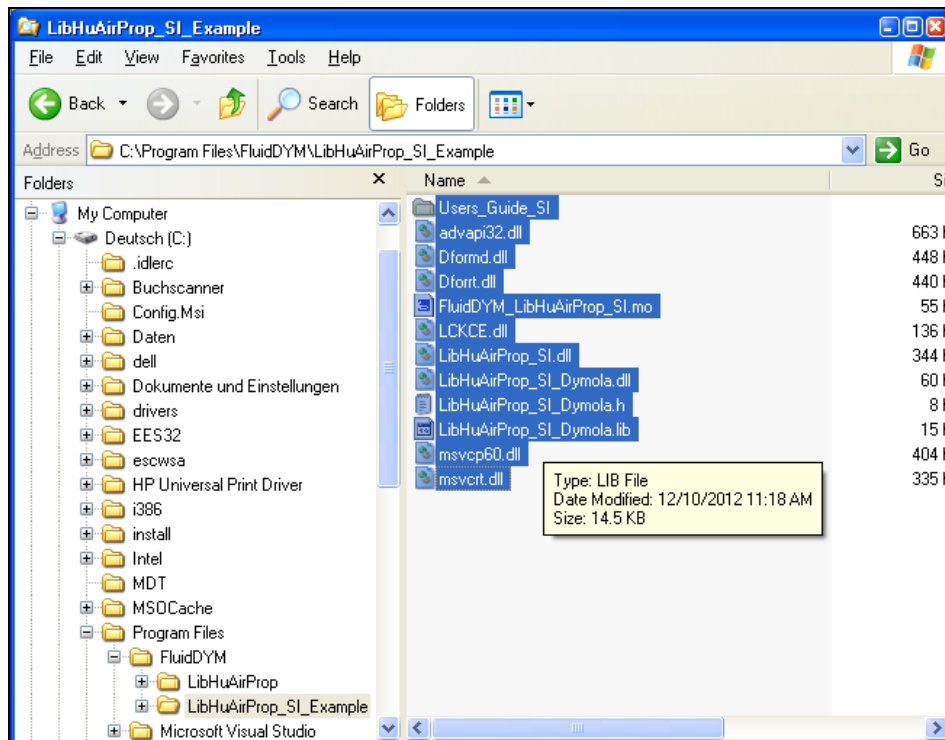
- Switch into the directory "\LibHuAirProp" within "FluidDYM", the standard being: "C:\Program Files\FuildDYM\LibHuAirProp".
- You will see the following window:



**Figure 2.2.2:** *LibHuAirProp\_SI* directory including installed files

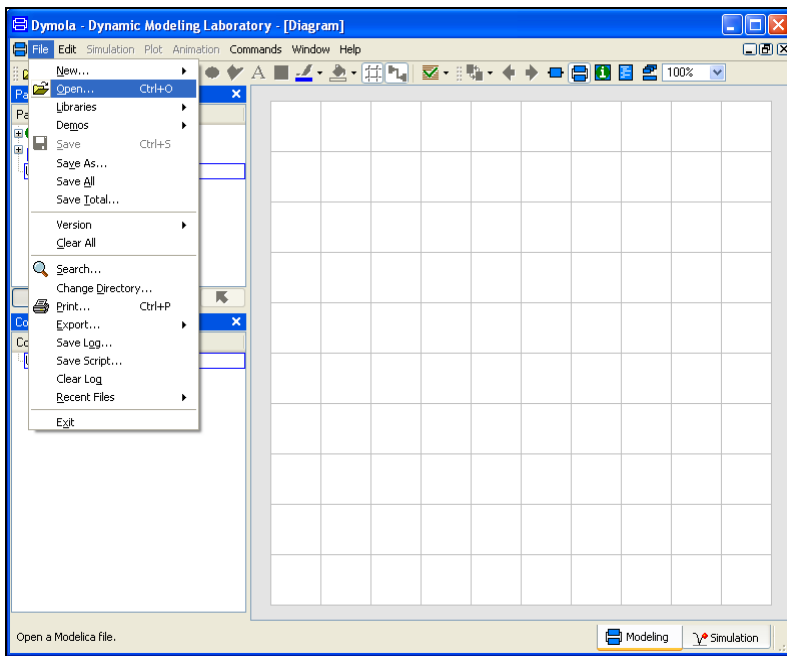
In order to calculate the function  $h = f(p, t, W)$ , the following files are necessary. Copy these into the directory "C:\Program Files\FluidDYM\LibHuAirProp\_SI\_Example":

- "advapi32.dll"
  - "Dforrt.dll"
  - "Dformd.dll"
  - "FluidDYM\_HuAirProp\_SI.mo"
  - "LCKCE.dll"
  - "LibHuAirProp\_SI.dll"
  - "LibHuAirProp\_SI\_Dymola.dll"
  - "LibHuAirProp\_SI\_Dymola.h"
  - "LibHuAirProp\_SI\_Dymola.lib"
  - "msvc60.dll"
  - "msvcrt.dll"
  - the folder "Users\_Guide"
- Mark up these files, then click "Edit" in the upper menu bar and select "Copy".
  - Switch into the directory "C:\Program Files\FluidDYM\LibHuAirProp\_SI\_Example", click "Edit" and then "Paste".
  - You will see the following window:



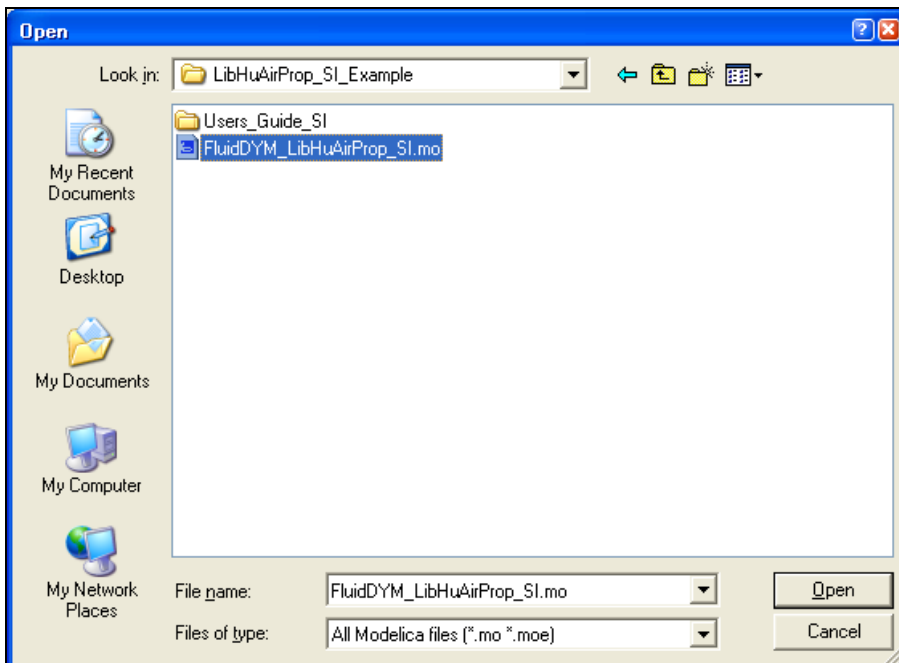
**Figure 2.2.3:** *LibHuAirProp\_SI\_Example* directory including the newly-copied files

- Start Dymola®.
- Now click on "File" in the Dymola menu bar and select "Open" (see Figure 2.2.4).



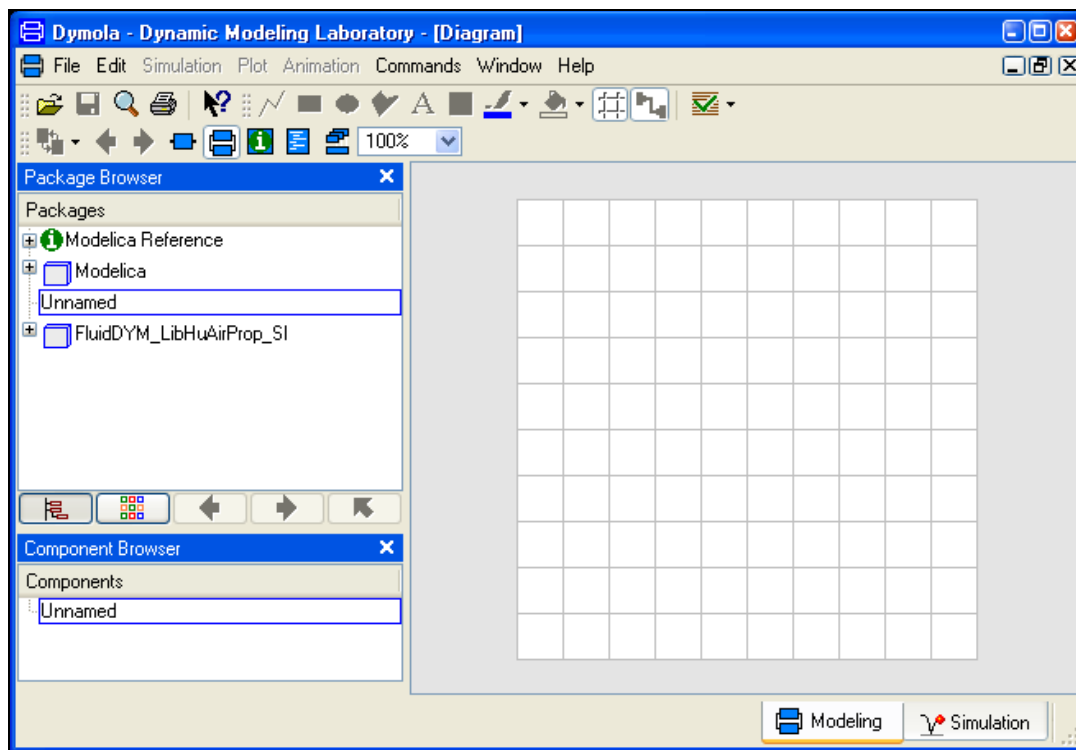
**Figure 2.2.4:** Selecting the menu entry "Open"

- Search and click on the directory "C:\Program Files\FluidDYM\LibHuAirProp\_SI\_Example" in the menu that appears.
- Select the "FluidDYM\_LibHuAirProp\_SI.mo" file and click on the "Open" button (see Figure 2.2.5)



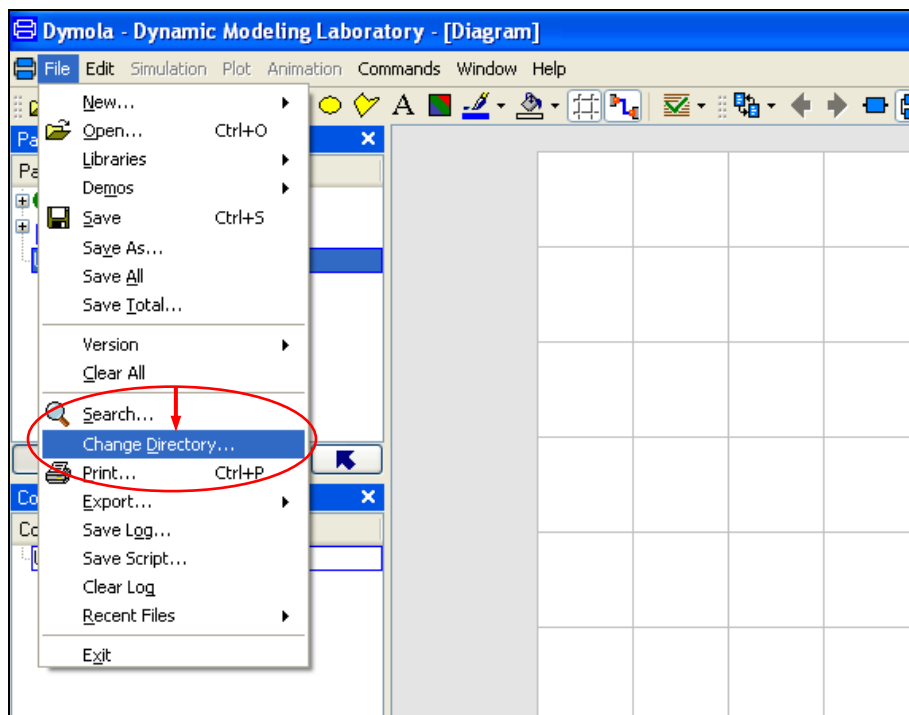
**Figure 2.2.5:** Selecting the *FluidDYM\_LibHuAirProp\_SI.mo* file

- The library will be loaded by Dymola which may take a few seconds.
- After Dymola has finished loading the LibHuAirProp\_SI library, you will see the window shown in Figure 2.2.6.



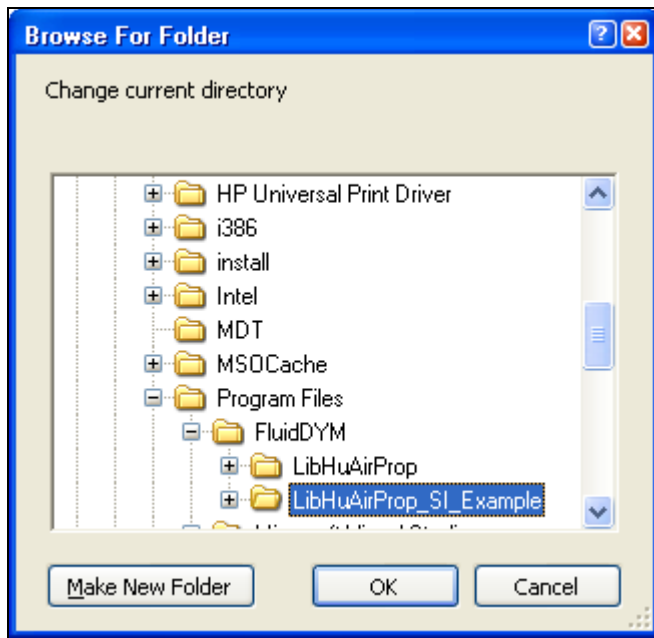
**Figure 2.2.6:** Dymola window after loading the *LibHuAirProp\_SI* library

- Now, click on "File" in the Dymola menu bar and select "Change Directory..." in order to open the folder "\LibHuAirProp\_SI\_Example" (see Figure 2.2.7).



**Figure 2.2.7:** Selecting the menu entry "Change Directory..."

- Search and click on the directory "C:\Program Files\FluidDYM\LibHuAirProp\_SI\_Example" in the menu that appears (see figure below).

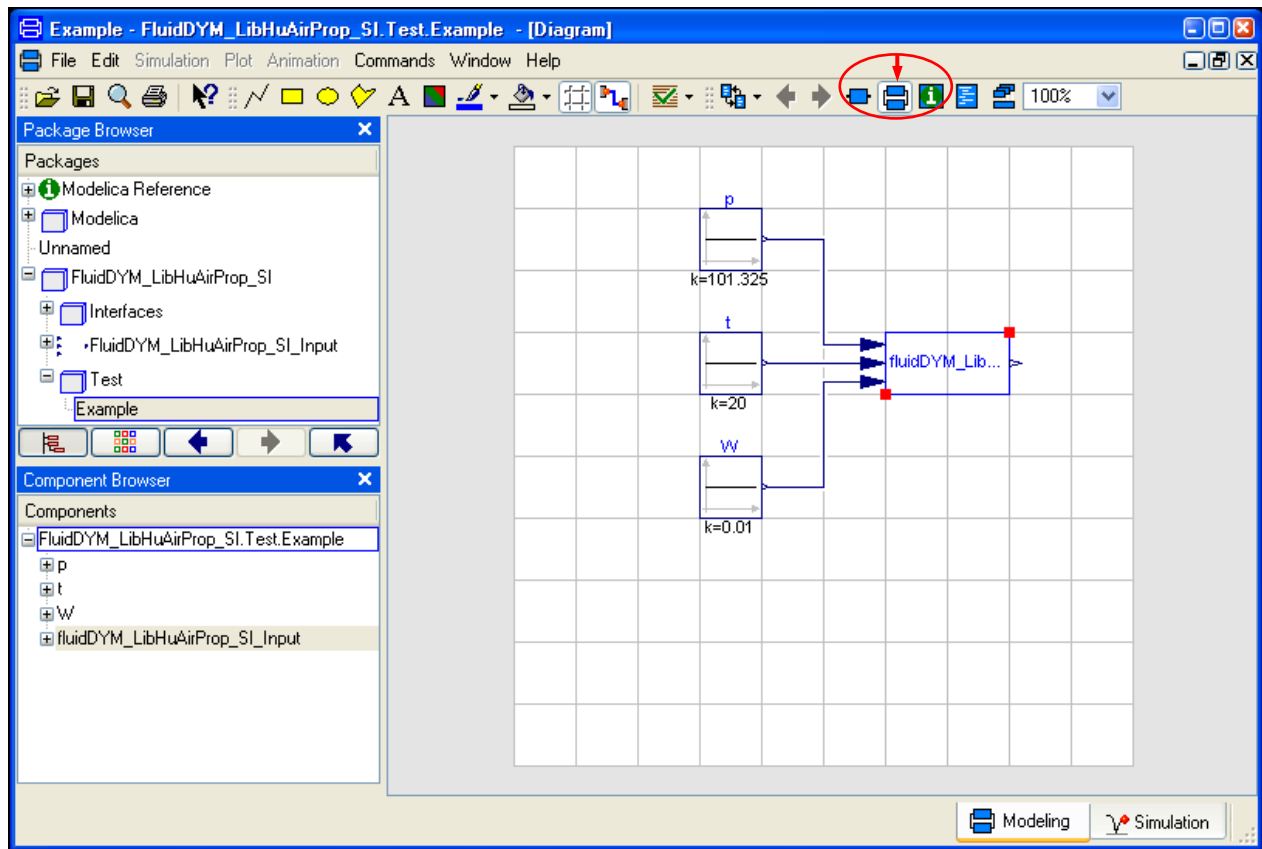


**Figure 2.2.8:** Selecting the *LibHuAirProp\_SI\_Example* directory

- Confirm your selection by clicking the "OK" button.

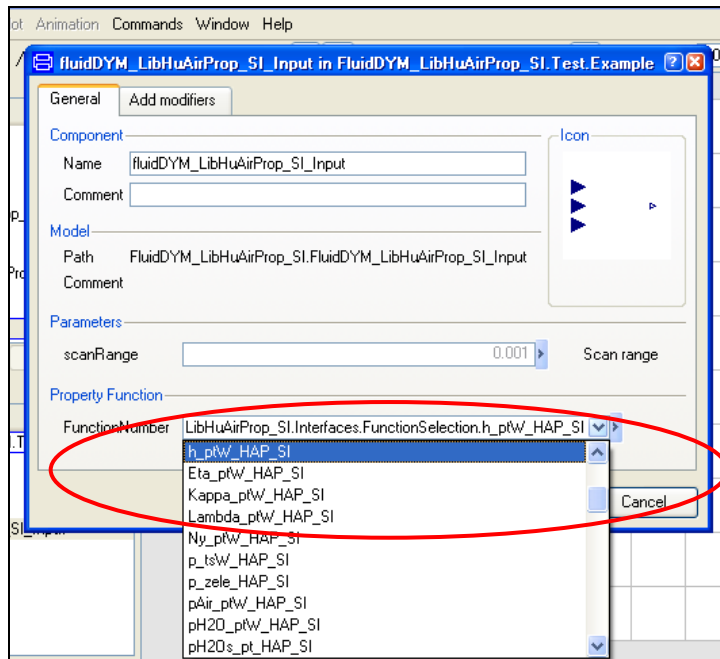
As indicated in the table of property functions in Chapter 1, you have to call up the function "h\_ptW\_HAP\_SI" as follows for calculating  $h = f(p, t, W)$ .

- Click on the Dymola-Block "Test," which can be found in the FluidDYM\_HuAirProp\_SI package in the "Package Browser" on the left hand side of the Dymola window. Here choose Example by double-clicking on it.
- Now click on the  button in the Dymola menu bar in order to switch to the Diagram Mode. You will see the following window:



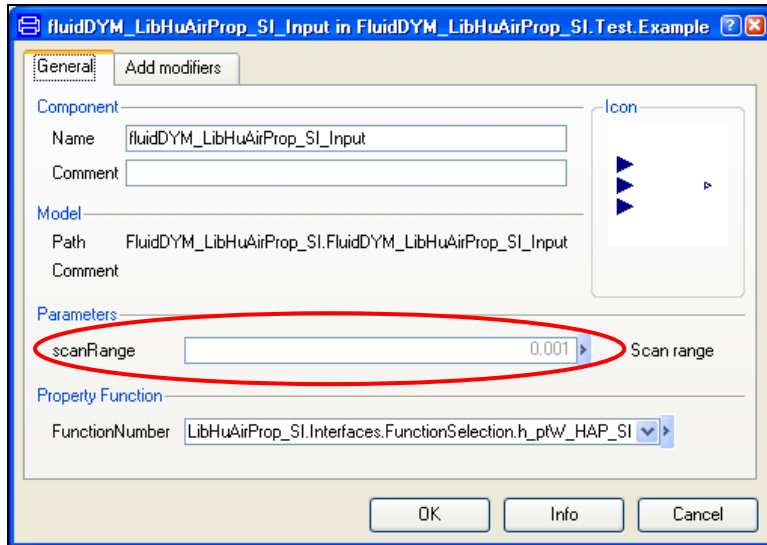
**Figure 2.2.9:** Dymola in Diagram Mode

- Now double-click on the "FluidDYM\_LibHuAirProp\_SI\_Input" block on the right hand side of the Dymola window.
- Search and click the " $h_{ptW\_HAP\_SI}$ " function next to "Function Number" in the menu that appears (see figure below).



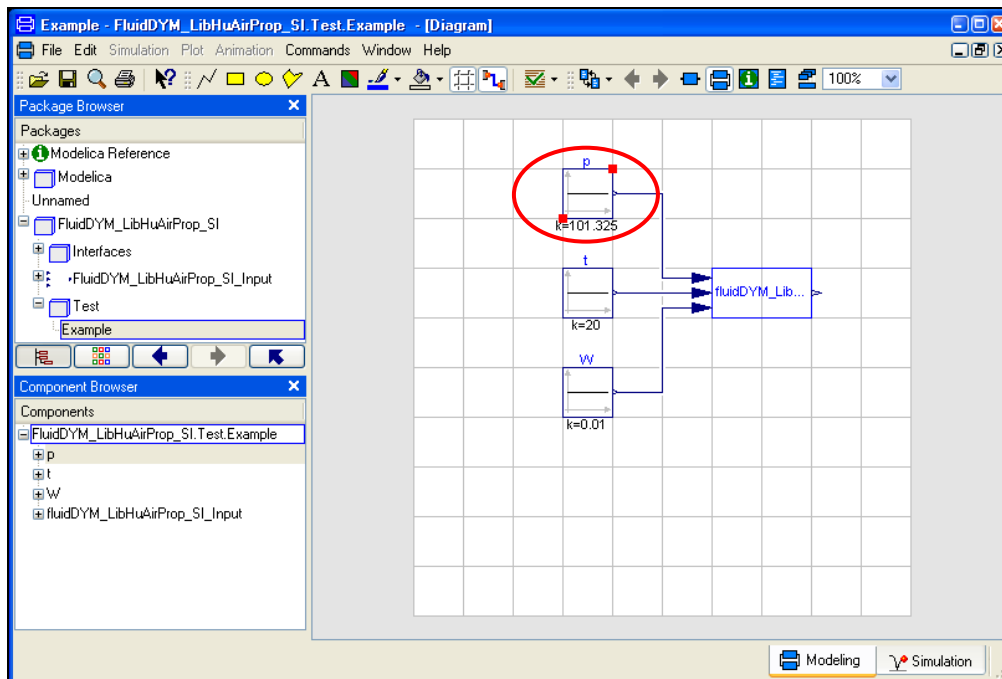
**Figure 2.2.10:** Choosing the function  $h_{ptW\_HAP\_SI}$

- You can set the scan range (how many times the property will be calculated per second) next to "scanRange". The preset value 0.001 means that the property will be calculated 1000 times per second. If you enter the value 1, for example, the property will be calculated once per second. Do not change the preset value of 0.001 for our example calculation.



**Figure 2.2.11:** Setting the scan range

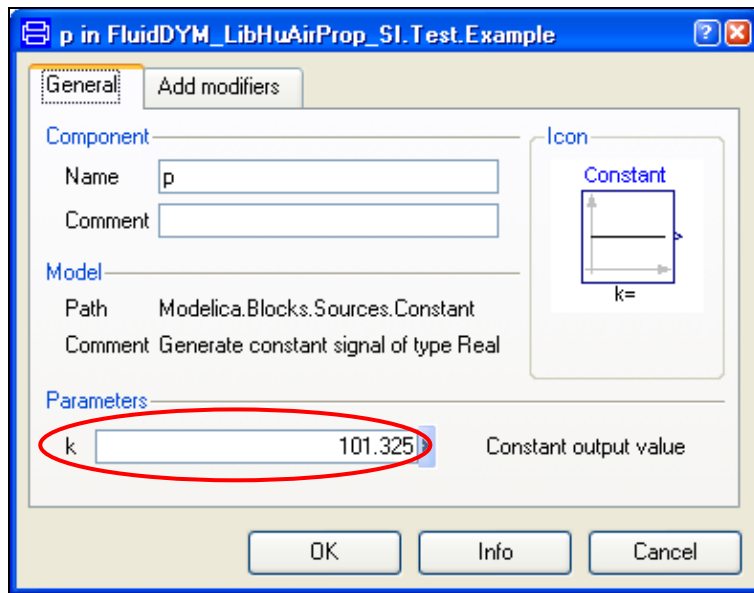
- Now we will configure the input parameters  $p$ ,  $t$ , and  $W$ . When calculating a function with only two input parameters, the third input parameter will not be defined.
- First, double click on the "p" block which represents the first input parameter, here the pressure  $p$  in kPa (see Figure 2.2.12).



**Figure 2.2.12:** "Parameter p" block in Dymola

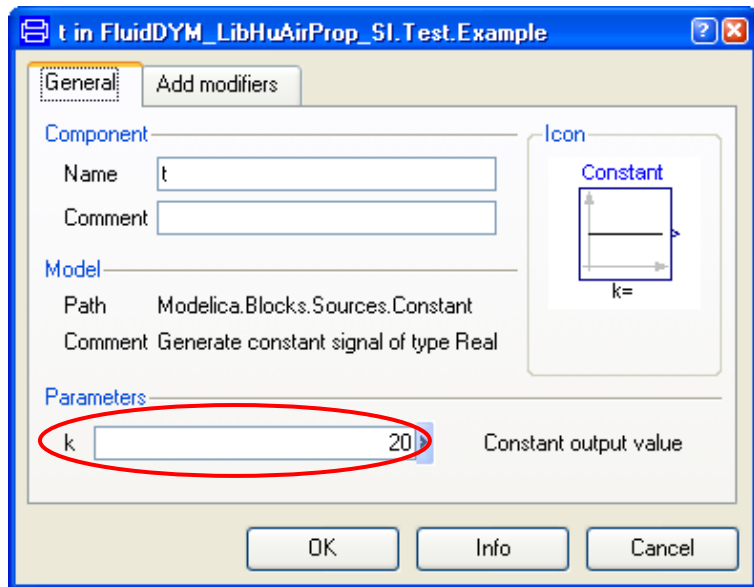
- Enter the value 101.325 on the line next to "k" in the dialog window which appears and then click the "OK" button (see Figure 2.2.13).





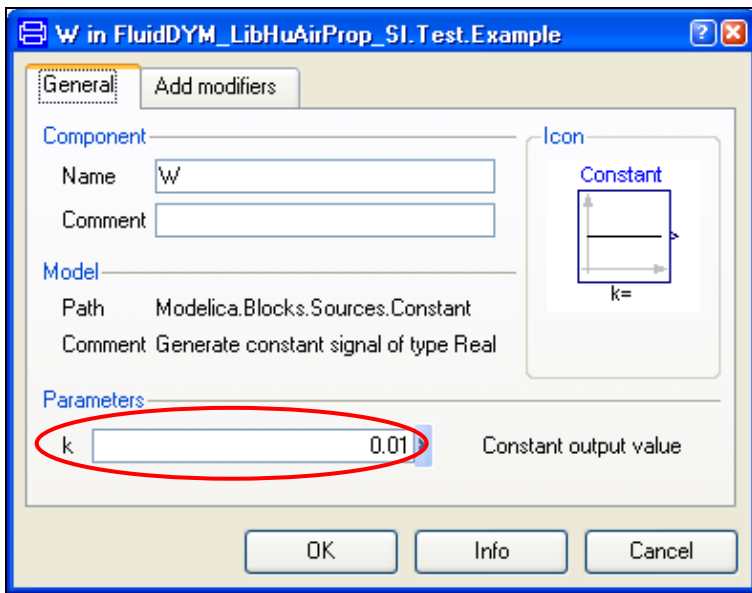
**Figure 2.2.13:** Entering the value for the pressure  $p$

- Now, double click on the "t" block which represents the second input parameter, here the temperature  $t$  in °C.
- Enter the value 20 on the line next to "k" in the dialog window which appears and then click the "OK" button (see Figure 2.2.14).



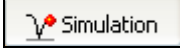
**Figure 2.2.14:** Entering the value for the temperature  $t$

- Now, double click on the "W" block which represents the third input parameter, here the humidity ratio  $W$  in  $\text{kg}_w/\text{kg}_a$ .
- Enter the value 0.01 on the line next to "k" in the dialog window which appears and then click the "OK" button (see Figure 2.2.15).

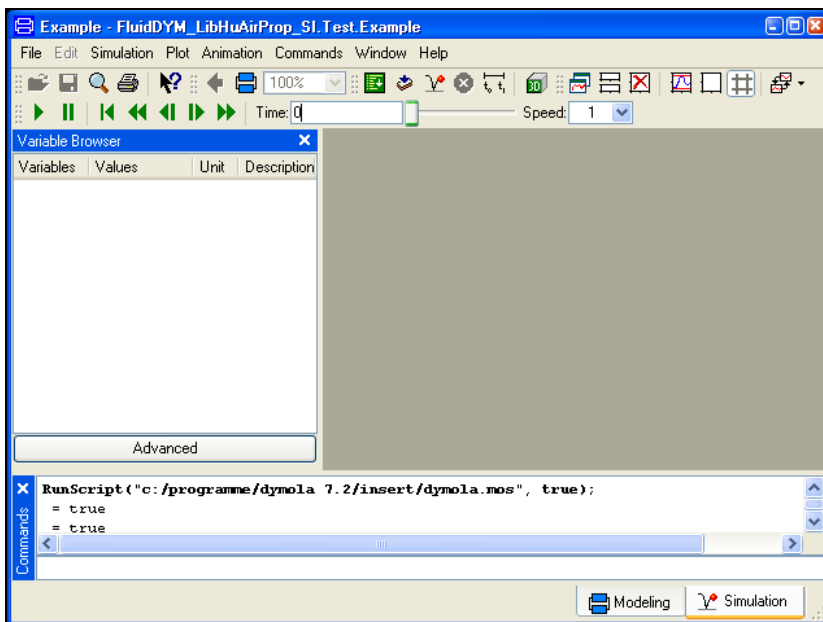


**Figure 2.2.15:** Entering the value for the humidity ratio  $W$

All parameters have now been defined.

- Click on the  button in the lower right area of Dymola in order to switch into the "Simulation Mode".

In Figure 2.2.16 you can see what the Dymola "Simulation Mode" looks like.

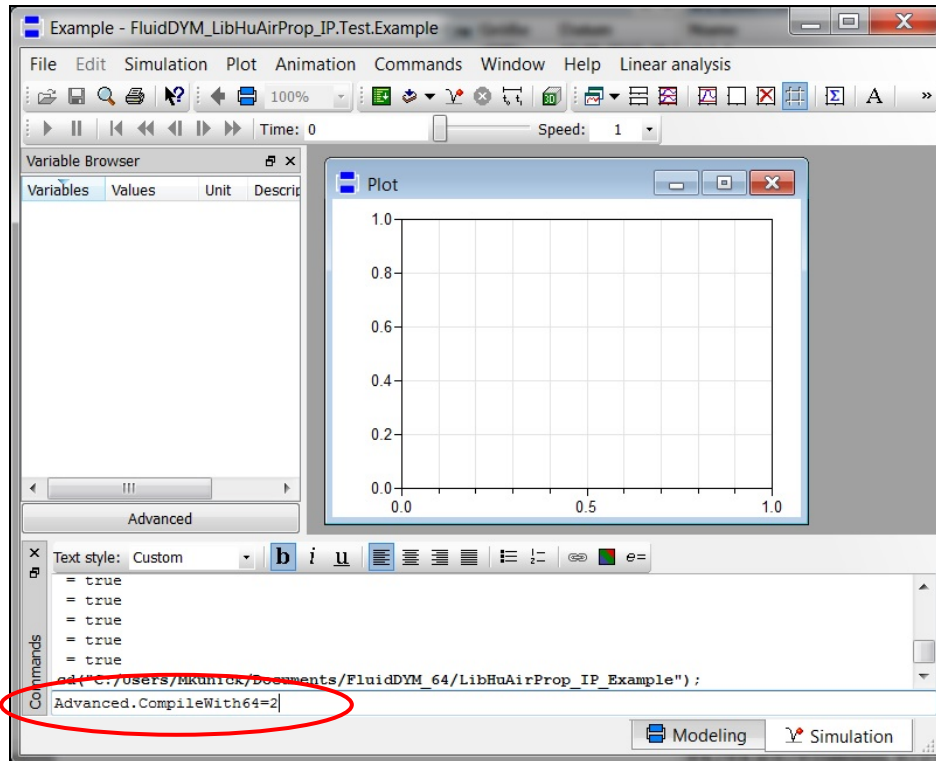


**Figure 2.2.16:** "Simulation Mode" window

**IMPORTANT NOTICE:**

Per default the 64-bit version of Dymola creates a 32-bit simulation process. If you want to create a 64-bit simulation process you must have installed the 64-bit version of FluidDYM LibHuAirProp and you now need to enter the following command into the command line of Dymola and confirm your entry by pressing the Enter key:

**"Advanced.CompileWith64=2"**



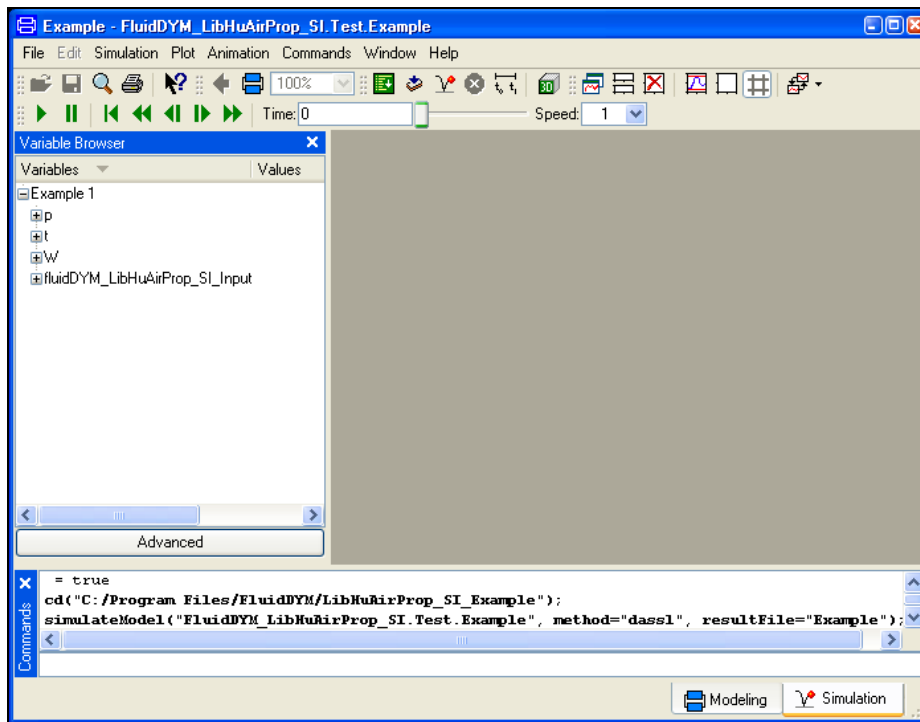
**Figure 2.2.17:** "Simulation Mode" window with 64-bit command

Now, your 64-bit Dymola creates 64-bit simulation processes with FluidDYM LibHuAirProp.

Please note that if you restart Dymola and want to create 64-bit simulation processes again, you will always have to enter this command anew.

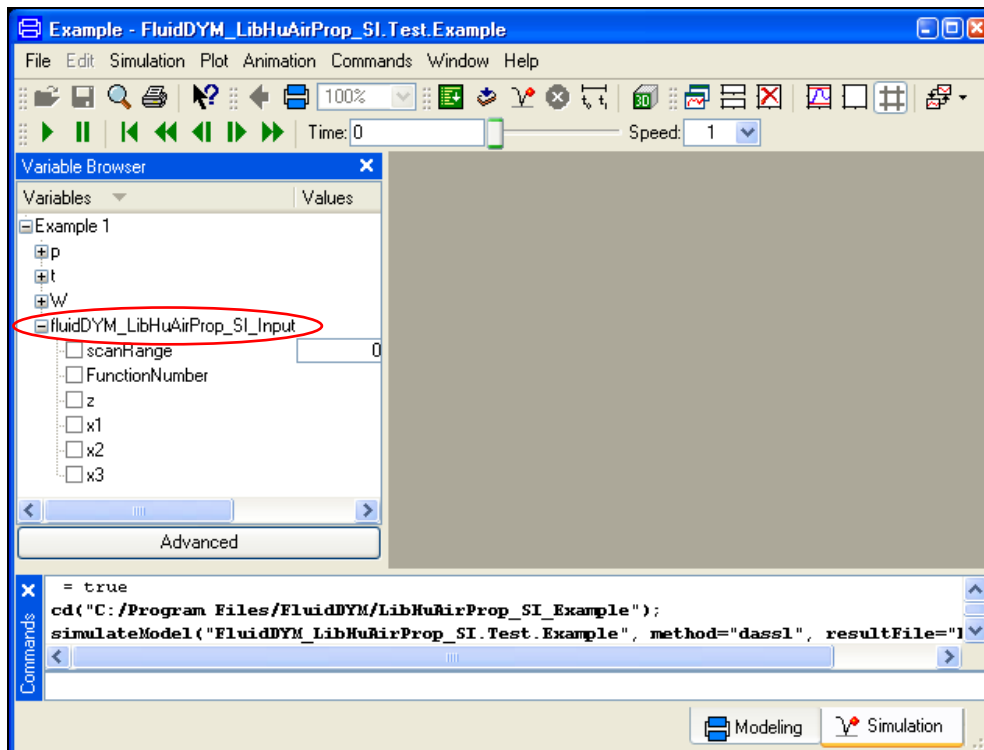
For further information concerning this matter, please see the Dymola user's guide.

- Click on the "Simulate" Button  in the Dymola menu bar to start the calculation. Now the model will be compiled and the simulation starts.
- Afterwards you will see the following entries within the "Variable Browser" window in Dymola (see Figure 2.2.18):



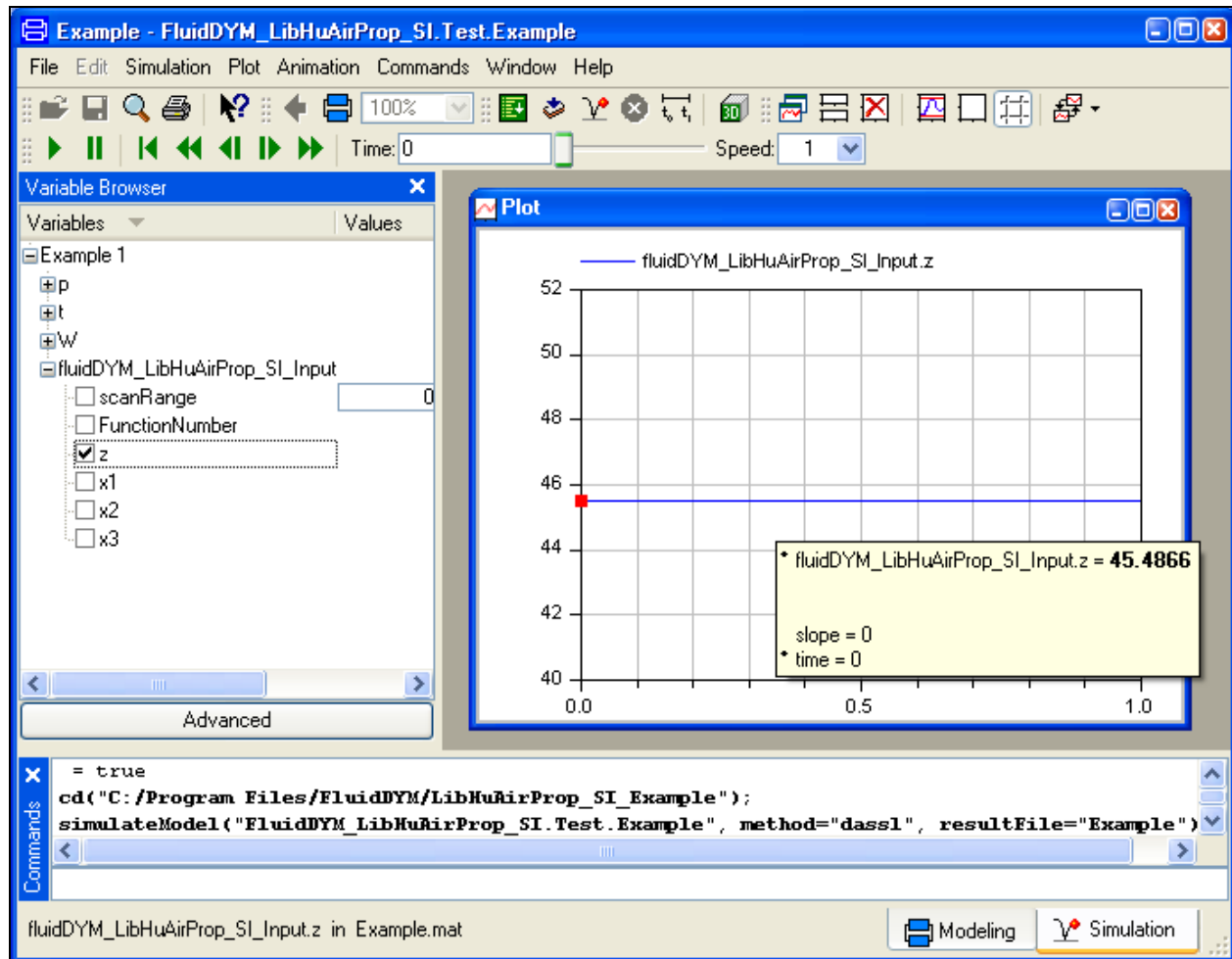
**Figure 2.2.18:** "Variable Browser" with new entries

- By clicking on the "NewPlotWindow" button , a new diagram window will be opened.
- Click on "fluidDYM\_LibHuAirProp\_SI\_Input" within the "Variable Browser"; then you will see the input and output parameters "scanRange", "FunctionNumber", "z", "x1", "x2", and "x3" (see Figure 2.2.19).



**Figure 2.2.19:** Parameters of *fluidDYM\_LibHuAirProp\_SI\_Input*

- After clicking on the output parameter "z", the calculated property will be represented graphically in the "PlotWindow".
- Move the mouse over the curve to see the result of the simulation at a specific point in time (see Figure 2.2.20).



**Figure 2.2.20:** "DiagramWindow" showing the result

The result for  $h$  appears in the "DiagramWindow"

⇒ The result in our sample calculation here is: " $h = 45.4866$ ". The corresponding unit is kJ/kg (see table of the property functions in Chapter 1).

- Now click on the Modeling button  in the lower right area of Dymola in order to switch into the "Modeling Mode". Here you can arbitrarily change the values for  $p$ ,  $t$ , or  $W$  in the appropriate blocks.

## 2.3 Removing FluidDYM including LibHuAirProp

The de-installation of FluidDYM and ASHRAE-LibHuAirProp\_SI is described in section 2.4 in "Part I-P Units" of this User's Guide.



## **3 Property Functions of ASHRAE-LibHuAirProp-SI**

### **3.1 Functions for Real Moist Air**

**Thermal Diffusivity  $a = f(p, t, W)$** **Function Name:**

a\_ptW\_HAP\_SI

**Fortran Program:**

REAL\*8 FUNCTION A\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**a\_ptW\_HAP\_SI - Thermal diffusivity of humid air in m<sup>2</sup>/s**Range of Validity:**

Temperature  $t$ : from -73.15°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq W_s$

**Comments:**

- Thermal diffusivity  $a = \frac{\lambda}{\rho \cdot c_p}$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

a\_ptW\_HAP\_SI = -1000

**References:**

$\lambda(p, t, W)$  Herrmann et al. [3], [4]  
 $\rho(p, t, W)$  Herrmann et al. [1], [2]  
 $c_p(p, t, W)$  Herrmann et al. [1], [2]



**Relative Pressure Coefficient  $\alpha_p = f(p, t, W)$** 
**Function Name:**

alphap\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  ALPHAP_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$     -    Total pressure  $p$  in kPa  
 $t$     -    Temperature  $t$  in °C  
 $W$     -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

alphap\_ptW\_HAP\_SI - Relative pressure coefficient of humid air in 1/K

**Range of Validity:**

Temperature  $t$ :                      from -143.15°C to 350°C  
 Total pressure  $p$ :                    from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :                     $0 \leq W \leq W_s$

**Comments:**

- Relative pressure coefficient  $\alpha_p = \frac{1}{p} \left( \frac{\partial p}{\partial T} \right)_v$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

alphap\_ptW\_HAP\_SI = -1000

**References:**

$\rho(p, t, W)$     Herrmann et al. [1], [2]

**Isothermal Stress Coefficient  $\beta_p = f(p, t, W)$** 
**Function Name:**

betap\_ptW\_HAP\_SI

**Fortran Program:**

REAL\*8 FUNCTION BETAP\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**betap\_ptW\_HAP\_SI - Isothermal stress coefficient of humid air in kg/m<sup>3</sup>**Range of Validity:**

Temperature  $t$ : from -143.15°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq W_s$

**Comments:**

- Isothermal stress coefficient  $\beta_p = -\frac{1}{p} \left( \frac{\partial p}{\partial v} \right)_T$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

betap\_ptW\_HAP\_SI = -1000

**References:** $v(p, t, W)$  Herrmann et al. [1], [2]

**Speed of Sound  $c = f(p, t, W)$** 
**Function Name:**

c\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION C_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

c\_ptW\_HAP\_SI - Speed of sound of humid air in m/s

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Speed of sound  $c = v \sqrt{-\left(\frac{\partial p}{\partial v}\right)_s}$

- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

c\_ptW\_HAP\_SI = -1000

**References:**

$v(p, t, W)$  Herrmann et al. [1], [2]

**Specific Isobaric Heat Capacity  $c_p = f(p, t, W)$** 
**Function Name:**

cp\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION CP_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in kPa  
 $t$        -    Temperature  $t$  in °C  
 $W$       -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

cp\_ptW\_HAP\_SI - Specific isobaric heat capacity of humid air in kJ/(kg K)

**Range of Validity:**

Temperature  $t$ :                from -143.15°C to 350°C  
 Total pressure  $p$ :            from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :             $0 \leq W \leq W_s$

**Comments:**

- Specific isobaric heat capacity  $c_p = \left( \frac{\partial h}{\partial T} \right)_p$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

cp\_ptW\_HAP\_SI = -1000

**References:**

$h(p, t, W)$      Herrmann et al. [1], [2]

**Specific Isochoric Heat Capacity  $c_v = f(p, t, W)$** 
**Function Name:**

cv\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION CV_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in kPa  
 $t$        -    Temperature  $t$  in °C  
 $W$       -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

cv\_ptW\_HAP\_SI - Specific isochoric heat capacity of humid air in kJ/(kg K)

**Range of Validity:**

Temperature  $t$ :                from -143.15°C to 350°C  
 Total pressure  $p$ :            from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :             $0 \leq W \leq W_s$

**Comments:**

- Specific isochoric heat capacity  $c_v = \left( \frac{\partial u}{\partial T} \right)_v$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

cv\_ptW\_HAP\_SI = -1000

**References:**

$c_v(p, t, W)$     Herrmann et al. [3], [4]

**Enhancement Factor  $f = f(p,t)$** **Function Name:**

f\_pt\_HAP\_SI

**Fortran Program:**

REAL\*8 FUNCTION F\_PT\_HUAIRPROP(P,T), REAL\*8 P,T

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C

**Result:**

f\_pt\_HAP\_SI - Enhancement factor of water (decimal ratio)

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa

**Comments:**

- Enhancement factor  $f = \frac{\rho_{\text{H}_2\text{O},s}}{\rho_s(t)}$   
 with  $\rho_s(t)$  for  $t \geq 0.01^\circ\text{C}$  - Steam pressure of water  
 for  $t < 0.01^\circ\text{C}$  - Sublimation pressure of water
- Describes the enhancement of the saturation pressure of water in the air atmosphere under elevated pressure
- Derived iteratively from the isothermal compressibility of liquid water, from Henry's constant [15], [16] and from the virial coefficients of air, water, and the air-water mixture

**Result for Wrong Input Values:**

f\_pt\_HAP\_SI = -1000

**References:** $f(p,t)$  Herrmann et al. [1], [2]

**Air-Specific Enthalpy  $h = f(p, t, W)$** 
**Function Name:**

h\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION H_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

h\_ptW\_HAP\_SI - Air-specific enthalpy in kJ/kg<sub>a</sub>

**Range of Validity:**

Temperature  $t$ : from -143.5°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

h\_ptW\_HAP\_SI = -1000

**References:**

$h(p, t, W)$  Herrmann et al. [1], [2]  
 $h_w(p, t)$  IAPWS-IF97 [7], [8] and IAPWS-06 [11]  
 $h_a(t)$  Lemmon et al. [14]

## Dynamic Viscosity $\eta = f(p, t, W)$

### Function Name:

Eta\_ptW\_HAP\_SI

### Fortran Program:

```
REAL*8 FUNCTION ETA_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

### Input Values:

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

### Result:

Eta\_ptW\_HAP\_SI - Dynamic viscosity of humid air in Pa s

### Range of Validity:

Temperature  $t$ : from -73.15°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

### Comments:

- A new very accurate algorithm is implemented between 0°C and 350°C
- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

### Result for Wrong Input Values:

Eta\_ptW\_HAP\_SI = -1000

### References:

$\eta(p, t, W)$  Herrmann et al. [3], [4]  
 $\eta_a(t)$  Lemmon et al. [18]  
 $\eta_w(p, t)$  IAPWS-IF97 [7], [8] and IAPWS-08 [19]



## Isentropic Exponent $\kappa = f(p, t, W)$

### Function Name:

Kappa\_ptW\_HAP\_SI

### Fortran Program:

```
REAL*8 FUNCTION KAPPA_PTW_HUAIRPROP(P,T, W), REAL*8 P,T,W
```

### Input Values:

$p$     -    Total pressure  $p$  in kPa  
 $t$     -    Temperature  $t$  in °C  
 $W$     -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

### Result:

Kappa\_ptW\_HAP\_SI - Isentropic exponent

### Range of Validity:

Temperature  $t$ :                      from -143.5°C to 350°C  
 Total pressure  $p$ :                    from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :                     $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

### Comments:

- Isentropic exponent  $\kappa = -\frac{v}{p} \left( \frac{\partial p}{\partial v} \right)_s$
- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets homogeneously mixed) is applied for  $t \geq 0.01^\circ\text{C}$ . For temperatures below (ice fog) the value of the saturated state is applied.

### Result for Wrong Input Values:

Kappa\_ptW\_HAP\_SI = -1000

### References:

$v(p, t, W)$     Herrmann et al. [1], [2]

**Thermal Conductivity  $\lambda = f(p, t, W)$**

**Function Name:**

Lambda\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  LAMBDA_PTW_HUAIRPROP(P,T, W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

Lambda\_ptW\_HAP\_SI - Thermal conductivity in W/(m K)

**Range of Validity:**

Temperature  $t$ : from -73.5°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- A new very accurate algorithm is implemented between 0°C and 350°C
- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

Lambda\_ptW\_HAP\_SI = -1000

**References:**

$\lambda(p, t, W)$  Herrmann et al. [3], [4]  
 $\lambda_a(t)$  Lemmon et al. [18]  
 $\lambda_w(p, t)$  IAPWS-IF97 [7], [8] and IAPWS-08 [20]

**Kinematic Viscosity  $\nu = f(p, t, W)$** 
**Function Name:**

Ny\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  NY_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in kPa  
 $t$      -    Temperature  $t$  in °C  
 $W$      -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

Ny\_ptW\_HAP\_SI - Kinematic viscosity in m<sup>2</sup>/s

**Range of Validity:**

Temperature  $t$ :                      from -73.5°C to 350°C  
 Total pressure  $p$ :                    from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :                     $0 \leq W \leq W_s$

**Comments:**

- Kinematic Viscosity  $\nu = \frac{\eta}{\rho}$

**Result for Wrong Input Values:**

Ny\_ptW\_HAP\_SI = -1000

**References:**

$\eta(p, t, W)$     Herrmann et al. [3], [4]  
 $\rho(p, t, W)$     Herrmann et al. [1], [2]

|                                                                    |
|--------------------------------------------------------------------|
| <b>Backward Function: Total Pressure <math>p = f(t,s,W)</math></b> |
|--------------------------------------------------------------------|

**Function Name:**

p\_tsW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION P_TSW_HUAIRPROP(T,S,W), REAL*8 T,S,W
```

**Input Values:**

$t$      -    Temperature  $t$  in °C  
 $s$      -    Air-specific entropy  $s$  in kJ/(kg<sub>a</sub> K)  
 $W$      -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

p\_tsW\_HAP\_SI - Total pressure in kPa

**Range of Validity:**

Temperature  $t$ :                    from -143.5°C to 350°C  
 Air-specific entropy  $s$ :            from -26.53 kJ/(kg<sub>a</sub> K) to 38.990 kJ/(kg<sub>a</sub> K)  
 Humidity ratio  $W$ :                 $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Iteration of total pressure  $p$  from  $s = f(p,t,W)$

**Result for Wrong Input Values:**

p\_tsW\_HAP\_SI = -1000

**References:**

$s(p,t,W)$     Herrmann et al. [1], [2]

**Pressure  $p = f(z_{\text{ele}})$** 
**Function Name:**

p\_zele\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION P_ZELE_HUAIRPROP(ZELE), REAL*8 ZELE
```

**Input Values:**

$z_{\text{ele}}$  - Elevation  $z_{\text{ele}}$  in m

**Result:**

p\_zele\_HAP\_SI - Pressure of humid air in kPa

**Range of Validity:**

Elevation  $z_{\text{ele}}$  from -5,000 m to 11,000 m

**Comments:**

- Pressure of humid air from elevation

$$- p(z_{\text{ele}}) = 101.325 \text{ kPa} \cdot \left( 1 - 2.25577 \cdot 10^{-5} \cdot \frac{z_{\text{ele}}}{\text{m}} \right)^{5.256}$$

**Result for Wrong Input Values:**

p\_zele\_HAP\_SI = -1000

**References:**

$p(z_{\text{ele}})$  ASHRAE [23]

**Partial Pressure of Dry Air  $p_{\text{Air}} = f(p, t, W)$**

**Function Name:**

pAir\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION PAIR_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

pAir\_ptW\_HAP\_SI - Partial pressure of (dry) air in humid air in kPa

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Partial pressure of (dry) air in humid air  $p_{\text{Air}} = 1 - p_{\text{H}_2\text{O}}$
- Partial pressure of water vapor at saturation is calculated in case of supersaturated humid air ( $W > W_s(p, t)$ )
- The temperature value is used to calculate the saturation state

**Result for Wrong Input Values:**

pAir\_ptW\_HAP\_SI = -1000

**References:**

$p_{\text{H}_2\text{O}}(p, W)$  Herrmann et al. [1], [2]

**Partial Pressure of Water Vapor  $p_{\text{H}_2\text{O}} = f(p, t, W)$** 
**Function Name:**

pH2O\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  PH2O_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in kPa  
 $t$        -    Temperature  $t$  in °C  
 $W$       -    Humidity ratio  $W$  in  $\text{kg}_w/\text{kg}_a$

**Result:**

pH2O\_ptW\_HAP\_SI - Partial pressure of water vapor in humid air in kPa

**Range of Validity:**

Temperature  $t$ :                    from -143.15°C to 350°C  
 Total pressure  $p$ :                from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :                 $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Partial pressure of water vapor in humid air  $p_{\text{H}_2\text{O}} = \frac{W \cdot p}{\left(\frac{R_a}{R_w} + W\right)}$
- Partial pressure of water vapor at saturation is calculated in case of supersaturated humid air ( $W > W_s(p, t)$ )
- The temperature value is used to calculate the saturation state

**Result for Wrong Input Values:**

pH2O\_ptW\_HAP\_SI = -1000

**References:**
 $p_{\text{H}_2\text{O}}(p, W)$     Herrmann et al. [1], [2]

**Partial Saturation Pressure of Water Vapor  $p_{\text{H}_2\text{O},s} = f(p, t)$** 
**Function Name:**

pH2Os\_pt\_HAP\_SI

**Fortran Program:**

REAL\*8 FUNCTION PH2OS\_PT\_HUAIRPROP(P,T), REAL\*8 P,T

**Input Values:** $p$  - Total pressure  $p$  in kPa $t$  - Temperature  $t$  in °C**Result:**

pH2Os\_pt\_HAP\_SI - Partial saturation pressure of water vapor in humid air in kPa

**Range of Validity:**Temperature  $t$ : from -143.15°C to 350°CTotal pressure  $p$ : from 0.01 kPa to 10 000 kPa**Comments:**- Partial pressure of steam at saturation  $p_{\text{H}_2\text{O},s} = f \cdot p_s(t)$ with  $p_s(t)$  for  $t \geq 0.01^\circ\text{C}$  - Steam pressure of waterfor  $t < 0.01^\circ\text{C}$  - Sublimation pressure of water**Result for Wrong Input Values:**

pH2Os\_pt\_HAP\_SI = -1000

**References:** $f(p, t)$  Herrmann et al. [1], [2] $p_s(t)$  for  $t \geq 0.01^\circ\text{C}$  IAPWS-IF97 [7], [8]for  $t < 0.01^\circ\text{C}$  IAPWS-08 [11]



## Relative Humidity $\varphi = f(p, t, W)$

### Function Name:

phi\_ptW\_HAP\_SI

### Fortran Program:

```
REAL*8 FUNCTION PHI_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

### Input Values:

$p$      -    Total pressure  $p$  in kPa  
 $t$        -    Temperature  $t$  in °C  
 $W$       -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

### Result:

phi\_ptW\_HAP\_SI - Relative humidity (decimal ratio)

### Range of Validity:

Temperature  $t$ :                      from -143.15°C to 350°C  
 Total pressure  $p$ :                    from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :                    $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

### Comments:

- Relative humidity  $\varphi = \frac{p_{\text{H}_2\text{O}}}{p_{\text{H}_2\text{O},s}}$
- This equation is valid for  $p_{\text{H}_2\text{O}} \leq p_{\text{H}_2\text{O},s}$  and for  $0 \leq \varphi \leq 1$

### Result for Wrong Input Values:

phi\_ptW\_HAP\_SI = -1000

### References:

$\varphi(p, t, W)$  Herrmann et al. [1], [2]

**Prandtl Number  $Pr = f(p, t, W)$** **Function Name:**

Pr\_ptW\_HAP\_SI

**Fortran Program:**

REAL\*8 FUNCTION PR\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

Pr\_ptW\_HAP\_SI - Prandtl number

**Range of Validity:**

Temperature  $t$ : from -73.5°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Prandtl number  $Pr = \frac{\eta \cdot c_p}{\lambda}$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

Pr\_ptW\_HAP\_SI = -1000

**References:**

$\eta(p, t, W)$  Herrmann et al. [3], [4]  
 $c_p(p, t, W)$  Herrmann et al. [3], [4]  
 $\lambda(p, t, W)$  Lemmon et al. [20]

**Mole Fraction of Dry Air  $\psi_{\text{Air}} = f(W)$** 
**Function Name:**

PsiAir\_W\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION PSIAIR_W_HUAIRPROP(W), REAL*8 W
```

**Input Values:**

$W$  - Humidity ratio  $W$  in  $\text{kg}_w/\text{kg}_a$

**Result:**

PsiAir\_W\_HAP\_SI - Mole fraction of (dry) air in humid air in  $\text{mol}_a/\text{mol}$

**Range of Validity:**

Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Mole fraction of air  $\psi_{\text{Air}} = 1 - \psi_{\text{H}_2\text{O}} = 1 - \left( \frac{W}{\frac{R_a}{R_{\text{H}_2\text{O}}} + W} \right)$

**Result for Wrong Input Values:**

PsiAir\_W\_HAP\_SI = -1000

**References:**

$\psi_{\text{Air}}(W)$  Herrmann et al. [1], [2]

**Mole Fraction of Water  $\psi_{\text{H}_2\text{O}} = f(W)$**

**Function Name:**

PsiH2O\_W\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION PSIH2O_W_HUAIRPROP(W), REAL*8 W
```

**Input Values:**

$W$  - Humidity ratio  $W$  in  $\text{kg}_w/\text{kg}_a$

**Result:**

PsiH2O\_W\_HAP\_SI - Mole fraction of water in humid air in  $\text{mol}_w/\text{mol}$

**Range of Validity:**

Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Mole fraction of water  $\psi_{\text{H}_2\text{O}} = \frac{W}{\frac{R_a}{R_{\text{H}_2\text{O}}} + W}$

**Result for Wrong Input Values:**

PsiH2O\_W\_HAP\_SI = -1000

**References:**

$\psi_{\text{H}_2\text{O}}(W)$  Herrmann et al. [1], [2]

**Density  $\rho = f(p, t, W)$** **Function Name:**

Rho\_ptW\_HAP\_SI

**Fortran Program:**

REAL\*8 FUNCTION RHO\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**Rho\_ptW\_HAP\_SI - Density of humid air in kg/m<sup>3</sup>**Range of Validity:**

Temperature  $t$ : from -143.15°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Density of humid air obtained from air-specific volume:  $\rho = \frac{1+W}{v}$

**Result for Wrong Input Values:**

Rho\_ptW\_HAP\_SI = -1000

**References:** $\rho(p, t, W)$  Herrmann et al. [1], [2]

**Air-Specific Entropy  $s = f(p, t, W)$**

**Function Name:**

s\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION S_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

s\_ptW\_HAP\_SI - Air-specific entropy in kJ/(kg<sub>a</sub> K)

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 350°C  
 Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

s\_ptW\_HAP\_SI = -1000

**References:**

$s(p, t, W)$  Herrmann et al. [1], [2]

**Backward Function: Temperature  $t = f(p, h, \varphi)$** 
**Function Name:**

t\_phphi\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  T_PHPHI_HUAIRPROP(P,H,PHI), REAL*8 P,H,PHI
```

**Input Values:**

$p$      -    Total pressure  $p$  in kPa  
 $h$      -    Air-specific enthalpy  $h$  in kJ/kg<sub>a</sub>  
 $\varphi$     -    Relative humidity  $\varphi$  (decimal ratio)

**Result:**

t\_phphi\_HAP\_SI - Temperature from pressure, enthalpy, and relative humidity in °C

**Range of Validity:**

Total pressure  $p$ :                from 0.01 kPa to 10 000 kPa  
 Air-specific enthalpy  $h$ :        from -5745 kJ/kg<sub>a</sub> to 29690 kJ/kg<sub>a</sub>  
 Relative humidity  $\varphi$ :             $0 \leq \varphi \leq 1$

**Comments:**

- Iteration of temperature  $t$  from  $h = f(p, t, W)$  using  $W = f(p, t, \varphi)$

**Result for Wrong Input Values:**

t\_phphi\_HAP\_SI = -1000

**References:**

$h(p, t, W)$     Herrmann et al. [1], [2]

## Backward Function: Temperature $t = f(p, h, W)$

### Function Name:

t\_phW\_HAP\_SI

### Fortran Program:

```
REAL*8 FUNCTION T_PHW_HUAIRPROP(P,H,W), REAL*8 P,H,W
```

### Input Values:

$p$  - Total pressure  $p$  in kPa  
 $h$  - Air-specific enthalpy  $h$  in kJ/kg<sub>a</sub>  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

### Result:

t\_phW\_HAP\_SI - Temperature from pressure, enthalpy, and humidity ratio in °C

### Range of Validity:

Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Air-specific enthalpy  $h$ : from -5745 kJ/kg<sub>a</sub> to 29690 kJ/kg<sub>a</sub>  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

### Comments:

- Iteration of temperature  $t$  from  $h = f(p, t, W)$

### Result for Wrong Input Values:

t\_phW\_HAP\_SI = -1000

### References:

$h(p, t, W)$  Herrmann et al. [1], [2]



**Backward Function: Temperature  $t = f(p, s, W)$** 
**Function Name:**

t\_psW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION T_PSW_HUAIRPROP(P,S,W), REAL*8 P,S,W
```

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $s$  - Air-specific entropy  $s$  in kJ/(kg<sub>a</sub> K)  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

t\_psW\_HAP\_SI - Temperature from pressure, entropy, and humidity ratio in °C

**Range of Validity:**

Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Air-specific entropy  $s$ : from -26.53 kJ/(kg<sub>a</sub> K) to 38.990 kJ/(kg<sub>a</sub> K)  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Iteration of temperature  $t$  from  $s = f(p, t, W)$

**Result for Wrong Input Values:**

t\_psW\_HAP\_SI = -1000

**References:**

$s(p, t, W)$  Herrmann et al. [1], [2]

## Backward Function: Temperature $t = f(p, t_{wb}, W)$

### Function Name:

t\_ptwbW\_HAP\_SI

### Fortran Program:

```
REAL*8 FUNCTION T_PTWWBW_HUAIRPROP(P,TWB,W), REAL*8 P,TWB,W
```

### Input Values:

$p$  - Total pressure  $p$  in kPa  
 $t_{wb}$  - Wet-bulb temperature in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

### Result:

t\_ptwbW\_HAP\_SI - Temperature from pressure, wet bulb temperature and humidity ratio in °C

### Range of Validity:

Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Wet bulb temperature  $t_{wb}$ : from -143.15°C to 350°C  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

### Comments:

- Iteration of temperature  $t$  from  $t_{wb} = f(p, t, W)$

### Result for Wrong Input Values:

t\_ptwbW\_HAP\_SI = -1000

### References:

$t_{wb}(p, t, W)$  Herrmann et al. [1], [2]

**Dew-Point/Frost-Point Temperature  $t_d = f(p, W)$** 
**Function Name:**

td\_pW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION TD_PW_HUAIRPROP(P,W), REAL*8 P,W
```

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $W$  - Humidity ratio  $W$  in  $\text{kg}_w/\text{kg}_a$

**Result:**

td\_pW\_HAP\_SI - Dew-point/frost-point temperature in °C

**Range of Validity:**

Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

Dew-point temperature  $t_d = t_s(p_{\text{H}_2\text{O}})$  for  $t \geq 0.01^\circ\text{C}$  (saturation temperature of water in humid air)

$t_d = t_{\text{sub}}(p_{\text{H}_2\text{O}})$  for  $t \leq 0.01^\circ\text{C}$  (sublimation temperature of water in humid air)

**Result for Wrong Input Values:**

td\_pW\_HAP\_SI = -1000

**References:**

$t_s(p_{\text{H}_2\text{O}})$  for  $t_d \geq 0.01^\circ\text{C}$  IAPWS-IF97 [7], [8]  
 $t_{\text{sub}}(p_{\text{H}_2\text{O}})$  for  $t_d \leq 0.01^\circ\text{C}$  IAPWS-08 [11]  
 $p_{\text{H}_2\text{O}}$  Herrmann et. al. [1], [2]

## Saturation Temperature $t_s = f(p, p_{H_2O})$

### Function Name:

ts\_ppH2O\_HAP\_SI

### Fortran Program:

```
REAL*8 FUNCTION TS_PPH2O_HUAIRPROP(P,PH2O), REAL*8 P,PH2O
```

### Input Values:

$p$  - Total pressure  $p$  in kPa  
 $p_{H_2O}$  - Partial pressure of water vapor  $p_{H_2O}$  in kPa

### Result:

ts\_ppH2O\_HAP\_SI - Saturation temperature in °C

### Range of Validity:

Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Partial Pressure  $p_{H_2O}$ : from 0.01 kPa to 10 000 kPa

### Comments:

- Iteration of saturation temperature  $t_s$  from  $p_{H_2O,s} = f(p, t)$

### Result for Wrong Input Values:

ts\_ppH2O\_HAP\_SI = -1000

### References:

$p_{H_2O,s}$  Herrmann et. al. [1], [2]

**Wet-Bulb/Ice-Bulb Temperature  $t_{wb} = f(p, t, W)$** 
**Function Name:**

twb\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION TWB_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in kPa  
 $t$        -    Temperature  $t$  in °C  
 $W$       -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

twb\_ptW\_HAP\_SI - Wet-bulb/ice-bulb temperature in °C

**Range of Validity:**

Temperature  $t$ :                    from -143.15°C to 350°C  
 Total pressure  $p$ :                from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :                 $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Iteration of wet-bulb/ice-bulb temperature  $t_{wb}$   
   from  $h^{\text{unsaturated}}(p, t, W) = h^{\text{fog}}(p, t_{wb}, W)$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

twb\_ptW\_HAP\_SI = -1000

**References:** $t_{wb}(p, t, W)$  Herrmann et al. [1], [2]

**Air-Specific Internal Energy  $u = f(p, t, W)$** 
**Function Name:**

u\_ptW\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  U_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in kPa  
 $t$        -    Temperature  $t$  in °C  
 $W$       -    Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

u\_ptW\_HAP\_SI    -    Air-specific internal energy in kJ/kg<sub>a</sub>

**Range of Validity:**

Temperature  $t$ :                    from -143.15°C to 350°C  
 Total pressure  $p$ :                from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :                 $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Internal energy  $u = h - pv$

**Result for Wrong Input Values:**

u\_ptW\_HAP\_SI = -1000

**References:**

$u(p, t, W)$     Herrmann et al. [1], [2]

**Air-Specific Volume  $v = f(p, t, W)$** 
**Function Name:**

`v_ptW_HAP_SI`

**Fortran Program:**

```
REAL*8 FUNCTION V_PTW_HUAIRPROP(P,T,W), REAL*8 P,T,W
```

**Input Values:**

$p$      -    Total pressure  $p$  in kPa  
 $t$        -    Temperature  $t$  in °C  
 $W$       -    Humidity ratio  $W$  in  $\text{kg}_w/\text{kg}_a$

**Result:**

`v_ptW_HAP_SI`    -    Air-specific volume in  $\text{m}^3/\text{kg}_a$

**Range of Validity:**

Temperature  $t$ :                      from -143.15°C to 350°C  
 Total pressure  $p$ :                    from 0.01 kPa to 10 000 kPa  
 Humidity ratio  $W$ :                     $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- When calculating supersaturated air an ideal mixing model (saturated humid air and water droplets (or ice crystals) homogeneously mixed) is applied

**Result for Wrong Input Values:**

`v_ptW_HAP_SI` = -1000

**References:**

$v(p, t, W)$     Herrmann et al. [1], [2]

**Humidity Ratio from Partial Pressure of Steam  $W = f(p, t, p_{H_2O})$** 
**Function Name:**

W\_ptpH2O\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION W_PTPH2O_HUAIRPROP(P,T,PH2O), REAL*8 P,T,PH2O
```

**Input Values:**

- $p$  - Total pressure  $p$  in kPa
- $t$  - Temperature  $t$  in °C
- $p_{H_2O}$  - Partial pressure of water  $p_{H_2O}$  in kPa

**Result:**

W\_ptpH2O\_HAP\_SI - Humidity ratio from temperature and partial pressure of water vapor in  $\text{kg}_w/\text{kg}_a$

**Range of Validity:**

- Total pressure  $p$ : from 0.01 kPa to 10 000 kPa
- Temperature  $t$ : from -143.15°C to 350°C
- Partial pressure  $p_{H_2O}$ : from 0.01 kPa to 10 000 kPa

**Comments:**

- Iteration of humidity ratio  $W$  from  $p_{H_2O} = f(p, t, W)$
- Result for supersaturated humid air is  $W_s$

**Result for Wrong Input Values:**

W\_ptpH2O\_HAP\_SI = -1000

**References:**

$p_{H_2O}(p, t, W)$  Herrmann et al. [1], [2]



W\_ptphi\_HAP\_SI

### Fortran Program:

```
REAL*8 FUNCTION  W_PTPHI_HUAIRPROP(P,T,PHI), REAL*8 P,T,PHI
```

**Input Values:**

- $p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $\varphi$  - Relative humidity (decimal ratio)

**Result:**

W\_ptphi\_HAP\_SI - Humidity ratio from temperature and relative humidity  
in  $\text{kg}_w/\text{kg}_a$

### Range of Validity:

- |                               |                             |
|-------------------------------|-----------------------------|
| Temperature $t$ :             | from -143.15°C to 350°C     |
| Total pressure $p$ :          | from 0.01 kPa to 10 000 kPa |
| Relative humidity $\varphi$ : | $0 \leq \varphi \leq 1$     |

**Comments:**

- Iteration of humidity ratio  $W$  from  $\phi = f(p, t, W)$

### Result for Wrong Input Values:

W\_ptphi\_HAP\_SI = -1000

### References:

 $\varphi(p, t, W)$  Herrmann et al. [1], [2]

**Humidity Ratio from Dew-Point Temperature  $W = f(p, t_d)$** 
**Function Name:**

W\_ptd\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION W_PTD_HUAIRPROP(P,TD), REAL*8 P,TD
```

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t_d$  - Dew-point temperature  $t_d$  in °C

**Result:**

W\_ptd\_HAP\_SI - Humidity ratio from temperature and dew-point temperature  
in  $\text{kg}_w/\text{kg}_a$

**Range of Validity:**

Dew point temperature  $t_d$ : from -143.15°C to 350°C  
Total pressure  $p$ : from 0.01 kPa to 10 000 kPa

**Comments:**

- Iteration of humidity ratio  $W$  from  $t_d = f(p, W)$

**Result for Wrong Input Values:**

W\_ptd\_HAP\_SI = -1000

**References:**

$t_d(p, W)$  Herrmann et al. [1], [2]

W\_pttwb\_HAP\_SI

## Fortran Program:

```
REAL*8 FUNCTION  W_PTTWB_HUAIRPROP(P,T,TWB), REAL*8 P,T,TWB
```

**Input Values:**

- $p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $t_{wb}$  - Wet-bulb temperature in °C

**Result:**

W\_pttwb\_HAP\_SI - Humidity ratio from temperature and wet-bulb temperature  
in  $\text{kg}_w/\text{kg}_a$

### Range of Validity:

- |                                 |                             |
|---------------------------------|-----------------------------|
| Total pressure $p$ :            | from 0.01 kPa to 10 000 kPa |
| Temperature $t$ :               | from -143.15°C to 350°C     |
| Wet-bulb temperature $t_{wb}$ : | from -143.15°C to 350°C     |

**Comments:**

- Iteration of humidity ratio  $W$  from  $t_{wb} = f(p, t, W)$
- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

### Result for Wrong Input Values:

W\_pttwb\_HAP\_SI = -1000

### References:

|                   |                          |
|-------------------|--------------------------|
| $t_{wb}(p, t, W)$ | Herrmann et al. [1], [2] |
|-------------------|--------------------------|

## Saturation Humidity Ratio $W_s = f(p, t)$

### Function Name:

Ws\_pt\_HAP\_SI

### Fortran Program:

```
REAL*8 FUNCTION WS_PT_HUAIRPROP(P,T), REAL*8 P,T
```

### Input Values:

$p$      -    Total pressure  $p$  in kPa  
 $t$        -    Temperature  $t$  in °C

### Result:

Ws\_pt\_HAP\_SI    -    Saturation humidity ratio (mass fraction) in  $\text{kg}_w/\text{kg}_a$

### Range of Validity:

Total pressure  $p$ :                      from 0.01 kPa to 10 000 kPa  
 Temperature  $t$ :                         from -143.15°C to 350°C

### Comments:

- Calculation of saturation humidity ratio  $W_s$  from  $W_s = \frac{M_{\text{H}_2\text{O}}}{M_a} \frac{p_{\text{H}_2\text{O},s}}{(p - p_{\text{H}_2\text{O},s})}$

### Result for Wrong Input Values:

Ws\_pt\_HAP\_SI = -1000

### References:

$p_{\text{H}_2\text{O},s}$             Herrmann et al. [1], [2]

**Mass Fraction of Dry Air  $\xi_{\text{Air}} = f(W)$** 
**Function Name:**

XiAir\_W\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  XIAIR_W_HUAIRPROP(W), REAL*8 W
```

**Input Values:**

$W$  - Humidity ratio  $W$  in  $\text{kg}_w/\text{kg}_a$

**Result:**

XiAir\_W\_HAP\_SI - Mass fraction of (dry) air in humid air in  $\text{kg}_a/\text{kg}$

**Range of Validity:**

Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Mass fraction of (dry) air  $\xi_{\text{Air}} = 1 - \xi_{\text{H}_2\text{O}} = 1 - \frac{W}{1 + W}$

**Result for Wrong Input Values:**

XiAir\_W\_HAP\_SI = -1000

**References:**

$\xi_{\text{Air}}(W)$  Herrmann et al. [1], [2]

**Mass Fraction of Water Vapor  $\xi_{\text{H}_2\text{O}} = f(W)$**

**Function Name:**

XiH2O\_W\_HAP\_SI

**Fortran Program:**

```
REAL*8 FUNCTION XIH2O_W_HUAIRPROP(W), REAL*8 W
```

**Input Values:**

$W$  - Humidity ratio  $W$  in  $\text{kg}_w/\text{kg}_a$

**Result:**

XiH2O\_W\_HAP\_SI - Mass fraction of water vapor in humid air in  $\text{kg}_w/\text{kg}$

**Range of Validity:**

Humidity ratio  $W$ :  $0 \leq W \leq 10 \text{ kg}_w/\text{kg}_a$

**Comments:**

- Mass fraction of water vapor  $\xi_{\text{H}_2\text{O}} = \frac{W}{1+W}$

**Result for Wrong Input Values:**

XiH2O\_W\_HAP\_SI = -1000

**References:**

$\xi_{\text{H}_2\text{O}}(W)$  Herrmann et al. [1], [2]

**Compression Factor  $Z = f(p, t, W)$** **Function Name:**

Z\_ptW\_HAP\_SI

**Fortran Program:**

REAL\*8 FUNCTION Z\_PTW\_HUAIRPROP(P,T,W), REAL\*8 P,T,W

**Input Values:**

$p$  - Total pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C  
 $W$  - Humidity ratio  $W$  in kg<sub>w</sub>/kg<sub>a</sub>

**Result:**

Z\_ptW\_HAP\_SI - Compression factor (decimal ratio)

**Range of Validity:**

Total pressure  $p$ : from 0.01 kPa to 10 000 kPa  
 Temperature  $t$ : from -143.15°C to 350°C  
 Humidity ratio  $W$ :  $0 \leq W \leq W_s$

**Comments:**

- Compression factor  $Z = 1 + \frac{B_m}{\bar{v}} + \frac{C_m}{\bar{v}^2}$

with  $\bar{v} = \frac{M}{\rho} = \frac{M v}{1+W}$

and  $M$  is the molar mass of humid air

- Calculation for supersaturated humid air ( $W > W_s$ ) is not possible

**Result for Wrong Input Values:**

Z\_ptW\_HAP\_SI = -1000

**References:**

$B_m(t, W), C_m(t, W)$  Herrmann et al. [1], [2]

$\rho(p, t, W), v(p, t, W)$  Herrmann et al. [1], [2]

## **3.2 Functions for Steam and Water for Temperatures $t \geq 0^\circ\text{C}$**



**Specific Enthalpy of Liquid Water  $h_{\text{liq}} = f(p, t)$** 
**Function Name:**

hliq\_pt\_97\_SI

**Fortran Program:**

REAL\*8 FUNCTION HLIQ\_PT\_97(P,T), REAL\*8 P,T

**Input Values:**

$p$  - Pressure  $p$  in kPa  
 $t$  - Temperature  $t$  in °C

**Result:**

hliq\_pt\_97\_SI - Specific enthalpy of liquid water in kJ/kg

**Range of Validity:**

Pressure  $p$ : from  $p_s(0^\circ\text{C}) = 0.6112$  kPa to 10000 kPa  
 Temperature  $t$ : from  $0^\circ\text{C}$  to  $350^\circ\text{C}$

**Comments:**- Specific enthalpy of liquid water  $h_{\text{liq}} = h^{97}(p, t)$  (Region 1)**Result for Wrong Input Values:**

hliq\_pt\_97\_SI = -1000

**References:** $h^{97}(p, t)$  IAPWS-IF97 [7], [8]

**Specific Enthalpy of Saturated Liquid Water  $h_{\text{liq},s} = f(t)$** 
**Function Name:**

hliqs\_t\_97\_SI

**Fortran Program:**

REAL\*8 FUNCTION HLIQS\_T\_97(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °C**Result:**

hliqs\_t\_97\_SI - Specific enthalpy of saturated liquid water in kJ/kg

**Range of Validity:**Temperature  $t$ : from 0°C to 350°C**Comments:**- Specific enthalpy of liquid water  $h_{\text{liq},s} = h^{97}(p_s, t)$  (Region 1)with  $p_s = p_s^{97}(t)$ **Result for Wrong Input Values:**

hliqs\_t\_97\_SI = -1000

**References:** $h^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

**Specific Enthalpy of Saturated Water Vapor  $h_{\text{vap},s} = f(t)$** 
**Function Name:**

hvaps\_t\_97\_SI

**Fortran Program:**

```
REAL*8 FUNCTION HVAPS_T_97(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

hvaps\_t\_97\_SI - Specific enthalpy of saturated water vapor in kJ/kg

**Range of Validity:**

Temperature  $t$ : from 0°C to 350°C

**Comments:**

- Specific enthalpy of saturated water vapor  $h_{\text{vap},s} = h^{97}(p_s, t)$  (Region 2)  
with  $p_s = p_s^{97}(t)$

**Result for Wrong Input Values:**

hvaps\_t\_97\_SI = -1000

**References:**

$h^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

## Saturation Pressure of Water $p_s = f(t)$

### Function Name:

ps\_t\_97\_SI

### Fortran Program:

```
REAL*8 FUNCTION PS_T_97(T), REAL*8 T
```

### Input Values:

$t$  - Temperature  $t$  in °C

### Result:

ps\_t\_97\_SI - Saturation pressure of water in kPa

### Range of Validity:

Temperature  $t$ : from 0°C to 350°C

### Comments:

- Saturation pressure of water  $p_s = p_s^{97}(t)$  (Region 4)

### Result for Wrong Input Values:

ps\_t\_97\_SI -1000

### References:

$p_s^{97}(t)$  IAPWS-IF97 [7], [8]

## Specific Entropy of Liquid Water $s_{\text{liq}} = f(p, t)$

### Function Name:

sliq\_pt\_97\_SI

### Fortran Program:

```
REAL*8 FUNCTION SLIQ_PT_97(P,T), REAL*8 P,T
```

### Input Values:

$p$      -    Pressure  $p$  in kPa  
 $t$      -    Temperature  $t$  in °C

### Result:

sliq\_pt\_97\_SI - Specific entropy of liquid water in kJ/(kg K)

### Range of Validity:

Pressure  $p$ :                      from  $p_s(0^\circ\text{C}) = 0.6112$  kPa to 10000 kPa  
 Temperature  $t$ :                      from  $0^\circ\text{C}$  to  $350^\circ\text{C}$

### Comments:

- Specific entropy of liquid water  $s_{\text{liq}} = s^{97}(p, t)$  (Region 1)

### Result for Wrong Input Values:

sliq\_pt\_97\_SI = -1000

### References:

$s^{97}(p, t)$      IAPWS-IF97 [7], [8]

**Specific Entropy of Saturated Liquid Water  $s_{\text{liq},s} = f(t)$** 
**Function Name:**

sliqs\_t\_97\_SI

**Fortran Program:**

REAL\*8 FUNCTION SLIQS\_T\_97(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °C**Result:**

sliqs\_t\_97\_SI - Specific entropy of saturated liquid water in kJ/(kg K)

**Range of Validity:**Temperature  $t$ : from 0°C to 350°C**Comments:**- Specific entropy of liquid water  $s_{\text{liq},s} = s^{97}(p_s, t)$  (Region 1)with  $p_s = p_s^{97}(t)$ **Result for Wrong Input Values:**

sliqs\_t\_97\_SI = -1000

**References:** $s^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

## Specific Entropy of Saturated Water Vapor $s_{\text{vap},s} = f(t)$

**Function Name:**

svaps\_t\_97\_SI

**Fortran Program:**

```
REAL*8 FUNCTION SVAPS_T_97(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

svaps\_t\_97\_SI - Specific entropy of saturated water vapor in kJ/(kg K)

**Range of Validity:**

Temperature  $t$ : from 0°C to 350°C

**Comments:**

- Specific entropy of saturated water vapor  $s_{\text{vap},s} = s^{97}(p_s, t)$  (Region 2)
- with  $p_s = p_s^{97}(t)$

**Result for Wrong Input Values:**

svaps\_t\_97\_SI = -1000

**References:**

$s^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

## Saturation Temperature of Water $t_s = f(p)$

**Function Name:**

ts\_p\_97\_SI

**Fortran Program:**

```
REAL*8 FUNCTION TS_P_97(P), REAL*8 P
```

**Input Values:**

$p$  - Pressure  $p$  in kPa

**Result:**

ts\_p\_97\_SI - Saturation temperature of water in °C

**Range of Validity:**

Pressure  $p$ : from 0.6112 kPa to 10 000 kPa

**Comments:**

- Saturation temperature of water  $t_s = t_s^{97}(p)$  (Region 4)

**Result for Wrong Input Values:**

ts\_p\_97\_SI = -1000

**References:**

$t_s^{97}(p)$  IAPWS-IF97 [7], [8]



## Specific Volume of Liquid Water $v_{\text{liq}} = f(p, t)$

### Function Name:

vliq\_pt\_97\_SI

### Fortran Program:

```
REAL*8 FUNCTION  VLIQ_PT_97(P,T), REAL*8 P,T
```

### Input Values:

$p$      -    Pressure  $p$  in kPa  
 $t$      -    Temperature  $t$  in °C

### Result:

vliq\_pt\_97\_SI - Specific volume of liquid water in m<sup>3</sup>/kg

### Range of Validity:

Pressure  $p$ :                      from  $p_s(0^\circ\text{C}) = 0.6112$  kPa to 10 000 kPa  
 Temperature  $t$ :                from 0°C to 350°C

### Comments:

- Specific volume of liquid water  $v_{\text{liq}} = v^{97}(p, t)$  (Region 1)

### Result for Wrong Input Values:

vliq\_pt\_97\_SI = -1000

### References:

$v^{97}(p, t)$      IAPWS-IF97 [7], [8]

**Specific Volume of Saturated Liquid Water  $v_{\text{liq},s} = f(t)$** 
**Function Name:**

vliqs\_t\_97\_SI

**Fortran Program:**

REAL\*8 FUNCTION VLIQS\_T\_97(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °C**Result:**vliqs\_t\_97\_SI - Specific volume of saturated liquid water in  $\text{m}^3/\text{kg}$ **Range of Validity:**Temperature  $t$ : from 0°C to 350°C**Comments:**- Specific volume of liquid water  $v_{\text{liq},s} = v^{97}(p_s, t)$  (Region 1)with  $p_s = p_s^{97}(t)$ **Result for Wrong Input Values:**

vliqs\_t\_97\_SI = -1000

**References:** $v^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

**Specific Volume of Saturated Water Vapor  $v_{\text{vap},s} = f(t)$** 
**Function Name:**

vvaps\_t\_97\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  VVAPS_T_97(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

vvaps\_t\_97\_SI - Specific volume of saturated water vapor in  $\text{m}^3/\text{kg}$

**Range of Validity:**

Temperature  $t$ : from 0°C to 350°C

**Comments:**

- Specific volume of saturated water vapor  $v_{\text{vap},s} = v^{97}(p_s, t)$  (Region 2)  
with  $p_s = p_s^{97}(t)$

**Result for Wrong Input Values:**

vvaps\_t\_97\_SI = -1000

**References:**

$v^{97}(p, t), p_s^{97}(t)$  IAPWS-IF97 [7], [8]

### **3.3 Functions for Steam and Water for Temperatures $t \leq 0^\circ\text{C}$**

**Specific Enthalpy of Saturated Ice  $h_{\text{ice,sub}} = f(t)$** 
**Function Name:**

hicesub\_t\_06\_SI

**Fortran Program:**

```
REAL*8 FUNCTION HICESUB_T_06(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

hicesub\_t\_06\_SI - Specific enthalpy of saturated ice in kJ/kg

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 0°C

**Comments:**

- Specific enthalpy of saturated ice  $h_{\text{ice,sub}} = h^{06}(\rho_{\text{sub}}, t)$   
 with  $\rho_{\text{sub}} = \rho_{\text{sub}}^{08}(t)$

**Result for Wrong Input Values:**

hicesub\_t\_06\_SI = -1000

**References:**

$h^{06}(p, t)$  IAPWS-06 [10]

$\rho_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

**Specific Enthalpy of Saturated Water Vapor  $h_{\text{vap,sub}} = f(t)$** 
**Function Name:**

hvapsub\_t\_95\_SI

**Fortran Program:**

```
REAL*8 FUNCTION HVAPSUB_T_95(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

hvapsub\_t\_95\_SI - Specific enthalpy of saturated water vapor in kJ/kg

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 0°C

**Comments:**

- Specific enthalpy of saturated water vapor  $h_{\text{vap,sub}} = h^{95}(p_{\text{sub}}, t)$

with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$

**Result for Wrong Input Values:**

hvapsub\_t\_95\_SI = -1000

**References:**

$h^{95}(p, t)$  IAPWS-95 [5], [6]

$p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

## Melting Pressure $p_{\text{mel}} = f(t)$

**Function Name:**

pmel\_t\_08\_SI

**Fortran Program:**

```
REAL*8 FUNCTION PMEL_T_08 (T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

pmel\_t\_08\_SI - Melting pressure of ice in kPa

**Range of Validity:**

Temperature  $t$ : from -21.985°C to 0°C

**Result for Wrong Input Values:**

pmel\_t\_08\_SI = -1000

**References:**

$p_{\text{mel}}^{08}(t)$  IAPWS-08 [11]

## Sublimation Pressure $p_{\text{sub}} = f(t)$

**Function Name:**

psub\_t\_08\_SI

**Fortran Program:**

```
REAL*8 FUNCTION PSUB_T_08 (T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

psub\_t\_08\_SI - Sublimation pressure of ice in kPa

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 0°C

**Result for Wrong Input Values:**

psub\_t\_08\_SI = -1000

**References:**

$p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]



## Specific Entropy of Saturated Ice $s_{\text{ice,sub}} = f(t)$

**Function Name:**

sicesub\_t\_06\_SI

**Fortran Program:**

```
REAL*8 FUNCTION SICESUB_T_06(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

sicesub\_t\_06\_SI - Specific entropy of saturated ice in kJ/(kg K)

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 0°C

**Comments:**

- Specific entropy of saturated ice  $s_{\text{ice,sub}} = s^{06}(p_{\text{sub}}, t)$   
 with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$

**Result for Wrong Input Values:**

sicesub\_t\_06\_SI = -1000

**References:**

$s^{06}(p, t)$  IAPWS-06 [10]

$p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

**Specific Entropy of Saturated Water Vapor  $s_{\text{vap,sub}} = f(t)$** 
**Function Name:**

svapsub\_t\_95\_SI

**Fortran Program:**

REAL\*8 FUNCTION SVAPSUB\_T\_95(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °C**Result:**

svapsub\_t\_95\_SI - Specific entropy of saturated water vapor in kJ/(kg K)

**Range of Validity:**Temperature  $t$ : from -143.15°C to 0°C**Comments:**- Specific entropy of saturated water vapor  $s_{\text{vap,sub}} = s^{95}(p_{\text{sub}}, t)$ with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$ **Result for Wrong Input Values:**

svapsub\_t\_95\_SI = -1000

**References:** $s^{95}(p, t)$  IAPWS-95 [7], [8] $p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

**Melting Temperature  $t_{\text{mel}} = f(p)$** 
**Function Name:**
 $t_{\text{mel\_p\_08\_SI}}$ 
**Fortran Program:**

```
REAL*8 FUNCTION TMEL_P_08(P), REAL*8 P
```

**Input Values:**

$p$  - Pressure  $p$  in kPa

**Result:**

$t_{\text{mel\_p\_08\_SI}}$  - Melting temperature of ice in °C

**Range of Validity:**

Pressure  $p$ : from  $p_s(0^\circ\text{C}) = 0.6112 \text{ kPa}$  to  $10\,000 \text{ kPa}$

**Result for Wrong Input Values:**

$t_{\text{mel\_p\_08\_SI}} = -1000$

**References:**

$t_{\text{mel}}^{08}(p)$  IAPWS-08 [11]

**Sublimation Temperature  $t_{\text{sub}} = f(p)$**

**Function Name:**

tsub\_p\_08\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  TSUB_P_08(P), REAL*8 P
```

**Input Values:**

$p$  - Pressure  $p$  in kPa

**Result:**

tsub\_p\_08\_SI - Sublimation temperature of ice in °C

**Range of Validity:**

Pressure  $p$ : from  $p_{\text{subl}}(-143.15^\circ\text{C}) = 1.2002 \times 10^{-11}$  kPa to  $p_{\text{subl}}(0^\circ\text{C}) = 0.6112$  kPa

**Result for Wrong Input Values:**

tsub\_p\_08\_SI = -1000

**References:**

$t_{\text{sub}}^{08}(p)$  IAPWS-08 [11]

**Specific Volume of Saturated Ice  $v_{\text{ice,sub}} = f(t)$** 
**Function Name:**

vicesub\_t\_06\_SI

**Fortran Program:**

REAL\*8 FUNCTION VICESUB\_T\_06(T), REAL\*8 T

**Input Values:** $t$  - Temperature  $t$  in °C**Result:**vicesub\_t\_06\_SI - Specific volume of saturated ice in  $\text{m}^3/\text{kg}$ **Range of Validity:**Temperature  $t$ : from -143.15°C to 0°C**Comments:**- Specific volume of saturated ice  $v_{\text{ice,sub}} = v^{06}(p_{\text{sub}}, t)$ with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$ **Result for Wrong Input Values:**

vicesub\_t\_06\_SI = -1000

**References:** $v^{06}(p, t)$  IAPWS-06 [10] $p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]

**Specific Volume of Saturated Water Vapor  $v_{\text{vap,sub}} = f(t)$** 
**Function Name:**

vvapsub\_t\_95\_SI

**Fortran Program:**

```
REAL*8 FUNCTION  VVAPSUB_T_95(T), REAL*8 T
```

**Input Values:**

$t$  - Temperature  $t$  in °C

**Result:**

vvapsub\_t\_95\_SI - Specific volume of saturated water vapor in  $\text{m}^3/\text{kg}$

**Range of Validity:**

Temperature  $t$ : from -143.15°C to 0°C

**Comments:**

- Specific volume of saturated water vapor  $v_{\text{vap,sub}} = v^{95}(p_{\text{sub}}, t)$

with  $p_{\text{sub}} = p_{\text{sub}}^{08}(t)$

**Result for Wrong Input Values:**

vvapsub\_t\_95\_SI = -1000

**References:**

$v^{95}(p, t)$  IAPWS-95 [7], [8]

$p_{\text{sub}}^{08}(t)$  IAPWS-08 [11]



## 4. Property Libraries for Calculating Heat Cycles, Boilers, Turbines and Refrigerators

### Water and Steam

#### Library LibIF97

- Industrial Formulation IAPWS-IF97 (Revision 2007)
- Supplementary Standards
  - IAPWS-IF97-S01
  - IAPWS-IF97-S03rev
  - IAPWS-IF97-S04
  - IAPWS-IF97-S05
- IAPWS Revised Advisory Note No. 3 on Thermodynamic Derivatives (2008)

### Humid Combustion Gas Mixtures

#### Library LibHuGas

Model: Ideal mixture of the real fluids:  
 $\text{CO}_2$  - Span and Wagner     $\text{O}_2$  - Schmidt and Wagner  
 $\text{H}_2\text{O}$  - IAPWS-95    Ar - Tegeler et al.  
 $\text{N}_2$  - Span et al.  
 and of the ideal gases:  
 $\text{SO}_2$ , CO, Ne (Scientific Formulation of Bückner et al.)  
 Consideration of:  
 Dissociation from VDI 4670 and Poynting effect

### Humid Air

#### Library LibHuAir

Model: Ideal mixture of the real fluids:  
 • Dry air from Lemmon et al.  
 • Steam, water and ice from IAPWS-IF97 and IAPWS-06  
 Consideration of:  
 • Condensation and freezing of steam  
 • Dissociation from the VDI 4670  
 • Poynting effect from ASHRAE RP-1485

### Carbon Dioxide Including Dry Ice

#### Library LibCO2

Formulation of Span and Wagner (1996)

### Seawater

#### Library LibSeaWa

IAPWS Industrial Formulation 2013

### Ice

#### Library LibICE

Ice from IAPWS-06, Melting and sublimation pressures from IAPWS-08, Water from IAPWS-IF97, Steam from IAPWS-95 and -IF97

### Ideal Gas Mixtures

#### Library LibIdGasMix

Model: Ideal mixture of the ideal gases:  

|               |                      |               |            |
|---------------|----------------------|---------------|------------|
| Ar            | NO                   | He            | Propylene  |
| Ne            | $\text{H}_2\text{O}$ | $\text{F}_2$  | Propane    |
| $\text{N}_2$  | $\text{SO}_2$        | $\text{NH}_3$ | Iso-Butane |
| $\text{O}_2$  | $\text{H}_2$         | Methane       | n-Butane   |
| CO            | $\text{H}_2\text{S}$ | Ethane        | Benzene    |
| $\text{CO}_2$ | OH                   | Ethylene      | Methanol   |
| Air           |                      |               |            |

Consideration of:  
 • Dissociation from the VDI Guideline 4670

#### Library LibIDGAS

Model: Ideal gas mixture from VDI Guideline 4670

Consideration of:  
 • Dissociation from the VDI Guideline 4670

### Humid Air

#### Library ASHRAE LibHuAirProp

Model: Virial Equation from ASHRAE Report RP-1485 for real mixture of the real fluids:  
 - Dry air  
 - Steam

Consideration of:  
 • Enhancement of the partial saturation pressure of water vapor at elevated total pressures  
[www.ashrae.org/bookstore](http://www.ashrae.org/bookstore)

### Dry Air Including Liquid Air

#### Library LibRealAir

Formulation of Lemmon et al. (2000)

### Refrigerants

#### Ammonia

#### Library LibNH3

Formulation of Tillner-Roth et al. (1993)

#### R134a

#### Library LibR134a

Formulation of Tillner-Roth and Baehr (1994)

#### Iso-Butane

#### Library LibButane\_Iso

Formulation of Bückner and Wagner (2006)

#### n-Butane

#### Library LibButane\_n

Formulation of Bückner and Wagner (2006)

### Mixtures for Absorption Processes

#### Ammonia/Water Mixtures

#### Library LibAmWa

IAPWS Guideline 2001 of Tillner-Roth and Friend (1998)  
 Helmholtz energy equation for the mixing term  
 (also useable for calculating Kalina Cycle)

#### Water/Lithium Bromide Mixtures

#### Library LibWaLi

Formulation of Kim and Infante Ferreira (2004)  
 Gibbs energy equation for the mixing term

### Liquid Coolants

#### Liquid Secondary Refrigerants

#### Library LibSecRef

Liquid solutions of water with

|                                   |                     |
|-----------------------------------|---------------------|
| $\text{C}_2\text{H}_6\text{O}_2$  | Ethylene glycol     |
| $\text{C}_3\text{H}_8\text{O}_2$  | Propylene glycol    |
| $\text{C}_2\text{H}_5\text{OH}$   | Ethyl alcohol       |
| $\text{CH}_3\text{OH}$            | Methyl alcohol      |
| $\text{C}_3\text{H}_8\text{O}_3$  | Glycerol            |
| $\text{K}_2\text{CO}_3$           | Potassium carbonate |
| $\text{CaCl}_2$                   | Calcium chloride    |
| $\text{MgCl}_2$                   | Magnesium chloride  |
| NaCl                              | Sodium chloride     |
| $\text{C}_2\text{H}_3\text{KO}_2$ | Potassium acetate   |

Formulation of the International Institute of Refrigeration (1997)

**Ethanol****Library LibC2H5OH**

Formulation of Schroeder (2012)

**Methanol****Library LibCH3OH**Formulation of  
de Reuck and Craven (1993)**Propane****Library LibPropane**Formulation of  
Lemmon et al. (2009)**Siloxanes as ORC Working Fluids**Octamethylcyclotetrasiloxane  $C_8H_{24}O_4Si_4$  **Library LibD4**Decamethylcyclopentasiloxane  $C_{10}H_{30}O_5Si_5$  **Library LibD5**Tetradecamethylhexasiloxane  $C_{14}H_{42}O_6Si_6$  **Library LibMD4M**Hexamethyldisiloxane  $C_6H_{18}OSi_2$  **Library LibMM**

Formulation of Colonna et al. (2006)

Dodecamethylcyclohexasiloxane  $C_{12}H_{36}O_6Si_6$  **Library LibD6**Decamethyltetrasiloxane  $C_{10}H_{30}O_3Si_4$  **Library LibMD2M**Dodecamethylpentasiloxane  $C_{12}H_{36}O_4Si_5$  **Library LibMD3M**Octamethyltrisiloxane  $C_8H_{24}O_2Si_3$  **Library LibMDM**

Formulation of Colonna et al. (2008)

**Nitrogen****Library LibN2**Formulation of  
Span et al. (2000)**Hydrogen****Library LibH2**Formulation of  
Leachman et al. (2009)**Helium****Library LibHe**

Formulation of Arp et al. (1998)

**Hydrocarbons**Decane  $C_{10}H_{22}$  **Library LibC10H22**Isopentane  $C_5H_{12}$  **Library LibC5H12\_ISO**Neopentane  $C_5H_{12}$  **Library LibC5H12\_NEO**Isohexane  $C_6H_{14}$  **Library LibC6H14**Toluene  $C_7H_8$  **Library LibC7H8**

Formulation of Lemmon and Span (2006)

**Further Fluids**Carbon monoxide  $CO$  **Library LibCO**Carbonyl sulfide  $COS$  **Library LibCOS**Hydrogen sulfide  $H_2S$  **Library LibH2S**Dinitrogen monoxide  $N_2O$  **Library LibN2O**Sulfur dioxide  $SO_2$  **Library LibSO2**Acetone  $C_3H_6O$  **Library LibC3H6O**

Formulation of Lemmon and Span (2006)

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Fax.: +49-3583-61-1846**The following thermodynamic and transport properties can be calculated<sup>a</sup>:****Thermodynamic Properties**

- Vapor pressure  $p_s$
- Saturation temperature  $T_s$
- Density  $\rho$
- Specific volume  $v$
- Enthalpy  $h$
- Internal energy  $u$
- Entropy  $s$
- Exergy  $e$
- Isobaric heat capacity  $c_p$
- Isochoric heat capacity  $c_v$
- Isentropic exponent  $\kappa$
- Speed of sound  $w$
- Surface tension  $\sigma$

**Transport Properties**

- Dynamic viscosity  $\eta$
- Kinematic viscosity  $\nu$
- Thermal conductivity  $\lambda$
- Prandtl number  $Pr$

**Backward Functions**

- $T, v, s(p, h)$
- $T, v, h(p, s)$
- $p, T, v(h, s)$
- $p, T(v, h)$
- $p, T(v, u)$

**Thermodynamic Derivatives**

- Partial derivatives can be calculated.

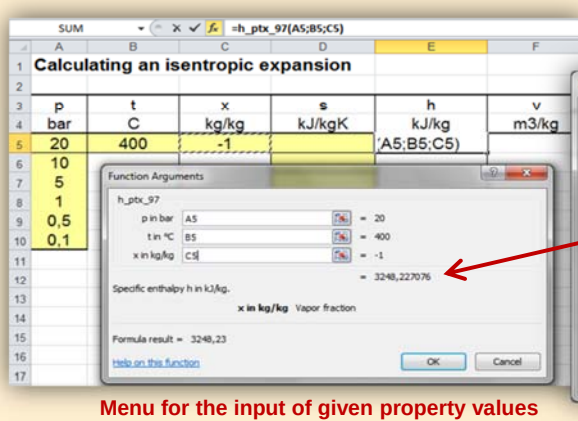
<sup>a</sup> Not all of these property functions are available in all property libraries.



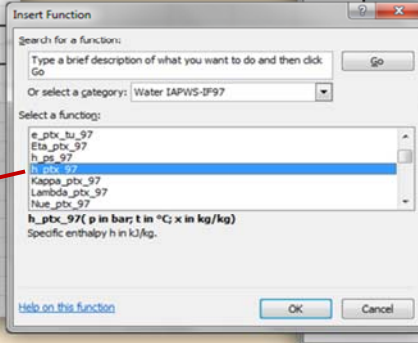


## Property Software for Calculating Heat Cycles, Boilers, Turbines and Refrigerators

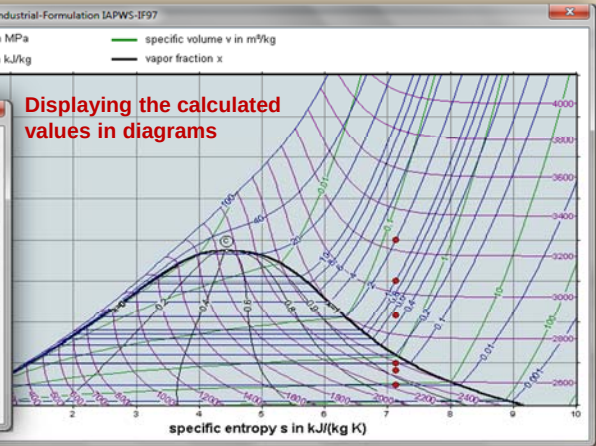
### Add-In FluidEXL<sup>Graphics</sup> for Excel<sup>®</sup>



Choosing a property library and a function

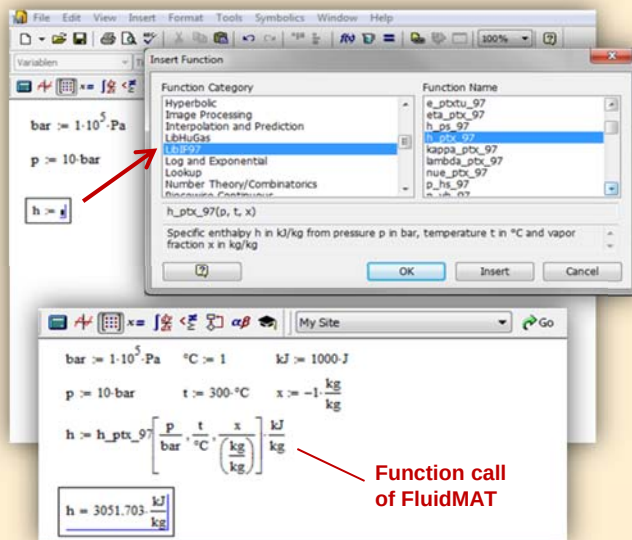


Displaying the calculated values in diagrams



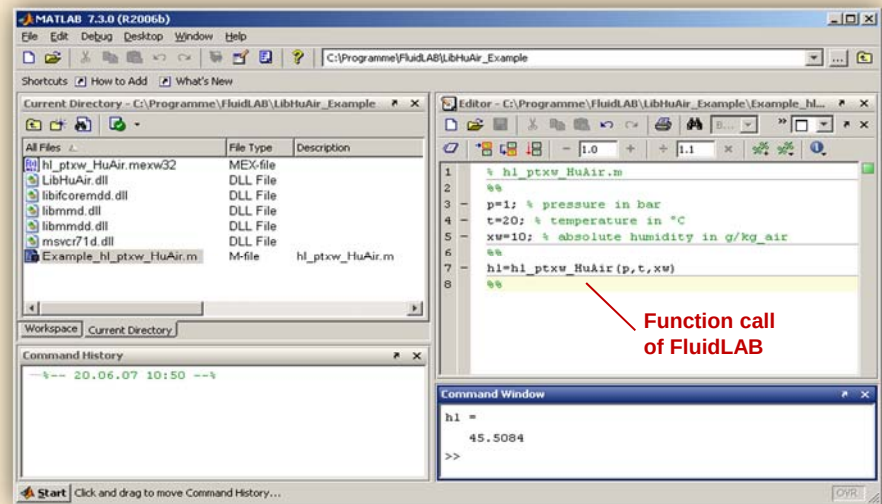
### Add-In FluidMAT<sup>®</sup> for Mathcad<sup>®</sup>

The property libraries can be used in Mathcad<sup>®</sup>.



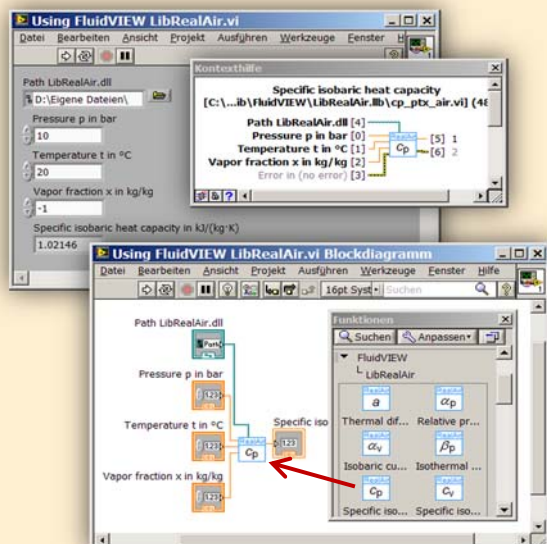
### Add-In FluidLAB<sup>®</sup> for MATLAB<sup>®</sup>

Using the Add-In FluidLAB the property functions can be called in MATLAB<sup>®</sup>.



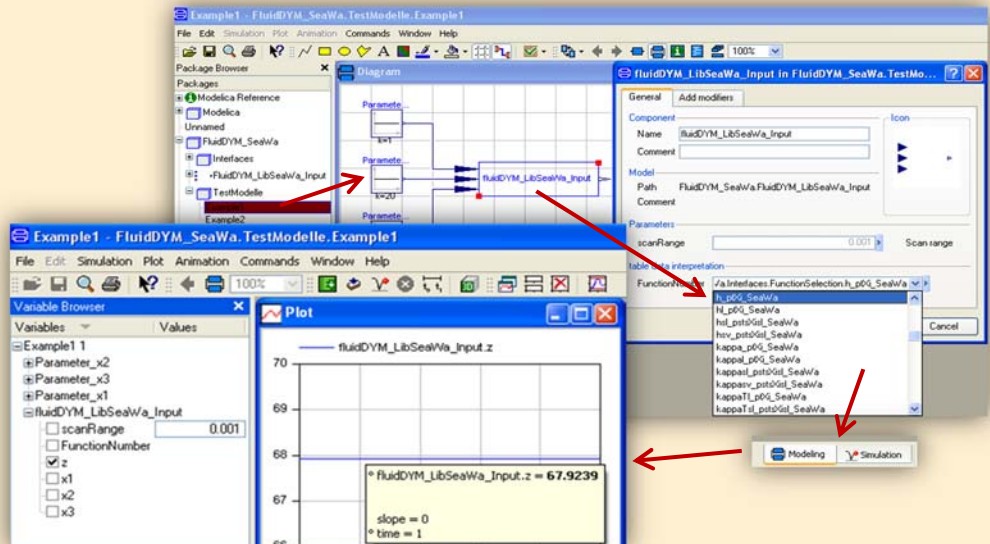
### Add-On FluidVIEW<sup>®</sup> for LabVIEW<sup>®</sup>

The property functions can be calculated in LabVIEW<sup>®</sup>.

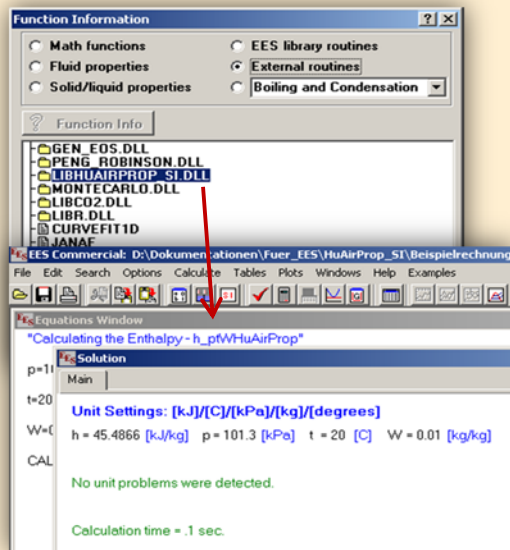


### Add-In FluidDYM<sup>®</sup> for DYMOLA<sup>®</sup> (Modelica) and SimulationX<sup>®</sup>

The property functions can be called in DYMOLA<sup>®</sup> and SimulationX<sup>®</sup>.



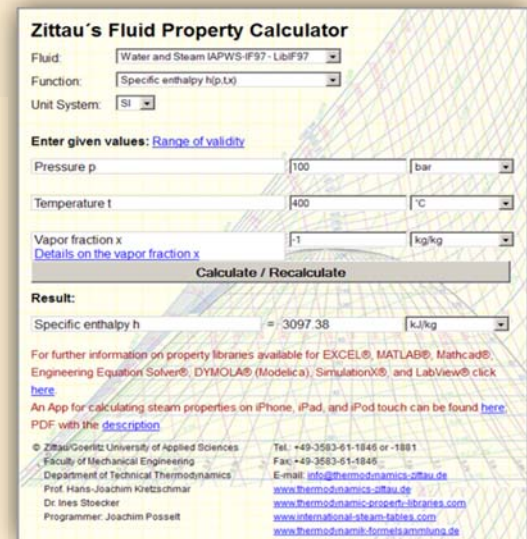
## Add-In FluidEES for Engineering Equation Solver®



## App International Steam Tables for iPhone, iPad, iPod touch, Android smart phones and tablets



## Online Property Calculator at [www.thermodynamics-zittau.de](http://www.thermodynamics-zittau.de)



## Property Software for Pocket Calculators

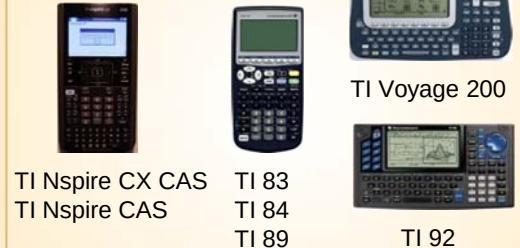
### FluidCasio



### FluidHP



### FluidTI



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The following thermodynamic and transport properties<sup>a</sup> can be calculated in Excel®, MATLAB®, Mathcad®, Engineering Equation Solver® EES, DYMOLA® (Modelica), SimulationX®, and LabVIEW®:

### Thermodynamic Properties

- Vapor pressure  $p_s$
- Saturation temperature  $T_s$
- Density  $\rho$
- Specific volume  $v$
- Enthalpy  $h$
- Internal energy  $u$
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- Dynamic viscosity  $\eta$
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- $p, T, v(h, s)$
- $p, T(v, h)$
- $p, T(v, u)$

### Thermodynamic Derivatives

- Partial derivatives can be calculated.

<sup>a</sup> Not all of these property functions are available in all property libraries.



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